# New multi-color photometric investigations of solar-like contact binary V680 Per 

Jing-Jing Wang ${ }^{1,3}$, Jia-Jia He ${ }^{2,3}$ and Song-Qing Zhao ${ }^{1}$<br>${ }^{1}$ China University of Petroleum-Beijing at Karamay, Karamay 834000, China; wangjingjing @cupk.edu.cn<br>${ }^{2}$ Yunnan Observatories, Chinese Academy of Sciences, Kunming 650216, China<br>${ }^{3}$ Key Laboratory of the Structure and Evolution of Celestial Objects, Chinese Academy of Sciences, Kunming 650216, China

Received 2019 November 15; accepted 2020 December 18


#### Abstract

High-precision CCD photometric observations of the contact binary V680 Per were obtained in 2016. Its symmetric multi-color light curves were analyzed by using the Wilson-Devinney (2013) program. These photometric solutions suggest that V680 Per is an A-type W UMa contact binary with the mass ratio of $q=0.693$ and a fill-out factor of $f=18.84 \%$ with a small temperature difference of 101 K . Based on all minimum times, the $O-C$ curve was analyzed for the first time in this study. A cyclic oscillation $\left(A_{3}=0.00093 \mathrm{~d}, T_{3}=4.92 \mathrm{yr}\right)$ superimposed on a secular decrease $\left(d P / d t=-8.16 \times 10^{-8} \mathrm{~d} \mathrm{yr}^{-1}\right)$ was identified. The continuous decrease in period is possibly a result of mass transfer from the more massive component to the less massive one, or angular momentum loss due to a magnetic stellar wind. Because of this secular decrease, it is predicted that the degree of contact will become higher, and V680 Per will evolve into a deeper overcontact binary.


Key words: binaries : eclipsing - stars: solar-type stars: individual (V680 Per)

## 1 INTRODUCTION

W UMa-type eclipsing binaries usually consist of two ellipsoidal FGK dwarfs, the components of which fil1 their critical Roche lobes, and sharing a common convective envelope (CCE). Thanks to plentiful photometric and spectroscopic data, a large number of these systems were discovered from survey projects, such as: LAMOST (Qian et al. 2017), OGLE (Rucinski 1997), Catalina Sky Survey (Drake et al. 2009 and ASAS (Gettel et al. 2006). Statistical studies show that most W UMa-type binaries are solar-type main-sequence stars that undergo the protonproton ( $p-p$ ) chain nuclear reaction in their stellar cores. However, the formation and evolution of W UMa contact binaries are still unclear. Some investigators assumed these binaries form from short-period detached binaries through angular momentum loss (Guinan \& Bradstreet 1988; Bradstreet \& Guinan 1994; Zhu et al. 2004; Zhu \& Qian 2006). Also, the third bodies may play a significant role in the origin of contact binaries by removing angular momentum from the central binary through early dynamical interaction and/or later evolution (Qian et al. 2014b; Zhu et al. 2013b). To understand these, it is necessary to s-
tudy low mass solar-type binaries and their additional companions.

V680 Per (= GSC 2336 0281) is a W UMa contact binary discovered by Zejda (2002), the orbital period of which was found to be 0.3739783 d. Samec et al. (2005) analyzed $U B V R_{c} I_{c}$-band light curves, and concluded that V680 Per is a W-type W UMa binary with a temperature difference of about 100 K and a cool spot on the more massive, cooler component. Up to now, the orbital period investigation of this system was ignored. There are some CCD minimum times from literatures that were recorded during the last 17 yr , and we obtained new higher precision light curves. In this paper, orbital period variations of V680 Per are analyzed and the corresponding photometric solution is re-obtained. Based on the properties of period change and derived parameters, the ternary nature, evolution and configuration are discussed.

