Limiting Magnitudes of the Wide Field Survey Telescope (WFST)

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Abstract

Expected to be of the highest survey power telescope in the northern hemisphere, the Wide Field Survey Telescope (WFST) will begin its routine observations of the northern sky since 2023. WFST will produce a lot of scientific data to support the researches of time-domain astronomy, asteroids and the solar system, galaxy formation and cosmology and so on. We estimated that the 5σ limiting magnitudes of WFST with 30 s exposure are $u = 22.31$ mag, $g = 23.42$ mag, $r = 22.95$ mag, $i = 22.43$ mag, $z = 21.50$ mag, $w = 23.61$ mag. The above values are calculated for the conditions of airmass $= 1.2$, seeing $= 0''/75$, precipitable water vapor $= 2.5$ mm and Moon-object separation $= 45^\circ$ at the darkest New Moon night of the Lenghu site ($V = 22.30$ mag, Moon phase $\theta = 0^\circ$). The limiting magnitudes in different Moon phase conditions are also calculated. The calculations are based on the empirical transmittance data of WFST optics, the vendor provided CCD quantum efficiency, the atmospheric model transmittance and spectrum of the site. In the absence of measurement data such as sky transmittance and spectrum, we use model data.

Key words: surveys – telescopes – techniques: photometric

1. Introduction

The Wide Field Survey Telescope (WFST; Lou et al. 2016; Shi et al. 2018; Lou et al. 2020; Lin et al. 2022) is an optical telescope to be installed at the Lenghu site, located on the Saishiteng mountain near Lenghu Town in Qinghai Province on the Tibetan Plateau, China in 2023. The WFST has a 2.5 m diameter primary mirror and a 5-lens corrector to form a prime-focus optics (Wang et al. 2016; Lou et al. 2016; Lou et al. 2020). The detector of WFST consists of nine 9 K $\times$ 9 K CCD chips and has 0.9 Giga pixels. The entire system is optimized for the wavelength range from 3200 to 9600 Å (Lou et al. 2016; Chen et al. 2019). With the aid of an active optics system and an ADC (atmospheric dispersion compensator), WFST can achieve an image quality of 0′4 80% energy enclosed across a field of view of 3° diameter and ~7 deg² area. WFST is able to survey ~2 $\times$ 10^7 deg² northern sky in rgrizw six bands. As a powerful survey telescope, its scientific data will greatly support researches of time-domain astronomy, asteroids and the solar system, the Milky Way and its satellite dwarf galaxies, galaxy formation and cosmology and so on.

In recent years, many large ground-based optical survey telescopes have been built or planned all over the world. SDSS (Kent 1994; Fukugita et al. 1996), Pan-STARRS (Jedicke & Pan-STARRS 2007; Chambers & Team 2016), SkyMapper (Schmidt et al. 2005; Rakich et al. 2006), ZTF (Bellm 2014; Bellm et al. 2019; Graham et al. 2019) and other built telescopes have produced a large amount of observation data, which has greatly promoted astronomical researches and solved many scientific problems. Soon new, survey telescopes such as LSST (Hlozek et al. 2019), Mephisto (Liu 2019; Lei et al. 2021; Yuan et al. 2020) and WFST will join their peers and conduct deeper multi-band surveys to provide crucial data to astrophysical researches. Combined with China Space Station Telescope (CSST; Zhao et al. 2016; Yuan et al. 2021) and other space telescopes, WFST will greatly improve human understanding of the universe and promote more important scientific discoveries.

The parameters of a survey telescope, such as the diameter of the primary mirror, quantum efficiency (QE) of CCD, and band transmittance, determine the throughput of the telescope. The site conditions of an astronomical observatory, such as atmospheric transmittance, altitude, seeing and sky background brightness, affect the depth of a survey program. The limiting magnitude of a survey telescope is an important guide for planning research objectives and project scopes. It is also the key for designing exposure time plans and survey strategies. Therefore, an accurate estimation of the limiting magnitudes are needed for the successful commission of a new telescope.

