

Heavy element contributions of rotating massive stars to interstellar medium

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Abstract Employing the stellar evolution code Modules for Experiments in Stellar Astrophysics (MESA), we calculate yields of heavy elements from massive stars via stellar wind and core–collapse supernova (CCSN) ejecta to the interstellar medium (ISM). In our models, the initial masses (M_{ini}) of massive stars are taken from 13 to $80 M_{\odot}$, their initial rotational velocities (V) are 0, 300 and 500 km s^{-1} , and their metallicities are $[\text{Fe}/\text{H}] = -3, -2, -1$ and 0. The yields of heavy elements coming from stellar winds are mainly affected by stellar rotation which changes the chemical abundances of stellar surfaces via chemically homogeneous evolution, and enhances mass-loss rate. We estimate that the stellar wind can produce heavy element yields of about 10^{-2} (for low metallicity models) to a mass of several M_{\odot} (for low metallicity and rapid rotation models). The yields of heavy elements produced by CCSN ejecta also depend on the large amount of remnant mass which is mainly determined by the mass of the CO-core. Our models calculate that the yields of heavy elements produced by CCSN ejecta can get up to several M_{\odot} . Compared with stellar wind, CCSN ejecta has a greater contribution to the heavy elements in ISM. We also compare the ^{56}Ni yields calculated in this work with the observational estimate. Our models only explain the ^{56}Ni masses produced by faint SNe or normal SNe with progenitor mass lower than about $25 M_{\odot}$, and greatly underestimate the ^{56}Ni masses produced by stars with masses higher than about $30 M_{\odot}$.

Key words: Stars: massive — rotation — ISM: abundances

1 INTRODUCTION

The interstellar medium (ISM) has the following constituents: atomic, gas ions, dust grains, cosmic rays and also many molecules. Heavy elements are fundamental components in the ISM and play a critical role in the stellar evolution of astrophysics and chemical evolution in the ISM. It is well known that massive stars with an initial mass larger than $\sim 8 M_{\odot}$ play the most important role in producing heavy elements in the ISM (e.g., Dunne et al. 2003; Ablimit & Maeda 2018; Du 2020). These massive stars contribute to heavy elements via stellar wind and the ejecta of core–collapse supernovae (CCSNe). Although the heavy elements may originate from other sources including the stellar wind of asymptotic giant branch stars, ejecta of classical novae, binary merger, etc., their contribution is very low (Groenewegen & de Jong 1993; Marigo 2007; Hix 2001; Lü et al. 2013; Zhu et al. 2013; José et al. 2006; Li et al. 2016; Rukeya et al. 2017; Zhu et al. 2019; Duolikun et al. 2019; Shi et al. 2020; Guo et al. 2020).

The yields of heavy elements from massive stars have been investigated by many literatures (e.g., Woosley & Weaver 1995; Chieffi & Limongi 2004; Nomoto et al. 2006; Heger & Woosley 2010; Nomoto et al. 2013). However, these works do not consider mass loss which is very important for massive star evolution (A recent review can be seen in Smith 2014). Usually, the mass loss was thought to be caused by stellar wind driven by strong radiation (Castor et al. 1975; Puls et al. 2008). Simultaneously, it is also affected by metallicity and rotation (Vink 2000; Vink et al. 2001; Meynet 2000; Maeder & Meynet 2012). Because the efficiency of radiation pressure in removing the stellar envelope depends on metallicity, it has an effect on the mass-loss rates (\dot{M}) of massive stars by $\dot{M} \propto Z^m$, where the index range of m is from 0.5 to 0.94 (Vink 2000; Vink et al. 2001; Mokiem et al. 2007). Rotation can enhance the mass-loss rate (Langer et al. 1998; Heger 1998). More importantly, rapid rotation can result in quasi-chemically homogeneous evolution (CHE) induced by various instabilities, such as dynamical shear

instability, Solberg-Hiøland instability, secular shear instability, Eddington-Sweet circulation and Goldreich Schubert-Fricke instability (e.g., [Pinsonneault et al. 1989](#); [Heger & Langer 2000](#)). CHE can carry the heavy elements produced by nuclear burning in the core to the stellar surface, thus these heavy elements are able to enter the ISM via stellar wind (e.g., [Brott et al. 2011](#); [Song et al. 2016](#); [Cui et al. 2018](#)). The role of heavy element mixing is critical; it will affect the opacity of the envelope and increase the luminosity and effective temperature of the star ([Glebbeek et al. 2009](#)).

The standard non-rotating single-star model is strongly opposed as a possible progenitor of supernovae (SNe) ([Fremming et al. 2014](#); [Bersten & Nomoto 2014a](#)), but [Prantzos et al. \(2018\)](#) recently reported the heavy element yields of rotating massive stars. They considered effects of three initial rotational velocities, namely, 0, 150 and 300 km s⁻¹. Initial velocity above ~ 350 km s⁻¹ was more likely to attain the critical velocity ([Meynet & Maeder 2006](#)). Furthermore, in the VLT-FLAMES Tarantula Survey, [Dufton et al. \(2013\)](#) found that the projected rotational velocities of single early B-type stars can reach approximately 450 km s⁻¹. In binary systems, owing to mass transfer, rotation velocity will reach the Kepler velocity ([de Mink et al. 2013](#)).