## 2 OBSERVATIONS

The four-color photometric observations of V680 Per were carried out in two nights on January 11 and 13 in 2016, with the $1024 \times 1024$ PI1024 BFT CCD

Table 1 Coordinates of the Contact Binary V680 Per (V), and the Comparison (C) and Check Stars (Ch).

| Stars | $\alpha_{2000}$ | $\delta_{2000}$ | $V_{\mathrm{mag}}$ |
| :---: | :---: | :---: | :---: |
| V680 Per (V) | $02^{\mathrm{h}} 41^{\mathrm{m}} 41^{\mathrm{s}}$ | $+35^{\circ} 42^{\prime} 54^{\prime \prime} .9$ | 13.49 |
| TYC 2336-5891(C) | $02^{\mathrm{h}} 41^{\mathrm{m}} 57^{\mathrm{s}}$ | $+35^{\circ} 45^{\prime} 59^{\prime \prime} .5$ | 10.06 |
| TYC 2336-2411 (Ch) | $02^{\mathrm{h}} 41^{\mathrm{m}} 31^{\mathrm{s}}$ | $+35^{\circ} 49^{\prime} 06^{\prime \prime} .8$ | 10.77 |

camera attached to the $85-\mathrm{cm}$ telescope at Xinglong Station of National Astronomical Observatories, Chinese Academy of Sciences. The effective field of view was $16.5 \operatorname{arcmin} \times 16.5 \mathrm{arcmin}$, and the filter system was a standard Johnson-Cousins-Bessel multi-color CCD photometric system mounted at the primary focus (Zhou et al. 2009). The integration times were 20 s for $B$ band, 15 s for $V$ band, 10 s for $R_{c}$ band and 8 s for $I_{c}$ band. The variable (V), comparison star (C) and check star (Ch) are shown in Figure 1, and their coordinates and magnitudes are listed in Table 1. In observations, we used differential photometry to obtain light curves of V680 Per which are displayed in the upper panel of Figure 2. The PHOT task in the IRAF aperture photometry package was applied to reduce the observed images, including a flat field correction process (Kallrath \& Milone 1999). The mean photometric errors for individual observations are 0.0020 mag in the $B I_{c}$ band and 0.0015 mag in $V R_{c}$ band.

With the linear ephemeris equation,

$$
\text { Min.I }(H J D)=2457401.0543+0^{\mathrm{d}} .37422033 \times E,(1)
$$

the $B V R_{c} I_{c}$ light curves along with their magnitudes and phases are displayed in Figure 2. In the lower panel of Figure 2, the differential magnitudes between the comparison star (C) and check star (Ch) are almost stable, which hints that the observational conditions are good. From our new observations, we can see that the light curves of V680 Per are nearly symmetric, and belong to the EWtype. These curves allow us to obtain more reliable photometric solutions.

To get more times of light minimum, we also monitored it with the $60-\mathrm{cm}$ and $1.0-\mathrm{m}$ telescopes managed by Yunnan Observatories (YNO). These two telescopes were equipped with the same Cassegrain-focus multicolor CCD photometer, where an Andor DW436 2K CCD camera was employed. These CCD times of minimum light were determined and are listed in Table 2.

## 3 VARIATIONS OF THE $O-C$ DIAGRAM

The orbital period changes are one important tool to understand the evolution of contact binary stars, for example, AL Cas (Qian et al. 2014a), LU Lac (Liao et al. 2014) and RV Psc (He \& Qian 2009). Since V680 Per was discovered in 2002 (Zejda 2002), there are some CCD times
of minimum light, without visual or photographic ones. Considering the technology implemented in a CCD and some times of minimum without errors, we assigned the same weight to these times to describe the trend of the $O-C$ (Sterken 2005). In our present work, all available times of minimum light are collected. Minimum times with the same epoch have been averaged, and only the mean values are listed in Table 2.

By using the ephemeris expressed in Equation (1), we calculated the $(O-C)_{1}$ values, which are plotted in the upper panel of Figure 3. To explore the variations in $(O-C)_{1}$, we performed some tests such as linear ephemeris term, parabolic term, cyclic term and parabolic plus cyclic term to fit all of these data. The residuals of the different fittings are listed in Table 3, suggesting the cyclic plus parabolic ephemeris to be reliable.