In this work, we introduce the estimation of the limiting magnitudes of WFST. In Section 2 we describe the method that we adopt. In Section 3 we show our results of limiting magnitudes of the WFST.
2. Limiting Magnitudes

2.1. Throughput of WFST

The throughput of an astronomical observation \( T_{\text{tot}} \) is limited by the atmospheric transmittance \( T_{\text{atmo}} \), the transmittance of optics \( T_{\text{opt}} \), the transmittance of the filters \( T_{\text{band}} \) and the quantum efficiency of CCD \( QE_{\text{CCD}} \).

\[
T_{\text{tot}} = T_{\text{atmo}} \cdot T_{\text{opt}} \cdot T_{\text{band}} \cdot QE_{\text{CCD}} \quad (1)
\]

The optical system of WFST consists of a 2.5 m diameter primary mirror with a 760 mm diameter central hole, five corrector lenses, an ADC made with two glass wedges and \( ugrizw \) six switchable filters (Lou et al. 2016). Among five correcting lenses, only one is made of the N-BK7HT glass. The others and ADCs are made of the fused quartz. Since the transmittance of a fused quartz blank can be neglected, we simulate the total transmittance of the five-lens corrector and the ADC with the product of the transmittance of a 35 mm thick N-BK7 glass blank and the transmittance of 14 layers of anti-reflection (AR) coatings. The transmittance of the N-BK7 glass is obtained from SCHOTT and the transmittance of the AR coating is from Institute of Optics and Electronics (IOE)’s measurements. Because of the oversized Primary Focus Assembly (PFA), the actual aperture obscuration is 1 m diameter.

Because we do not have atmospheric transmittance and spectrum measurements at the site, we adopt SkyCalc (Version 2.0.9) to obtain model curves. SkyCalc is developed by astronomers in ESO based on the Cerro Paranal Advanced Sky Model (Noll et al. 2012; Jones et al. 2013; Moehler et al. 2014).

The atmospheric transmittance is affected by altitude, humidity, dust, and precipitable water vapor (PWV), among which the altitude is the most important factor. SkyCalc only provides the atmospheric transmittance at three astronomical sites: Paranal (2400 m), La Silla (2600 m) and the Extremely Large Telescope (ELT) site (3060 m). Figure 1 shows the three transmittance curves of the sites. We can see that three curves have same features that they are scaled according to different altitudes of three sites. This is reasonable because the geographic features of the three sites are very similar. The Paranal Observatory is on the Cerro Paranal mountain, which is in the Atacama Desert of northern Chile. The La Silla Observatory is located on the outskirts of the Chilean Atacama Desert. The 40 m-class ELT is on the Cerro Armazones mountain in the central part of the Atacama Desert. WFST is on the Saihhteng mountain in the Gobi desert area on the Tibetan Plateau. We consider that the geographic features of the area are more similar to those of sites in the high-altitude Atacama desert than those of oceanic mountain areas, such as Mauna Kea in Hawaii. It is a reasonable choice to obtain the atmospheric transmittance of the WFST site by using the spectra from SkyCalc. So we get the atmospheric transmittance curve of the WFST site at an altitude of 4200 m by scaling the atmospheric transmittance curves of paranal, lasilla and ELT sites. In our simulations, we assume that airmass = 1.0 and precipitable water vapor (PWV) = 2.5 mm. Figure 1 also shows the result of scaling.

As shown in Figure 2(a), combined system throughput, individual transmittance curves of the atmosphere and the corrector, the reflectivity of the primary mirror and the quantum
efficiency of the CCD are plotted respectively. We also plot the original estimate of the system throughput for WFST by Shi et al. (2018). We can see that the updated system throughput is higher than the early expectation in most wavelengths (Shi et al. 2018). The major reason is that the transmittances of the ADC and optical lenses are higher than the early estimate. In order to obtain high efficiency in short wavelengths, WFST selects e2v standard Si back-illuminated CCD detectors with the astro multi-2 coating. The QE of the CCDs is also increased.

Figure 2(b) shows the transmittance of the filters and the total throughput of WFST in six bands, which is calculated by using Equation (1).