Meanwhile, rapid rotation results in a more massive helium core via CHE ([Belczynski et al. 2016](#); [Eldridge & Maund 2016](#); [Mandel & De Mink 2016](#); [Marchant et al. 2016](#); [Wang et al. 2018](#)). On account of the helium-core, masses have strong effects on the remnant masses of neutron stars (NSs) and black holes (BHs) (e.g., [Hurley et al. 2000](#); [Belczynski et al. 2008](#)). At the pre-supernova (pre-SN) stage, a larger helium-core burning produces a bigger CO-core ([Meynet & Maeder 2006](#); [Köhler et al. 2015](#); [Marassi et al. 2019](#)). Hence, rotation as well affects the heavy elements in CCSN ejecta. Very recently, in order to study dust formation in CCSN ejecta, [Marassi et al. \(2019\)](#) considered the effects of rotation, metallicity and fallback, in computing the heavy element yields of massive stars. However, they still did not consider the yields via stellar wind.

Therefore, it is necessary to study the heavy element yields coming from stellar wind and CCSN ejecta for massive stars. Even research on the relevant factors of elemental abundance is very urgent. In this paper, we study the effects of metallicity, rotation and fallback on the contribution of heavy elements produced by massive stars. In Section 2, the input physical parameters in models are described. The detailed results are discussed in Section 3. The main conclusions appear in Section 4.

2 MODEL

We use the open-source stellar evolution code Modules for Experiments in Stellar Astrophysics (MESA, version 10108, model CCSN) to simulate massive star evolutions ([Paxton et al. 2011, 2013, 2015](#)). In these simulations, we select a 67–isotope network. The mixing-length parameter (α_{mlt}) is taken as 1.5 ([Brott et al. 2011](#); [Moravveji 2016](#); [Ma et al. 2020](#); [Shi et al. 2020](#)). In addition, the Ledoux criterion is connected with boundaries of convection, and semi-convection (α_{sc}) is selected as 0.02. Most of all, MESA has the Ledoux criterion $\nabla = \nabla_{\text{rad}}$ in the overshoot area, which is different from the deep overshoot method ([Maeder 1975](#); [Viallet et al. 2015](#)). Overshooting between the convective core and radiative one of the interior diffusion parameter is expressed by $f_{\text{ov}} = 0.05$. Another effective parameter ($f_{\text{o}} = 0.02$) is from the surface down to the overshoot layer ([Paxton et al. 2011](#); [Moravveji 2016](#); [Higgins & Vink 2019](#)). They are considered at all stages of evolution, and can also affect the total mass of stellar loss. Thermohaline mixing parameter (α_{th}) is equal to 2.0 ([Kippenhahn et al. 1980](#); [Paxton et al. 2013](#)). In this work, we rely on the formulae of [Vink et al. \(2001\)](#) to calculate the mass-loss rates. In addition, rotation can enhance mass-loss rate by

$$\dot{M}(\Omega) = \left(\frac{1}{1 - \Omega/\Omega_{\text{crit}}} \right)^{\gamma} \dot{M}(0), \quad (1)$$

where $\dot{M}(0)$ is the mass-loss rate without rotation, Ω and Ω_{crit} represent the angular velocity and critical Keplerian angular velocity, respectively, and parameter γ equals 0.43 ([Langer et al. 1998](#)). $\dot{M}(0)$ is calculated by the formulae in [Vink et al. \(2001\)](#). But when the angular velocity reaches the critical angular velocity, there will be a singularity. We limit the mass loss rate so that the mass loss time scale is longer than the thermal time scale of the star, see equations (1)–(3) in [Yoon et al. \(2012\)](#).

In order to discuss the effects of metallicity, the four initial metallicities are taken in different models as follows: [Fe/H]=0, [Fe/H]=-1, [Fe/H]=-2 and [Fe/H]=-3. Here, [Fe/H]=log[(Fe/H)/(Fe/H)_⊙] where [Fe/H]_⊙=0.02 is the solar metallicity ([Thielemann et al. 2010](#); [Chiaki et al. 2015](#)).

Considering that rotational velocity of massive stars may get up to the critical velocity ([de Mink et al. 2013](#)) at the stellar surface, we take the initial rotational velocities in different simulations as 0, 300 and 500 km s⁻¹, respectively. Rotation triggers some instabilities, then leads to angular momentum transport and chemical mixing (e.g., [Meynet 2012](#)). Based on the research of [Pinsonneault et al. \(1989\)](#), [Heger & Langer \(2000\)](#) and [Yoon & Langer \(2006\)](#), MESA considers the ratio of turbulent viscosity to the diffusion coefficient (f_c) and

the ratio of sensitivity to chemical gradients (f_μ) to calculate angular momentum transport and chemical mixing induced by rotation. [Zhu et al. \(2017\)](#) and [Cui et al. \(2018\)](#) employed MESA to investigate rotating massive stars. Following them, we choose $f_c = 0.0228$ and $f_\mu = 0.1$, respectively.