Based on the least-squares method, a cyclic plus parabolic term yields the following equation (Sterken 2005; Irwin 1952),

$$
\begin{equation*}
T=T_{0}+P_{0} E+\frac{1}{2} \frac{d P}{d t} P E^{2}+A_{3} \sin (\omega E+\phi) \tag{2}
\end{equation*}
$$

where $A_{3}$ is the amplitude of the sinusoidal variation, $T_{3}$ the period of the cycle, $\omega\left(=\frac{360^{\circ}}{T_{3}} P\right)$ the angle per unit epoch and $\phi$ the phase. We obtained the new ephemeris

$$
\begin{align*}
\text { Min.I }(H J D) & =2457401.0534( \pm 0.0002) \\
& +0 .^{\mathrm{d}} 37421962( \pm 0.00000007) \times E \\
& -4.18( \pm 0.49) \times 10^{-11} \times E^{2} \\
& +0.00093( \pm 0.00019) \sin \left[0^{\circ} .075022 \times E\right. \\
& \left.+77^{\circ} .74\left( \pm 14^{\circ} .30\right)\right] . \tag{3}
\end{align*}
$$

As displayed in the upper panel of Figure 3, the general trend of the $(O-C)_{1}$ curve manifests a downward parabolic change, indicating that the period is continuously decreasing. After the long-term decrease was removed from the $(O-C)_{1}$ curve, we found there is a periodic variation displayed in the middle of Figure 3.

The parabolic term in this ephemeris indicates a longterm period decrease at a rate of $d P / d t=-8.16 \times$ $10^{-8} \mathrm{~d} \mathrm{yr}^{-1}$. In the middle panel, the red solid line represents the oscillation with an amplitude of 0.00093 d and a period of 4.92 yr . The corresponding residuals from the whole fitting are displayed in the lower panel of Figure 3.

## 4 PHOTOMETRIC SOLUTIONS WITH THE WILSON-DEVINNEY PROGRAM

By modeling with Binary Maker 2.0, the preliminary solutions from Samec et al. (2005) revealed that the system was a W-type, W UMa binary with $q=M_{2} / M_{1}=$ 0.418 , and a temperature difference of $\Delta T=T_{1}-T_{2}=$


Fig. 1 Observed CCD images of V680 Per (V), and the comparison (C) and check stars (Ch).


Fig. 2 Upper: $B V R_{c} I_{c}$-band observations of V680 Per in 2016, with 85-cm telescope at Xinglong Station. For each subgraph: blue refers to the $B$-band magnitudes of the variable star minus the comparison star (V-C), black to the $V$-band, red to the $R_{c}$-band and green to the $I_{c}$-band. Lower: $B V R_{c} I_{c}$-band magnitudes of the comparison star minus the check star (C-Ch).
$5500 \mathrm{~K}-5608 \mathrm{~K}=-108 \mathrm{~K}$. To account for intercomponent mass flow or streaming in the "neck" of the Roche Lobe, we also added a cool spot on the more massive, cooler component. Our higher precision observations shown in Figure 2 are typical for EW-type variations as these light curves are from Samec et al. (2005). The depths between the primary and secondary minima are nearly the same. Besides, because the heights between two maxima are equal, there is no obvious O'Connell effect. In order to in-
vestigate the magnetic activities and understand their evolution, we intend to analyze the present multi-color light curves that were acquired in 2016. The photometric solutions are derived with the Wilson-Devinney program (WD), version 2013 (Wilson \& Devinney 1971; Wilson 1979; Wilson 1990; Van Hamme \& Wilson 2007; Wilson 2008).

According to the LAMOST spectral type of F5V, the temperature was fixed to be $T=6140 \mathrm{~K}$ in 2012 and $T=6067 \mathrm{~K}$ in 2016 (Qian et al. 2017), so we took the