2.2. Noise of WFST

Noise in astronomical CCD images mainly consists of the contributions from the artificial light on the ground, astrophysical sources, sky background, CCD dark current, and CCD readout noise. The site of WFST is on the Saishiteng mountain on the Tibetan Plateau, where the nearest residential area is Lenghu Town which is ~50 km from the observatory site and has a population of 200. There is no industrial activity and the ground light pollution. The Haixi Mongolian and Tibetan Autonomous Prefecture of Qinghai Province has announced the 17 800 square kilometres area of Lenghu as a dark night protecting region in the local law. It protects the good observational conditions of the Lenghu astronomical site. Deng et al. (2021) studied long-term astronomical conditions of the Lenghu site and pointed out that the sky background of a New Moon night can reach 22.3 mag arcsec−2 in the V band and the average night-sky brightness is around 22.0 mag arcsec−2 when the Moon is below the horizon. We adopt the AB magnitude system in this work.

The sky background spectrum of the Lenghu site is also calculated by the software SkyCalc (Noll et al. 2012; Jones et al. 2013; Moehler et al. 2014). The monthly averaged solar radio flux is equal to 130.00 sfu, that is the solar 10.7 cm radio flux in the Sun median active level (Sparavigna 2008; Petrova et al. 2021). Because the solar activities will affect the sky background brightness, it is necessary to take the solar activities into account when we estimate the sky background. We adopt the median values obtained from long-term solar monitoring programs as the baseline solar brightness. The spectral flux of one sky region is related to the Moon-Target separation and the Moon phase. We designate the Moon phase with the Moon phase angle (θ) 0° (New Moon), 45° (Waxing), 90° (Half Moon Waxing), 135° (Waxing), 180° (Full Moon) respectively. We assume that the separation of the Moon and a target is always 45° in our calculation. So the spectral flux of one region is only dependent on the altitude and the Moon phase. We get the sky background spectra under different Moon phase conditions at the Lenghu Observatory site by scaling the spectra of three ESO sites provided by SkyCalc. Figure 3(a) shows the sky background spectrum at the altitude of 4200 m (θ = 180°, here we just plot the spectra at a Full Moon night because it is easier to see their difference.), and the spectra of the three ESO sites at a Full Moon night. Figure 3(b) shows the sky spectra at Lenghu site under six different Moon phase conditions. As shown in the detail part of Figure 3(b), the sky background spectrum at a New Moon night (θ = 0°) and the sky spectrum at a dark night have almost the same flux.

We can get the magnitude $m_V$ by integrating the sky background spectrum multiplied by the V band filter transmission curve:

$$m_V = -2.5 \times \left( \log_{10} \frac{\int_0^\infty f_\lambda T_{band,\lambda} d\lambda}{\int_0^\infty T_{band,\lambda} d\lambda} \right) - 21.1 \quad (2)$$

where $f_\lambda$ is sky background spectral flux, $T_{band}$ is the Johnson V band transmission curve (Bessell 1990), and $ZP = -21.1$ is the
zero-point (Bessell & Murphy 2012). The modeled sky emission radiance flux from SkyCalc is in units of photon/s/m²/micron/arcsec². The Johnson V band sky background magnitude of a New Moon night with the SkyCalc model spectrum at an altitude of 4200 m is 21.74 mag arcsec⁻². We scale the 4200 m sky background spectrum so that the resulting spectrum has a V-band magnitude of 22.3 or 22.0 mag arcsec⁻², corresponding to the best and the average sky brightness conditions at the Lenghu site. As shown in Figure 3(b), there are differences among the sky spectra under different Moon phase conditions. We scale these sky spectra at different Moon phases use the the same scaling factor in the New Moon case, where we scale the spectrum from \( \theta = 0° = 21.74 \) to 22.30 mag arcsec⁻², so that differences among spectra at different Moon phases are not changed. The estimated V band Zenith sky background magnitudes at the Lenghu site with different Moon phases are:

- For \( \theta = 0° \), \( \theta = 45° \), \( \theta = 90° \), \( \theta = 135° \), \( \theta = 180° \), the sky background magnitudes are 22.30, 22.10, 21.29, 20.28, 18.90 mag arcsec⁻².

Table 1 shows the sky background magnitudes \( m_{AB} \) in WFST six bands.