MESA code can calculate the stellar evolution from pre-main sequence to CCSN. However, it cannot give the remnant masses after CCSN. In our work, following [Hurley et al. \(2000\)](#); [Belczynski et al. \(2008\)](#); [Wang et al. \(2018\)](#) the remnant masses of an NS or BH are given by the CO-core mass. When applying the CCSNe model of MESA via collapse of a core when the mass of Fe core $> 1.4 M_\odot$, we do not consider nuclear reactions at this stage. The explosion mechanism of CCSNe is a complex process which still has not been explained well. In our model, the explosion energy (E) is 1×10^{51} erg ([Nomoto et al. 2007](#); [Paxton et al. 2013](#); [Hirschi et al. 2017](#); [Curtis et al. 2019](#)).

Simultaneously, a supernova explosion occurs when stellar central density reaches $7.9 \times 10^9 \text{ g cm}^{-3}$ and central temperature is $\sim 6.5 \times 10^9 \text{ K}$.

3 RESULTS

Using MESA code, we simulate the evolutions from main sequence (MS) to CCSN for eight massive stars with masses of 13, 15, 20, 25, 30, 40, 60 and $80 M_\odot$. In order to discuss the effects of rotation, the initial rotational velocities are taken as 0, 300 and 500 km s^{-1} in different simulations. In order to check our model, we compare the evolutions of several stars with those in [Brott et al. \(2011\)](#) under similar input parameters. Figure 1 affirms that the evolutionary tracks in two works are similar. All heavy elements originating from the star are produced by nucleosynthesis. They are ejected into the ISM via stellar wind and CCSN ejecta.

3.1 Heavy Elements Coming from Stellar Wind

Before massive stars trigger CCSNe, their heavy elements enter the ISM via stellar winds. These heavy elements are located in the stellar envelope. In this work, we estimate the yields of the i -th heavy element by

$$M_i = \int_0^{t_{\text{pre}}} \dot{M}(t) X_i(t) dt, \quad (2)$$

where t_{pre} is the time from zero-age MS to pre-CCSN, and $\dot{M}(t)$ and $X_i(t)$ are the mass-loss rate and the mass fraction of the i -th heavy element on the surface of the massive star, respectively. Therefore, the heavy elements coming from stellar wind mainly depend on the mass-loss rates and the chemical abundances on the stellar surface.

In our model, the mass-loss rates are affected by metallicity and rotational velocity. Figure 2 shows the

evolutions of mass-loss rates for different initial mass stars with different metallicities and rotational velocities.

Comparing the two metallicity models, a high metallicity can result in a high mass-loss rate because $\dot{M} \propto Z^m$, where parameter m ranges from 0.64 to 0.85 ([Vink et al. 2001](#)). Simultaneously, as the mass-loss rates depend on the rotational velocities by Equation (1) mainly in the MS stage, we also consider the red supergiant (RSG) or Wolf-Rayet (WR) stage ([Nugis & Lamers 2000](#)). Therefore, the higher the initial rotational velocity is, the higher the mass-loss rate is. The mass-loss rate can be enhanced about 1–4 magnitudes when the initial rotational velocity increases from 0 to 500 km s^{-1} . The chemical abundances on stellar surfaces are determined by CHE. During MS late phase, the star begins to rapidly expand, and the rotational velocity sharply decreases. Therefore, CHE mainly works in MS phase. The heavy elements affected by nucleosynthesis during the MS phase are ^{12}C , ^{14}N and ^{16}O (key elements in the evolution of massive stars).

Figure 3 displays the evolutions of heavy-element (^{12}C , ^{14}N and ^{16}O) abundances on the stellar surfaces. Obviously, if there is no CHE in models without rotation, the heavy-element abundances on the stellar surface are constant during its life. However, in rotational models, the abundances of elements ^{12}C , ^{14}N and ^{16}O on the stellar surfaces change. ^{12}C and ^{16}O abundances decrease, while ^{14}N abundance increases. In particular, the lower the metallicity is, the stronger CHE is. Therefore, for lower metallicity models, the range of increase and decrease in abundance is more obvious. In addition, for the $60 M_\odot$ panel, because the H-rich shell is stripped out before the RSG phase, the star enters the WR stage. As Figure 3 illustrates, elements ^{12}C and ^{16}O under the stellar surface strongly increase while the element ^{14}N decreases. Similar results have been discussed in [Maeder & Meynet \(2001\)](#), [Hirschi et al. \(2005\)](#), [Chieffi & Limongi \(2013\)](#), [Groh et al. \(2014\)](#) and [Meyer et al. \(2020\)](#).