Table $2 O-C$ Values of Light Minimum Times for V680 Per

| HJD Epoch | $(O-C)_{1}$ | $(\mathrm{O}-\mathrm{C})_{2}$ | Residuals | Errors Ref. | HJD | Epoch | $(O-C)_{1}$ | $(\mathrm{O}-\mathrm{C})_{2}$ | Residuals | Errors | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2451550.3066-15634.5 | 0.000049 | -0.000704 | -0.001089 | 0.0031 Zejda (2002) | 2454838.0219 | -6849.0 | 0.002640 | 0.001025 | 0.000805 | None | $O-C$ Gateway |
| 2451576.3166-15565.0 | 0.001736 | 0.000962 | 0.000454 | 0.0045 Zejda (2002) | 2454843.0732 | -6835.5 | 0.001966 | 0.000352 | 0.000096 | None | $O-C$ Gateway |
| 2451771.4714-15043.5 | 0.000634 | -0.000287 | 0.000002 | 0.0055 Zejda (2002) | 2455114.9429 | -6109.0 | 0.000596 | -0.000932 | -0.0004 | 0.0006 | Diethelm (2010) |
| 2451841.4510-14856.5 | 0.001033 | 0.000062 | 0.000636 | 0.0019 Zejda (2002) | 2455119.8090 | -6096.0 | 0.001832 | 0.000305 | 0.000789 | 0.002 | iethelm (2010) |
| 2451841.6388-14856.0 | 0.001722 | 0.000752 | 0.001326 | 0.0014 Zejda (2002) | 2455119.99 | -6095.5 | 0.000722 | -0.000805 | -0.00 | 0.0002 | Diethelm (2010) |
| 2451876.4423-14763.0 | 0.002732 | 0.001737 | 0.002281 | 0.0016 Zejda (2002) | 2455121.8660 | -6090.5 | 0.000620 | -0.000906 | -0.0004 | . 000 | Diethelm (2010) |
| 2452995.7337-11772.0 | 0.001125 | -0.000438 | -0.000944 | .0003 Faulkner et al. (2004) | 2455171.8248 | -5957.0 | 0.001006 | -0.000501 | 0.000074 | 0.000 | Nelson (2010) |
| 2452996.6688-11769.5 | 0.000674 | -0.000889 | -0.001399 | 0.0006 Faulkner et al. (2004) | 2455847.8558 | -4150.5 | 0.002980 | 0.001801 | 0.001256 | 0.001 | Diethelm (2012) |
| 2451924.3389-14635.0 | $-0.000870$ | -0.001898 | -0.00157 | 0.0020 Zejda (2004) | 2455859.26 | -4120.0 | 0.000560 | -0.000612 | -0.001 | 0.0015 | ubscher \& Lehmann (2012) |
| 2452133.5310-14076.0 | 0.002065 | 0.000904 | 0.000432 | 0.0018 Zejda (2004) | 2455859.4552 | -4119.5 | 0.001549 | 0.000378 | -0.00019 | 0.001 | Hubscher \& Lehmann (2012) |
| 2452138.5820-14062.5 | 0.001091 | -0.000074 | -0.000522 | 0.0024 Zejda (2004) | 2455894.2583 | -4026.5 | 0.002159 | 0.001008 | 0.000452 | 0.000 | Hubscher \& Lehmann (2012) |
| 2452147.5654-14038.5 | 0.003203 | 0.002033 | 0.001631 | 0.0033 Zejda (2004) | 2455894.4451 | -4026.0 | 0.001849 | 0.000698 | 0.000142 | 0.001 | Hubscher \& Lehmann (2012) |
| 2452198.4573-13902.5 | 0.001138 | -0.000062 | -0.00011 | 0.0033 Zejda (2004) | 2456214.9626 | -3169.5 | -0.000364 | -0.001302 | -0.00119 | 0.000 | Diethelm (2013) |