### Table 1

<table>
<thead>
<tr>
<th>Moon Phases</th>
<th>u</th>
<th>g</th>
<th>r</th>
<th>i</th>
<th>z</th>
<th>w</th>
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<tbody>
<tr>
<td>0°</td>
<td>23.27</td>
<td>22.82</td>
<td>21.80</td>
<td>20.99</td>
<td>20.05</td>
<td>21.78</td>
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<tr>
<td>45°</td>
<td>23.02</td>
<td>22.49</td>
<td>21.66</td>
<td>20.93</td>
<td>20.03</td>
<td>21.64</td>
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<tr>
<td>90°</td>
<td>22.00</td>
<td>21.37</td>
<td>20.99</td>
<td>20.61</td>
<td>19.90</td>
<td>21.01</td>
</tr>
<tr>
<td>135°</td>
<td>20.86</td>
<td>20.21</td>
<td>20.08</td>
<td>20.01</td>
<td>19.61</td>
<td>20.12</td>
</tr>
<tr>
<td>180°</td>
<td>19.30</td>
<td>18.73</td>
<td>18.78</td>
<td>18.97</td>
<td>18.92</td>
<td>18.80</td>
</tr>
</tbody>
</table>

Note. The sky spectra is calculated by SkyCalc when airmass = 1.0, PWV = 2.5 mm. We calculated the sky background brightness \( m_{AB} \) when airmass = 1.2.

where

\[
ZP_{\text{band}} = \int_{0}^{\infty} \text{flux}_{AB} T_{\text{band}, \lambda} d\lambda
\]  

and

\[
\text{flux}_{AB} = 3631 \text{Jy for all frequencies}, \text{ and } T_{\text{band}, \lambda} \text{ is the transmittance curve of a particular band.}
\]

\[
\text{Sky}_{\text{band}} = \int_{0}^{\infty} f_{\lambda} T_{\text{band}, \lambda} d\lambda
\]

where \( f_{\lambda} \) is sky background spectral flux.

2.3. Limiting Magnitudes of WFST

Assuming the signal to noise ratio of WFST in all bands for a point source is \( S/N \), we can write the formula of the \( S/N \) as:

\[
\frac{S}{N} = \frac{S \cdot A \cdot \tau}{\sqrt{S \cdot A \cdot \tau + 2 \cdot n_{\text{pix}} \cdot [\text{Sky} \cdot A \cdot \alpha_{\text{pix}} + D] \cdot \tau + R^2}}
\]

where \( S \) is the source signal with a constant spectral flux, \( \tau \) is the standard exposure time (30 s), \( A \) is the effective area of the primary mirror (\( \sim 4.12 \times 10^4 \text{cm}^2 \)), \( \alpha_{\text{pix}} = 0.111 \text{ arcsec}^2 \) is the

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**Figure 3.** (a) The sky background spectrum (purple) at Zenith at the altitude of 4200 m in the Full Moon condition, and the spectra of three ESO sites when the Moon phase is \( \theta = 180° \). (b) The Zenith sky spectra of the 4200 m site in different Moon phase conditions. The sky background spectrum of Moon phase \( \theta = 180° \) and the spectrum of a dark night (when the Moon is under the horizon) have almost the same flux.
area of one pixel, \( D \) is the dark current of the CCD \( (D = 0.005 e^-/pixel/s, \, @-100^\circ C) \), \( R^2 \) is the readout noise of the CCD \( (R = 8 e^- \, \text{rms}) \), \( n_{\text{pix}} \) is the total pixel number in the point-spread function (PSF), the usage of a factor 2 is because we assume that the calculation is performed on sky subtracted images. An optimal PSF aperture of 1.18 times of the full width at half maximum (FWHM) is adopted for a non-Adaptive Optics case according to the Integration Time Calculator (ITC) of Gemini.\(^6\) The FWHM of the seeing degrades with the airmass and the wavelength as \( (\text{airmass})^{0.6} \times \lambda_{\text{eff}}^{0.2} \). Here \( \lambda_{\text{eff}} \) takes the value of 356.17, 476.34, 620.57, 753.07, 870.45, and 612.15 nm in the six bands ugrizw given by Equation (9).