Figure 4 depicts the yields of heavy elements (^{12}C , ^{14}N , ^{16}O and ^{56}Fe) produced via stellar winds. [Hirschi et al. \(2005b\)](#) also calculated the yields of heavy elements produced by stellar winds. In Table 3 for a model with $M_{\text{ini}} = 20 M_\odot$, $[\text{Fe}/\text{H}] = 0$ and $V = 300 \text{ km s}^{-1}$, [Hirschi et al. \(2005b\)](#) reported the yields of elements ^{12}C , ^{14}N and ^{16}O to be 1.73×10^{-2} , 4.30×10^{-2} and $2.75 \times 10^{-2} M_\odot$, respectively. Under similar input parameters, the yields in our models are 3.34×10^{-2} , 7.20×10^{-2} and $4.32 \times 10^{-2} M_\odot$, respectively. For a model with $M_{\text{ini}} = 40 M_\odot$, the corresponding values in [Hirschi et al. \(2005b\)](#) are 1.60, 1.73×10^{-1} and $3.34 \times 10^{-1} M_\odot$, respectively, while in our work they are 1.15, 1.74×10^{-1}

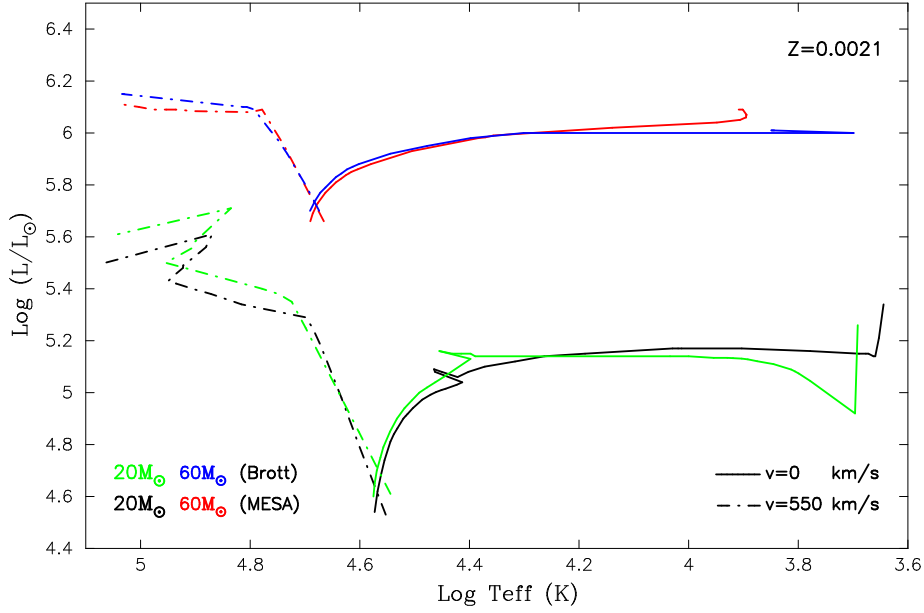


Fig. 1 The evolutions of massive stars with different masses and rotation velocities for $Z = 0.0021$. The *solid lines* represent a non-rotating star, while the *dash-dotted lines* signify a star with a rotation velocity of 550 km s^{-1} . *Green and blue lines* are the evolutionary tracks calculated by [Brott et al. \(2011\)](#), and *black and red lines* are simulated in our models.

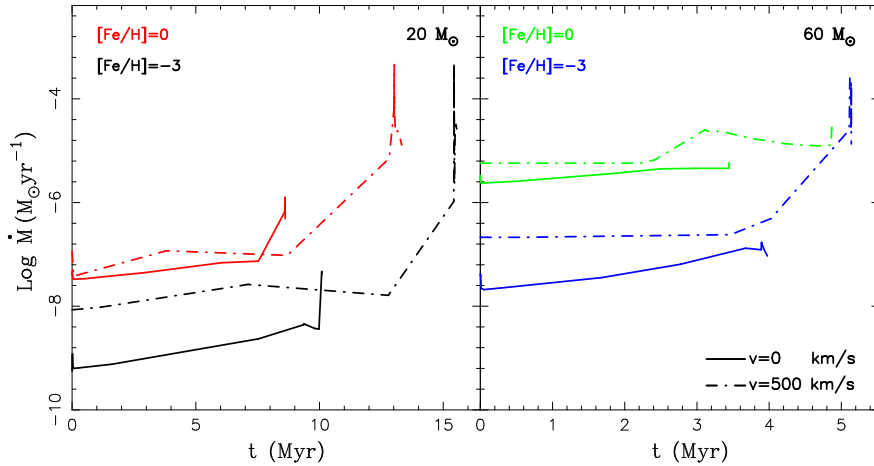


Fig. 2 The evolutions of mass-loss rates for models with different masses (20 and $60 M_{\odot}$), metallicities ($[\text{Fe}/\text{H}] = 0, -3$) and rotational velocities (0 and 500 km s^{-1}).

and $3.13 \times 10^{-1} M_{\odot}$, respectively. The results in both works are consistent.

In short, the yields of heavy elements coming from stellar winds can get to several M_{\odot} for high rotation and high metallicity, but they may only be $10^{-2} M_{\odot}$ for low rotation and low metallicity.