| 2452198.6443-13902.0 | 0.001028 | -0.000172 | -0.00022 | 0.0036 Zejda (2004) | 2457301.1389 | -267.0 | 0.001428 | 0.001456 | 0.000880 | None | $O-C$ Gateway |
| 2452213.4252-13862.5 | 0.000225 | -0.000984 | -0.000922 | 0.0049 Zejda (2004) | 2457301.3243 | -266.5 | -0.000282 | -0.000254 | -0.000829 | None | $O-C$ Gateway |
| 2452213.6141-13862.0 | 0.002014 | 0.000806 | 0.000869 | 0.0030 Zejda (2004) | 2457302.2624 | -264.0 | 0.002267 | 0.002296 | 0.001722 | None | $O-C$ Gateway |
| 2452521.5980-13039.0 | 0.002583 | 0.001211 | 0.000708 | 0.0020 Zejda (2004) | 2457732.9881 | 887.0 | 0.000367 | 0.000885 | 0.000364 | None | $O-C$ Gateway |
| 2452524.5904-13031.0 | 0.001220 | -0.000153 | -0.000667 | 0.0035 Zejda (2004) | 2458037.2260 | 1700.0 | -0.002861 | -0.001962 | -0.001441 | None | $O-C$ Gateway |
| 2452229.3309-13820.0 | 0.001561 | 0.000343 | 0.000524 | 0.0042 Zejda (2004) | 2455914.091 | -3973.5 | 0.001581 | 0.000443 | -0.00005 | . 000 | Present paper |
| 2452229.5196-13819.5 | 0.003150 | 0.001933 | 0.002115 | 0.0040 Zejda (2004) | 2457021.034 | -1015.5 | 0.001145 | 0.000887 | 0.001402 | 0.000 | Present paper |
| 2452234.5703-13806.0 | 0.001876 | 0.000655 | 0.000874 | 0.0032 Zejda (2004) | 2457398.9959 | -5.5 | -0.000188 | -0.000055 | $-0.0001$ | 00 | Present paper |
| 2452900.4943-12026.5 | 0.000799 | -0.000731 | -0.00061 | 0.0038 Zejda (2004) | 2457399.1831 | -5.0 | -0.000098 | 0.000036 | -0.000060 | 00 | Present paper |
| 2452999.8481-11761.0 | -0.000899 | -0.002463 | -0.00298 | 0.0004 Samec et al. (2005) | 2457401.0543 | 0.0 | 0.000000 | 0.000136 | 0.000054 | 0.000 | Present paper |
| 2452999.6624-11761.5 | 0.000511 | -0.001052 | -0.001573 | 0.0008 Samec et al. (2005) | 2458385.2497 | 2630.0 | -0.004068 | -0.002696 | -0.00249 | 000 | Present paper |
| 2453290.6198-10984.0 | 0.001605 | -0.000040 | 0.000518 | 0.0003 Zejda et al. (2006) | 2458425.1047 | 2736.5 | -0.003533 | -0.000395 | 0.000511 | 0.000 | Present paper |
| $2453713.3030-9854.5$ | 0.002942 | 0.001229 | 0.001761 | 0.0004 Zejda et al. (2006) | 2458455.0408 | 2816.5 | -0.005059 | -0.001846 | -0.000966 | 0.000 | Present paper |
| 2455543.6134-4963.5 | 0.001708 | 0.000363 | 0.000553 | 0.0003 Diethelm (2011) | 2458457.1004 | 2822.0 | -0.003671 | -0.000452 | 0.000425 | 0.000 | Present paper |
| 2453262.9265-11058.0 | 0.000609 | -0.001029 | -0.000453 | 0.0002 Krajci (2006) | 2458458.0332 | 2824.5 | -0.006422 | -0.003201 | $-0.002324$ | 0.0003 | Present paper |
| $2454793.8643-6967.0$ | 0.003039 | 0.001413 | 0.001525 | 0.0002 Nelson (2009) |  |  |  |  |  |  |  |