\[
\lambda_{\text{eff}} = \int_0^{\infty} \lambda T_{\text{band}} d\lambda / \int_0^{\infty} T_{\text{band}} d\lambda
\]

We can solve Equation (8) to obtain the signal of an astronomical object required at the detection limit of \( S/N = 5 \) and find the corresponding limiting magnitude \( m_{\text{lim}} \):

\[
m_{\text{lim}} = -2.5 \times \log_{10} \left( \frac{S}{0.61 \times \text{ZP}_{\text{lim}}} \right)
\]  

Table 2 lists the calculated limiting magnitudes of ugrizw six bands. We calculated the limiting magnitudes of WFST at different Moon phases when the sky background brightness is \( V = 22.0 \, \text{mag} \) and 22.3 mag, respectively. The results of a single exposure of 30 s and of coadded 100 frames with a total integration time of 100 \( \times \) 30 s are listed. It shows that WFST can reach 23.42 (25.95) mag in the g band with a 30 s (100 \( \times \) 30 s) exposure under the conditions with the sky background brightness \( V = 22.3 \, \text{mag}, \, \text{seeing} = 0''75, \, \text{airmass} = 1.2 \) and PWV = 2.5 mm. If the sky background is \( V = 22.0 \, \text{mag}, \) the above values are 23.32 (25.85) mag for 30 s (100 \( \times \) 30 s).

\(^6\) https://www.gemini.edu/observing/resources/itm/itm-help
3. Discussion and Conclusions

In the current work, by considering the observational conditions of WFST, including throughput, quantum efficiency, the noise, the area of the primary mirror and the sky background brightness, we compute the limiting magnitudes of WFST. We get the sky background magnitudes in the AB magnitude system in the Lenghu site at the New Moon night when airmass = 1.2: u, g, r, i, z, w = 23.27, 22.82, 21.80, 20.99, 20.05, 21.78 mag arcsec$^{-2}$. For the Lenghu darkest night condition ($V = 22.3$ mag arcsec$^{-2}$) and a exposure time of 30 s, the 5σ limiting magnitudes of WFST are: $m_{\lim}$, $g_{\lim}$, $r_{\lim}$, $i_{\lim}$, $z_{\lim}$, $w_{\lim}$ = 22.31, 23.42, 22.95, 22.43, 21.50, 23.61 mag. The current estimates of limiting magnitudes are deeper than those in Shi et al. (2018). This is because the current total throughput of WFST is higher than the previous value, especially the throughput increases by ∼50% from ∼0.4 to ∼0.6 in $gri$ bands (see Figure 2(a)), and the current Dark night sky background is lower than the previous estimation. Figure 4 compares the sky spectrum of New Moon night of the Lenghu site and the atmospheric transmittance curve between this work and Shi et al. (2018). We used SkyCalc to estimate the sky background spectrum and atmospheric transmittance, while Shi et al. (2018) used the software MODTRAN$^7$ for estimating the atmospheric transmittance at the 5130 m Ali area and used a Hawaii sky background spectrum as a sky background spectral template. The Hawaii sky brightness in $ugz$ bands is brighter than the current model when we scaled both of them into the same conditions of $m_V = 22.3$ mag arcsec$^{-2}$ and airmass = 1.2 (see Figure 4 (a)), Shi et al. (2018) assumed the V band sky brightness is $m_V = 21.50$ mag arcsec$^{-2}$. There is little difference between the current atmospheric transmittance model and the spectrum in Shi et al. (2018) (see Figure 4(b)). Our scaled atmospheric transmittance is close to the model of MODTRAN.

We also obtain the limiting magnitudes of WFST under various conditions (Figure 5). In Figure 5, panel (a) shows the WFST limiting magnitudes of different signal-to-noise ratio when the exposure time equals to 30 s and 100 × 30 s respectively, panel (b) shows the limiting magnitudes of different seeing conditions when signal-to-noise ratio = 5 and the exposure time = 30 s, 100 × 30 s respectively, and panel (c) shows the 5σ limiting magnitudes of different exposure times. These results are calculated with the sky spectrum scaled into airmass = 1.2 condition at a New Moon night (Moon phase $\theta = 0^\circ$).