3.2 Heavy Elements Coming from SN Ejecta

The heavy elements located in stellar interiors are ejected into the ISM via CCSN. They are mainly determined by mass fractions before CCSN occurs. Figures 5 and 6 feature the fractions of different elements in the models. For models with a mass of $20 M_{\odot}$, rapid rotation can

enhance mass-loss rates. A star with $V = 500 \text{ km s}^{-1}$ loses the whole hydrogen envelope. Simultaneously, it can trigger CHE, producing a larger CO-core. Therefore, compared with a star without rotation, it has a more massive core before CCSN. The stars with low metallicity can undergo efficient CHE and have low mass-loss rate. Their CO-cores at pre-CCSN are larger than those for stars with high metallicity. Similar results appear in models with a $60 M_{\odot}$ star. These results are consistent with those in [van Marle et al. \(2007\)](#), [Tominaga \(2008\)](#) and [Limongi & Chieffi \(2018\)](#). During CCSN, massive stars eject a portion of their masses and leave compact objects (NSs or BHs). Generally, the remnant mass (M_{rem}) is calculated by CO-core mass (M_{CO}) (e.g., [Belczynski et al.](#)

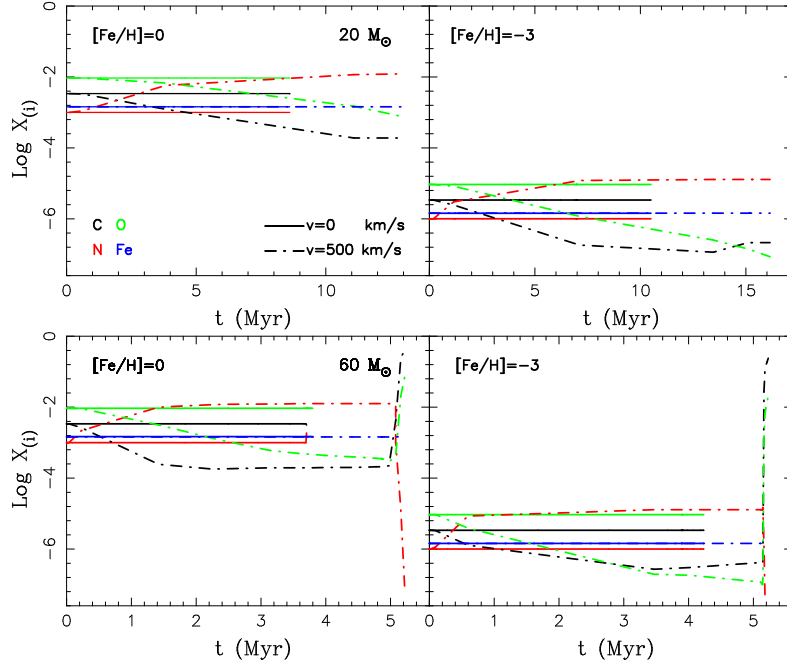


Fig. 3 The evolutions of heavy-element abundances [^{12}C (black), ^{14}N (red), ^{16}O (green) and ^{56}Fe (blue)] on the stellar surfaces for massive stars. The two panels in the top region represent the models with $20 M_{\odot}$, while the two panels in the bottom region are for $60 M_{\odot}$. The solid and dash-dotted lines represent the models with $V = 0$ and 500 km s^{-1} , respectively. The different metallicities are given in the left-top region of every panel.

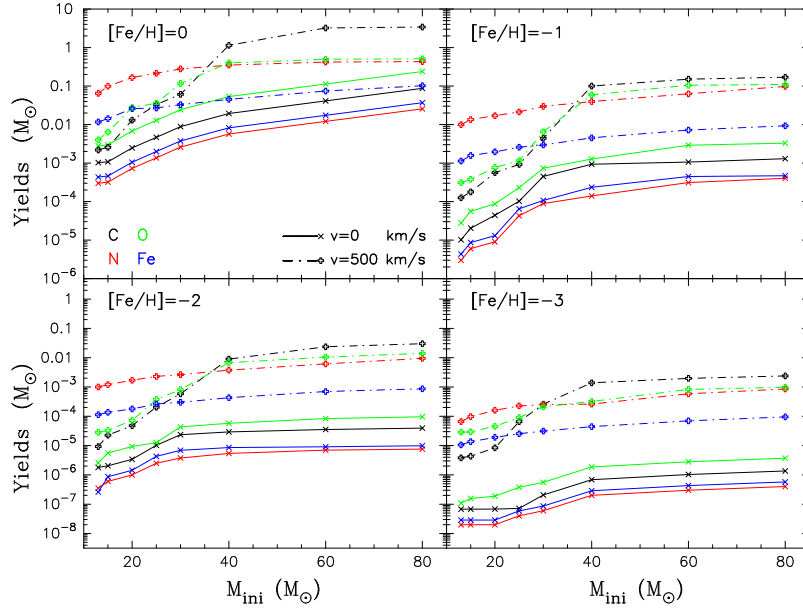


Fig. 4 The yields of the heavy elements, ^{12}C (black), ^{14}N (red), ^{16}O (green) and ^{56}Fe (blue), produced via stellar winds from massive stars with different initial masses, metallicities ($[\text{Fe}/\text{H}] = 0, -1, -2, -3$) and $V = 0, 500 \text{ km s}^{-1}$. The multiplication and addition symbols represent calculated models with $V = 0$ and 500 km s^{-1} , respectively.