Table 3 Fitting Residuals of Different Ephemeris Terms for $(O-C)_{1}$

| Linear | Parabolic | Cyclic | Parabolic+Cyclic |
| :---: | :---: | :---: | :---: |
| $1.6803 \times 10^{-6}$ | $1.2497 \times 10^{-6}$ | $1.7261 \times 10^{-6}$ | $1.0484 \times 10^{-6}$ |



Fig. 3 The $O-C$ diagram for V680 Per. Top panel: the dotted line represents the quadratic trend and the solid line signifies the cyclic trend. Middle panel: the solid line corresponds to the cyclic change. Bottom panel: the residuals with respect to Equation (3).


Fig. 4 Relation between $\Sigma$ and $q$. The minimum residual is achieved at $q=0.70$.
Table 4 Photometric Solutions of V680 Per

| Parameters | Photometric <br> elements | Errors | Parameters | Photometric <br> elements | Errors |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $g_{1}=g_{2}$ | 0.32 | Assumed | $L_{1} /\left(L_{1}+L_{2}\right)(B)$ | 0.6051 | $\pm 0.0005$ |
| $A_{1}=A_{2}$ | 0.5 | Assumed | $L_{1} /\left(L_{1}+L_{2}\right)(V)$ | 0.5991 | $\pm 0.0005$ |
| $\mathbf{L D}$ | -3 | Assumed | $L_{1} /\left(L_{1}+L_{2}\right)\left(R_{c}\right)$ | 0.5963 | $\pm 0.0005$ |
| $x_{1 \text { bol }}, y_{1 \text { bol }}$ | $0.541,0.172$ | Assumed | $L_{1} /\left(L_{1}+L_{2}\right)\left(I_{c}\right)$ | 0.5940 | $\pm 0.0006$ |
| $x_{2 \text { bol }}, y_{2 \text { bol }}$ | $0.638,0.163$ | Assumed | $r_{1}$ (pole) | 0.3980 | $\pm 0.0017$ |
| $T_{1}$ | $6104 K$ | Assumed | $r_{1}$ (side) | 0.4225 | $\pm 0.0022$ |
| $T_{2}$ | $6003 K$ | $\pm 5 K$ | $r_{1}$ (back) | 0.4573 | $\pm 0.0033$ |
| $\mathrm{q}\left(M_{2} / M_{1}\right)$ | 0.693 | $\pm 0.006$ | $r_{2}$ (pole) | 0.3372 | $\pm 0.0020$ |
| $\Omega_{\text {in }}$ | 3.2007 |  | $r_{2}$ (side) | 0.3547 | $\pm 0.0025$ |
| $\Omega_{\text {out }}$ | 2.8111 |  | $r_{2}$ (back) | 0.3937 | $\pm 0.0042$ |
| $\Omega_{1}=\Omega_{2}$ | 3.1570 | $\pm 0.0095$ | $f$ | $18.84 \%$ | $\pm 2.38 \%$ |
| $i$ | 72.970 | $\pm 0.049$ | $\Sigma \omega(O-C)^{2}$ | 0.0000124 |  |

average temperature $T_{1}=6104 \mathrm{~K}$ for the primary star (star eclipsed at primary light minimum). Considering the convective atmospheres of the components, the same values of gravity-darkening coefficients and bolometric albedo, i.e., $g_{1}=g_{2}=0.32$ (Lucy 1967) and $A_{1}=A_{2}=0.5$ (Ruciński 1969), were considered in the model.

The complete $B V R_{c} I_{c}$-band light curves are applied to look for a suitable mass ratio $q=M_{2} / M_{1}$ (the secondary divided by the primary). The relation between the sum of squared residuals $\sum\left(\omega_{i}(O-C)_{i}\right)^{2}$ and $q$ is displayed in Figure 4. The minimum in residuals is located at $q=0.70$ with a Differential Correction (DC) code. When we applied mass ratio as an adjustable parameter to perform the differential corrections, the suitable mass ratio $q$ converged at $q=0.693$. The derived parameters listed in Table 4 indicate that V680 Per is an A-type shallow-
contact binary without a spot. The theoretical light curves are displayed in Figure 5, and the configurations at phases $0.0,0.25,0.50$ are 0.75 were modeled with the Light Curve (LC) code and displayed in Figure 6.

## 5 DISCUSSION AND CONCLUSIONS

The $B V R_{c} I_{c}$-band light curve recorded in 2016 was analyzed by employing the 2013 version of W-D program. These solutions suggest that V680 Per is a typical A-type contact binary with a degree of contact of $f=18.84 \%$, $q=M_{2} / M_{1}=0.693$ and temperature difference of $\Delta T=T_{1}-T_{2}=6104 \mathrm{~K}-6003 \mathrm{~K}=101 \mathrm{~K}$, where both components share a CCE without spot activities. Based on the spectral type, the more massive component is F5V (Qian et al. 2017), and its corresponding mass is estimat-


Fig. 5 Observed $(\times)$ and theoretical (line) light curves calculated with the W-D (2013) program.