The WFST survey data will cover the entire northern sky. Its stacked scientific image data can be used to study asteroids, solar system, galaxies and cosmology. Its light curves can be used to discover variable objects. The estimated WFST limiting redshift of Type Ia supernovae (SNe Ia) can reach $z \sim 0.64$ (luminosity distance $\sim 6.3 \times 10^3$ Mpc) and $z \sim 1.67$ ($\sim 1.2 \times 10^4$ Mpc) when the exposure time is 30 s and 100 × 30 s. SNe Ia can be used to constrain the dark energy in the universe (Riess et al. 1998) and directly measure the Hubble constant (Riess et al. 2022). By simulating observations of the SNe Ia with the WFST at the Lenghu site, Hu et al. (2022) estimate that above $10^4$ pre-maximum SNe Ia will be discovered in one-year during the wide or deep observations, which suggests that WFST will be a powerful facility in revealing the physics of SNe Ia. Lin et al. (2022) computed the prospects of finding Tidal Disruption Events (TDEs) with the WFST. Their mock observations on 440 deg$^2$ field (CosmoDC2 catalog) show that ∼30 TDEs can be found per year in this field if observed at $ugri$ bands with 30 s exposures.

$^7$ http://modtran.spectral.com/
every 10 days. According to Gao et al. (2022), the event rate for galaxy-lensed orphan afterglows of γ-ray bursts (GRBs) is to be less than 0.7 yr⁻¹ for the whole sky survey of the WFST. Yu et al. (2021) estimated the multi-messenger detection rate of Binary Neutron Star Mergers is about 300–3500 yr⁻¹ with a GECAM-like detector for γ-ray emissions and an LSST/WFST detector for optical afterglows. Zhu et al. (2021) and Zhu et al. (2022) showed that the optimal detection rates of the KN-dominated and AG-dominated GRB afterglows events are ~0.2/0.5/0.8/20 yr⁻¹ and ~500/300/600/3000 yr⁻¹ for ZTF/Mephisto/WFST/LSST, respectively. There are also some studies looking forward to detecting active galactic nucleus (AGN) and researching AGN physics using WFST survey data (X.-F. Hu et al. 2023, in preparation, Su et al. 2023, in preparation).

There are large sky survey telescopes that have been built around the world, and a number of large sky survey telescopes are being built. These projects have produced or will generate a large amount of survey data and have an important impact in all fields of astronomy. Among them, the WFST will be completed in 2023. In the future, WFST (Lin et al. 2022; Shi et al. 2018), together with Mephisto (Lei et al. 2021; Lei et al. 2022; B.-Q. Chen et al. 2023, in preparation), Pan-STARRS (Jedicke & Pan-STARRS 2007; Chambers & Team 2016), SkyMapper (Schmidt et al. 2005; Rakich et al. 2006), ZTF (Bellm et al. 2019; Graham et al. 2019) and other telescopes will be able to carry out relay observations of the entire sky with large percentage time coverage, which will greatly enhance the development of the time-domain astronomy.

Acknowledgments

This work is supported by the Strategic Priority Research Program of Chinese Academy of Sciences (grant Nos. XDB 41000000 and XDB 41010105), the National Science Foundation of China (NSFC, grant Nos. 12233008, 12173037 and 11973038), the China Manned Space Project (No. CMS-CSST-2021-A07) and the Cyrus Chun Ying Tang Foundations. We thank Fredrik T Rantakyrö and Rodolfo Angeloni from Gemini Observatory for their patient elaboration on the Hawaii sky spectrum model and sky brightness measurements.

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References


Figure 5. (a) The limiting magnitudes of different S/N values when the exposure time is 30 s (dotted–dashed line) and 100 × 30 s (solid line); (b) The 5σ limiting magnitudes of different seeing conditions when the exposure time is 30 s (dotted–dashed line) and 100 × 30 s (solid line); (c) The 5σ limiting magnitudes of different exposure times when the seeing is 0°/75. The conditions for a New Moon night (θ = 0°) and airmass = 1.2. Note: The limiting magnitude curves of the g band (blue) and the w band (red) are so close that we cannot distinguish the two curves easily.