2008). In this work, we rely on equations (1) to (4) in Belczynski et al. (2008) to calculate M_{rem} .

Figure 7(left) displays M_{CO} and M_{rem} calculated by different models. M_{CO} and M_{rem} are mainly determined by mass-loss rates. The stars with high metallicity and high rotational velocity have high mass-loss rates, and their

M_{CO} and M_{rem} hardly exceed $10 M_{\odot}$. CHE triggered by rapid rotation can only increase the M_{CO} and M_{rem} of models with initial masses lower than about $30 M_{\odot}$. We compare the CO-core with the Belczynski et al. (2008) model with a rotation of 300 km s^{-1} ; obviously the sizes of the CO-cores in the two models are consistent.

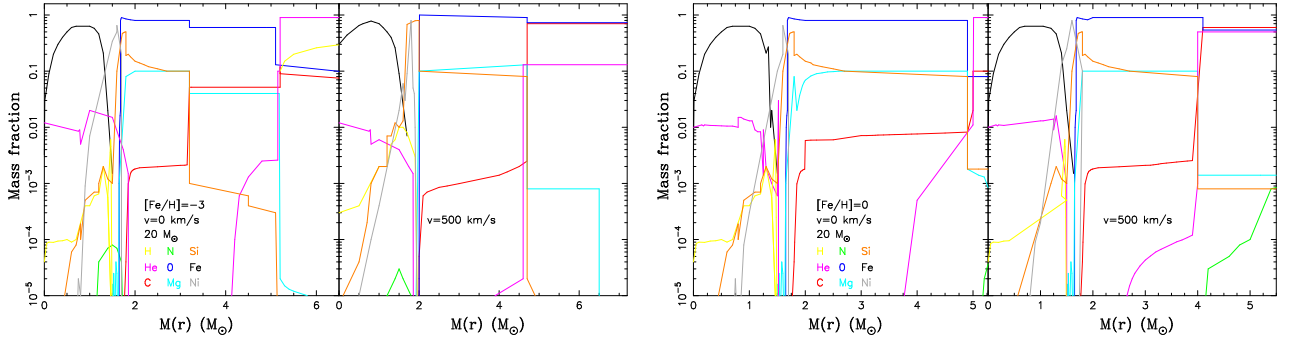


Fig. 5 The mass fractions of chemical elements in stellar interiors $[M(r)]$ at pre-CCSN for models with initial mass of $20 M_{\odot}$. The left two panels (the initial rotational velocities are 0 and 500 km s^{-1} in the *left* and *right* subpanels respectively) represent the models with $[\text{Fe}/\text{H}] = -3$, and the right two panels are for models with $[\text{Fe}/\text{H}] = 0$. The abundance of various chemical elements is represented by colored lines, for example, ^1H (yellow), ^{12}C (red), ^{14}N (green), etc.

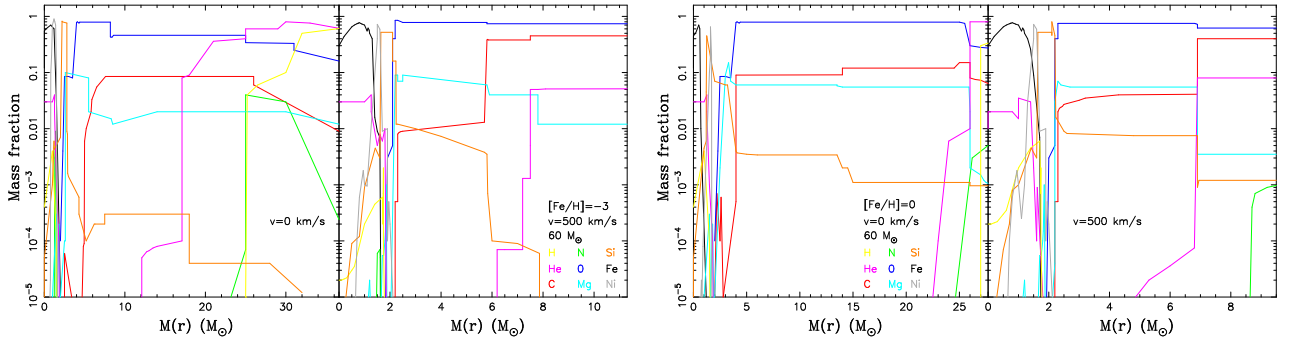


Fig. 6 Similar to Fig. 5 but for models with initial mass of $60 M_{\odot}$.