Fig. 6 Geometric configurations of V680 Per at phases $0.00,0.25,0.50$ and 0.75 .
ed as $M_{1}=1.40 M_{\odot}($ Cox \& Pilachowski 2000), and $M_{2}=0.97 M_{\odot}$.

In the $O-C$ diagram shown in Figure 3, the longterm decrease in period and cyclic oscillation were derived. The orbital period of V680 Per is decreasing at a rate of $d P / d t=-8.16 \times 10^{-8} \mathrm{~d} \mathrm{yr}^{-1}$. With the secular decrease in period, the degree of overcontact will become higher. Therefore, this system will evolve into a deeper overcon-
tact binary, if the decrease in orbital period is due to conservative mass transfer from the more massive component to the less massive one. By considering a conservative mass transfer equation from the primary to the secondary (Singh \& Chaubey 1986),

$$
\begin{equation*}
\frac{\dot{P}}{P}=3 \dot{M}_{2}\left(\frac{1}{M_{1}}-\frac{1}{M_{2}}\right), \tag{4}
\end{equation*}
$$



Fig. 7 The mass and orbital inclination for an assumed third body in V680 Per.
the mass transfer at a rate of $d M_{2} / d t=2.30 \times$ $10^{-7} M_{\odot} \mathrm{yr}^{-1}$ was determined. Therefore, the long-term decrease may result from conservative mass transfer from the more massive star to the less massive one, or angular momentum loss due to magnetic stellar wind.

Cyclic oscillations in the $O-C$ diagram are usually explained by the light-travel time effect via the presence of a third body (Liao \& Qian 2010; Zhu et al. 2013a,b; Qian et al. 2011, 2012, 2015). With the same method as used by Zhu et al. (2013a,b), the relations between semi-major axis of the third body, and of the third body mass, and the orbital inclination for an assumed third body in V680 Per are depicted in Figure 7. The estimated mass of the third body is $M_{3} \sin i^{\prime}=0.101 M_{\odot}$. If the orbital inclination $i^{\prime}$ is $90^{\circ}$, the mass of the third body should be $m_{3}=0.101 M_{\odot}$ with the maximal orbital radius of $a_{3}=3.75 \mathrm{AU}$. During the photometric solutions, we also searched for the contribution of the third body to the total light of the system, but the value of $L_{3}$ was always negative. Thus, the third body may be a very faint main sequence case.

Moreover, it is necessary for us to obtain many highprecision photometric and spectroscopic observations of V680 Per, in order to detect magnetic activities and determine the system's absolute parameters much more precisely.

Acknowledgements The CCD photometric observations of V680 Per were obtained with the $1.0-\mathrm{m}$ and $60-$ cm telescopes managed by Yunnan Observatories and with the $85-\mathrm{cm}$ telescope at Xinglong Station of National Astronomical Observatories. This work is supported by the Joint Research Found (Nos. U1831109 and U1631108) in Astronomy under cooperative agreement between the National Natural Science Foundation of China (NSFC) and Chinese Academy of Sciences (CAS), the Science Foundation of China University of Petroleum-Beijing at Karamay (Nos. RCYJ 2016B-03-004 and 2016B-03-006) and Key Laboratory for the Structure and Evolution of

Celestial Objects, Chinese Academy of Sciences (No. OP201708).

## References

Bradstreet, D. H., \& Guinan, E. F. 1994, in Astronomical Society of the Pacific Conference Series, 56, Stellar Mergers and Acquisitions: The Formation and Evolution of W Ursae Majoris Binaries, ed. A. W. Shafter, 228
Cox, A. N., \& Pilachowski, C. A. 2000, Physics Today, 53, 77
Diethelm, R. 2010, Information Bulletin on Variable Stars, 5920, 1
Diethelm, R. 2011, Information Bulletin on Variable Stars, 5960, 1

Diethelm, R. 2012, Information Bulletin on Variable Stars, 6011, 1

Diethelm, R. 2013, Information Bulletin on Variable Stars, 6042, 1
Drake, A. J., Djorgovski, S. G., Mahabal, A., et al. 2009, ApJ, 696, 870
Faulkner, D. R., Samec, R. G., Hawkins, N. C., et al. 2004, in American Astronomical Society Meeting Abstracts, 205, 18.04

Gettel, S. J., Geske, M. T., \& McKay, T. A. 2006, AJ, 131, 621
Guinan, E. F., \& Bradstreet, D. H. 1988, in NATO Advanced Science Institutes (ASI) Series C, 241, eds. A. K. Dupree, \& M. T. V. T. Lago, 345

He, J., \& Qian, S. 2009, Ap\&SS, 321, 209
Hubscher, J., \& Lehmann, P. B. 2012, Information Bulletin on Variable Stars, 6026, 1
Irwin, J. B. 1952, ApJ, 116, 211
Kallrath, J \& Milone, E. F. 1999, Eclipsing Binary Stars: Modeling and Analysis (New York: Springer)
Krajci, T. 2006, Information Bulletin on Variable Stars, 5690, 1
Liao, W. P., \& Qian, S. B. 2010, MNRAS, 405, 1930
Liao, W. P., Qian, S. B., Zhao, E. G., \& Jiang, L. Q. 2014, New Astron., 31, 65
Lucy, L. B. 1967, ZAp, 65, 89

Nelson, R. H. 2009, Information Bulletin on Variable Stars, 5875, 1
Nelson, R. H. 2010, Information Bulletin on Variable Stars, 5929, 1
Qian, S. B., Liu, L., Liao, W. P., et al. 2011, MNRAS, 414, L16
Qian, S. B., Liu, L., Zhu, L. Y., et al. 2012, MNRAS, 422, L24
Qian, S. B., Zhou, X., Zola, S., et al. 2014a, AJ, 148, 79
Qian, S. B., Wang, J. J., Zhu, L. Y., et al. 2014b, ApJS, 212, 4
Qian, S. B., Han, Z. T., Fernández Lajús, E., et al. 2015, ApJS, 221, 17
Qian, S.-B., He, J.-J., Zhang, J., et al. 2017, RAA (Research in Astronomy and Astrophysics), 17, 087
Ruciński, S. M. 1969, Acta Astronomica, 19, 245
Rucinski, S. M. 1997, AJ, 113, 1112
Samec, R. G., Hawkins, N. C., Miller, J., et al. 2005, Information
Bulletin on Variable Stars, 5610, 1
Singh, M., \& Chaubey, U. S. 1986, Ap\&SS, 124, 389
Sterken, C. 2005, in Astronomical Society of the Pacific

Conference Series, 335, Ole Roemer and the Light-Time Effect, ed. C. Sterken, 181
Van Hamme, W., \& Wilson, R. E. 2007, ApJ, 661, 1129
Wilson, R. E. 1979, ApJ, 234, 1054
Wilson, R. E. 1990, ApJ, 356, 613
Wilson, R. E. 2008, ApJ, 672, 575
Wilson, R. E., \& Devinney, E. J. 1971, ApJ, 166, 605
Zejda, M. 2002, Information Bulletin on Variable Stars, 5287, 1
Zejda, M. 2004, Information Bulletin on Variable Stars, 5583, 1
Zejda, M., Mikulasek, Z., \& Wolf, M. 2006, Information Bulletin on Variable Stars, 5741, 1
Zhou, A.-Y., Jiang, X.-J., Zhang, Y.-P., \& Wei, J.-Y. 2009, RAA (Research in Astronomy and Astrophysics), 9, 349
Zhu, L.-Y., Qian, S.-B., \& Xiang, F.-Y. 2004, PASJ, 56, 809
Zhu, L., \& Qian, S. 2006, MNRAS, 367, 423
Zhu, L. Y., Qian, S. B., Liu, N. P., Liu, L., \& Jiang, L. Q. 2013a, AJ, 145, 39
Zhu, L. Y., Qian, S. B., Zhou, X., et al. 2013b, AJ, 146, 28