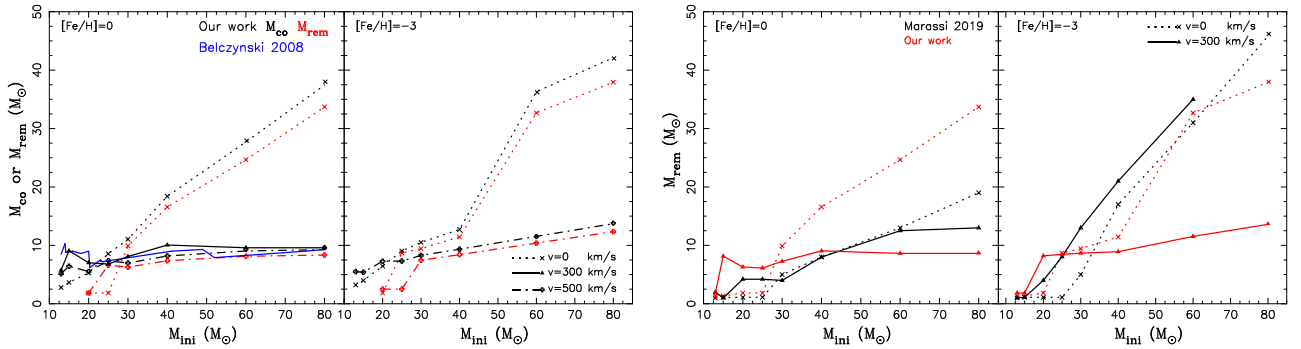


Fig. 7 *Left*: the CO-core (M_{CO}) and remnant (M_{rem}) masses vs. the initial masses in different models. The *black* and *red* lines represent M_{CO} and M_{rem} , respectively (Our work). The *solid blue* line signifies the CO-core size of the Belczynski et al. (2008) model with a rotation of 300 km s^{-1} . *Right*: comparison of the remnant masses in our work with those in Marassi et al. (2019). *Black* and *red* lines correspond to results from Marassi et al. (2019) and our work respectively.

Figure 7(right) compares M_{rem} calculated by this work with those in Marassi et al. (2019). Obviously, M_{rem} of stars with initial masses lower than about $30 M_{\odot}$ in our work is higher than that in Marassi et al. (2019), while others in our work are lower. The main reasons are mass-loss rates and the method for calculating remnant mass. For the former, as figure 2 in Marassi et al. (2019) demonstrates, the hydrogen envelope with a mass of about $3 M_{\odot}$ in the model with initial mass $60 M_{\odot}$ and $[\text{Fe}/\text{H}] = -$

1 is left before CCSN. However, under the model with $[\text{Fe}/\text{H}] = -1$, there is no hydrogen envelope for initial mass $60 M_{\odot}$ at pre-CCSN. For the latter, the remnant mass in Marassi et al. (2019) is determined by the initial mass and metallicity, while this work calculates M_{rem} via M_{CO} . Observation affirms that the CO nucleus will only appear when the gas density of the star reaches the standard value (Chen et al. 2006). The yield of the i -th element produced by CCSN ejecta can be calculated by explosion.

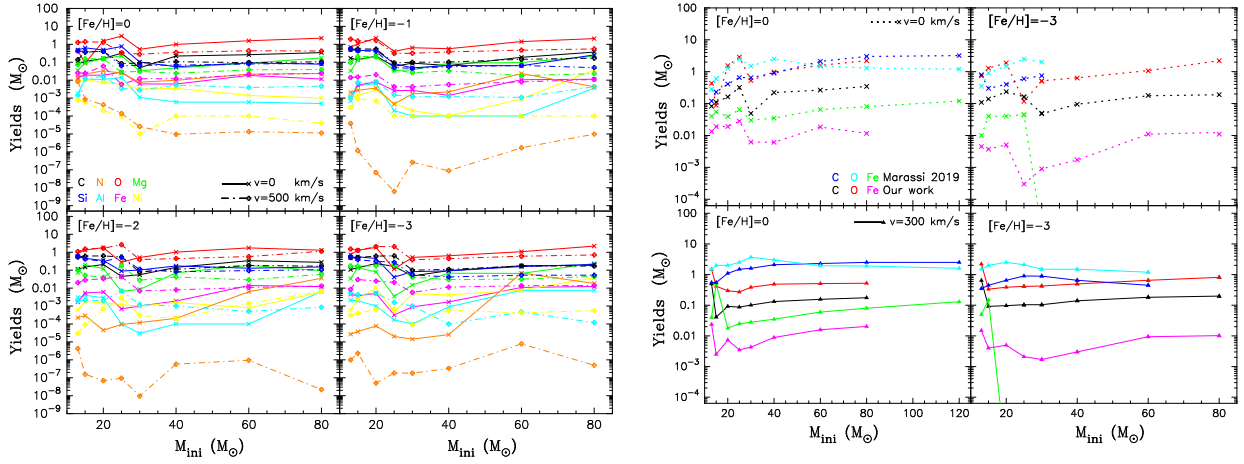


Fig. 8 Yields of heavy elements produced by CCSN ejecta. The *left* panel represents the results in this work. The *right* panel gives a comparison of our results with ones in [Marassi et al. \(2019\)](#).

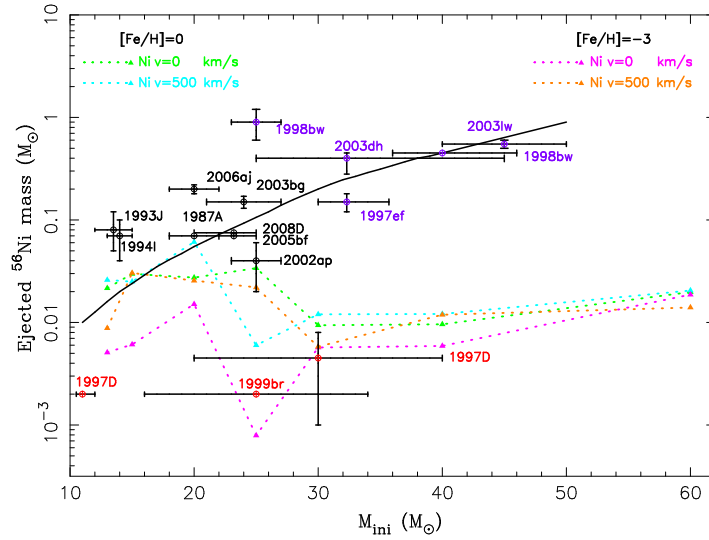


Fig. 9 The ^{56}Ni masses produced by CCSN ejecta and their progenitor masses at MS phase. These data come from [Nomoto et al. \(2013\)](#). The *red*, *black* and *purple* cycles represent faint SNe, normal SNe and hypernovae, respectively. The yields of ^{56}Ni calculated by our models are signified by *dotted lines* ($[\text{Fe}/\text{H}] = 0$) and *dashed lines* ($[\text{Fe}/\text{H}] = -3$). For example, the *green* and *blue* colors represent models with $V = 0$ and 500 km s^{-1} , respectively.

Figure 8 shows the yields of heavy elements produced by CCSN ejecta in this work.

$$M_i = \int_{M_{\text{rem}}}^{M_{\text{fin}}} [X_i(m) - X_i^0] dm, \quad (3)$$

where $X_i(m)$ is the i -th element mass fraction before the SN with Lagrangian coordinate m and X_i^0 is the initial abundance; the X_i^0 values of these elements are 0. M_{fin} is the final mass of the star ([Ekström et al. 2008](#)). However, compared with stellar winds (see Fig. 4), CCSN ejecta can produce more heavy elements, especially elements heavier than ^{16}O . Compared with [Marassi et al. \(2019\)](#), our work gives lower yields of heavy elements. The main reason is that our models have higher mass-loss rates. Before CCSN

occurs, the stars in our models have lost more mass than those in [Marassi et al. \(2019\)](#).

Via the comparison of observed light curves and theoretical models, [Nomoto et al. \(2013\)](#) estimated the ^{56}Ni masses produced by some CCSN ejecta and their progenitor masses, which are featured in Figure 9. Here, ^{56}Ni is caused by the decay of $^{56}\text{Ni} \rightarrow ^{56}\text{Co} \rightarrow ^{56}\text{Fe}$ ([Argast et al. 2002](#); [Hamuy 2003](#)). We calculate the yields of ^{56}Ni in the different initial mass models. Similar to the fixed energy models in [Marassi et al. \(2019\)](#), our results only explain the ^{56}Ni masses produced by faint SNe or normal SNe with progenitor masses lower than $25 M_{\odot}$. Clearly, our understanding of massive star evolution and the process involved in a CCSN is still poor.

4 CONCLUSIONS

In this work, we calculate the contribution of heavy elements from massive stars via stellar wind and CCSN ejecta to ISM.

In our models, the evolutions of massive stars are affected by rotation, mass-loss rate and metallicity. The rotation via CHE changes the chemical abundances of stellar surfaces, and enhances mass-loss rate. It can increase ^{14}N abundance by 10 times while decreasing ^{12}C and ^{16}O abundances by similar amounts. It can enhance the mass-loss rates by about 1–4 magnitude when the initial rotational velocity increases from 0 to 500 km s^{-1} . Therefore, the yields of heavy elements coming from stellar winds are mainly affected by stellar rotation. We estimate that the stellar wind can produce heavy element yields of about 10^{-2} (for low metallicity models) to a mass of several M_{\odot} (for low metallicity and rapid rotation models), which depends on stellar rotation and metallicity.

The yields of heavy elements produced by CCSN ejecta depend not only on rotation, mass-loss rate and metallicity, but also on the remnant mass of massive stars. Here, the latter mainly depends on the mass of the CO-core which is greatly affected by the above three parameters. Our models calculate that the yields of heavy elements produced by CCSN ejecta can reach a mass of up to several M_{\odot} . Compared with stellar wind, CCSN ejecta has a greater contribution to the heavy elements in ISM.

We also compare the ^{56}Ni yields calculated in this work with observational estimates. Our models only explain the ^{56}Ni masses produced by faint SNe or normal SNe with progenitor masses lower than about $25 M_{\odot}$, and greatly underestimate the ^{56}Ni masses produced by stars with initial masses higher than about $30 M_{\odot}$. It means that there is still a long way go in understanding massive star and CCSN evolution.

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