

Observational signature of a wind bubble environment for double neutron star mergers

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Abstract During the in-spiral stage of a compact binary, a wind bubble could be blown into the interstellar medium, if electromagnetic radiation due to the binary orbital motion is strong enough. Therefore, short-duration gamma-ray bursts (SGRBs) due to double neutron star mergers would in principle happen in a wind bubble environment, which can influence the propagation of the SGRB jet and consequent afterglow emission. By calculating the dynamics and synchrotron radiation of the jet-driven external shock, we reveal that an abrupt jump could appear in the afterglow light curves of SGRBs and the observational time of the jump is dependent on the viewing angle. This light curve jump provides an observational signature to constrain the radius of the wind bubble and thus the power of the electromagnetic radiation of the binary, by combining with gravitational wave detection.

Key words: gamma ray bursts: general — gravitational waves

1 INTRODUCTION

Short-duration gamma-ray bursts (SGRBs) of $T_{90} \lesssim 2$ s have long been hypothesized to originate from mergers of double neutron stars (NSs) or NS-black hole binaries (Paczynski 1986; Eichler 1989; Narayan et al. 1992). Since the first discovery of afterglow emission from SGRBs in 2005, this origin hypothesis has been increasingly supported by the large offsets of SGRBs from the centers of their host galaxies, by the non-detection of supernovae associated with SGRBs and by their event rates that can be connected with the cosmic star formation rates by power-law distributed time delays (Guetta & Piran 2006; Nakar et al. 2006; Virgili et al. 2011; Wanderman & Piran 2015). On 2017 August 17, GRB 170817A was observed by the *Fermi Gamma-Ray Telescope* (Abbott et al. 2017a,b,c) starting 1.7 s after the first detection of a gravitational wave (GW) from a double NS merger by advanced LIGO. This first SGRB-GW associated event eventually confirmed the long-hypothesized merger origin of SGRBs, although the very low luminosity of GRB 170817A (i.e., $L_{\text{iso}} \sim 10^{47}$ erg s $^{-1}$) still makes it very different from typical SGRBs (generally $L_{\text{iso}} \gtrsim 10^{49}$ erg s $^{-1}$).

The sites of compact binary mergers are usually far away from the centers of their host galaxies. Therefore, the environment of an SGRB, where an external shock is driven by the SGRB jet, is widely considered to be low-density. As inferred from the fittings to the afterglow emission of SGRBs, the density range of their environmental medium is around $n \sim (10^{-3} - 1)$ cm $^{-3}$ with a median value $\langle n \rangle < 0.15$ cm $^{-3}$ (Berger 2014). In the afterglow fittings, a uniform interstellar medium (ISM) environment is usually assumed. However, this assumption is not always valid, in particular, if the pre-merger compact binaries can lose their orbital energy through intense electromagnetic radiation alongside GW radiation (Medvedev & Loeb 2013b). At the final stage of the in-spiral of compact binaries, in particular double NS binaries, the electromagnetic radiation can in principle drive a relativistic binary wind to sweep up the ISM by a shock wave. As a result, a nearly-isotropic wind bubble can be blown and expand continuously until the merger occurs, which is bounded by a thin shell consisting of compressed ISM¹. Therefore, compact binary mergers could happen at the centers of

¹ This shocked ISM shell could be observed as a faint radio source due to its synchrotron radiation (Medvedev & Loeb 2013a).

wind bubbles. The resultant SGRB jets should first coast in a low-density wind nebula and then collide with a bubble shell, before the jets finally interact with the uniform ISM.

This paper is devoted to determining which observational signature can be caused by the interaction between an SGRB jet and a wind bubble, in particular when the observation is off-axis and the jet has a complicated structure, like the case of GRB 170817A. This work is rather similar to some previous studies of long-duration GRBs, where a wind bubble is blown by the stellar wind from the progenitor Wolf-Rayet star (Ramirez-Ruiz et al. 2001; Ramirez-Ruiz et al. 2005; Pe’er & Wijers 2006; Kong et al. 2010). Our model is described in the next section. Results and discussion are given in Sections 3 and 4, respectively.

2 THE MODEL

2.1 A Binary Wind Bubble

Besides GW radiation, in-spiraling NS binaries can also lose their orbital energy through electromagnetic radiation, due to the high orbital frequencies and strong magnetic fields of the NSs. This energy release could be initially in the form of Poynting flux and gradually convert into an ultra-relativistic electron-positron wind, just like the formation and evolution of a pulsar wind (Medvedev & Loeb 2013a). As a result, a wind bubble can be blown into the surrounding medium with a density profile of

$$n(r) = \begin{cases} n_b & R_t \leq r \leq R_b, \\ Kn_{\text{ism}} & R_b < r < R_s, \\ n_{\text{ism}} & R_s \leq r, \end{cases} \quad (1)$$

where n_b and n_{ism} are the densities of the wind nebula and the un-shocked ISM respectively, and $K = (\hat{\gamma} + 1)/(\hat{\gamma} - 1)$ is given by the Rankine-Hugoniot jump condition with $\hat{\gamma}$ being the adiabatic index of the shocked material. The structure of a wind bubble is illustrated in Figure 1. The characteristic radii R_t , R_b and R_s are in principle functions of time, which are determined by the electromagnetic radiation process of the binary. However, a precise calculation of this electromagnetic radiation is unavailable, because of the unknown spins of the NSs and the unclear configuration of their common magnetosphere. In any case, for an amount of energy E_s that is primarily released during a period t_s , the outer radius of the shocked ISM shell can be

estimated as

$$R_s \sim \left(\frac{3E_s t_s^2}{4\pi n_{\text{ism}} m_p} \right)^{1/5} \\ = 1.7 \times 10^{17} \text{cm} \left(\frac{E_{s,46} t_{s,7}^2}{n_{\text{ism},-3}} \right)^{1/5}. \quad (2)$$

This is derived from the following equations: $M_{\text{sw}} v^2 \sim E_s$, $R_s \sim vt_s$ and $M_{\text{sw}} = (4\pi/3)R_s^3 n_{\text{ism}} m_p$, where M_{sw} is the mass of the swept-up ISM in the shell and v is the velocity of the external shock. Subsequently, the outer radius of the wind bubble R_b can be determined by $n_{\text{ism}} R_s^3 = Kn_{\text{ism}}(R_s^3 - R_b^3)$ as

$$R_b = \left(\frac{K-1}{K} \right)^{1/3} R_s. \quad (3)$$

Finally, by considering that the pulsar wind bubble consists almost entirely of electrons and positrons, its density can be given by

$$n_b \sim \frac{3E_s}{4\pi(R_b^3 - R_t^3)\gamma_{e^\pm} m_e c^2} \\ = 7.8 \times 10^{-6} [1 - (R_t/R_b)^3]^{-1} \text{cm}^{-3} \\ \times E_{s,46}^{2/5} t_{s,7}^{-6/5} n_{\text{ism},-3}^{3/5} \gamma_{e^\pm,5}^{-1},$$

where γ_{e^\pm} is the typical random Lorentz factor of e^\pm in the shocked wind. By considering the mechanical balance between the two shocked regions, the radius of the termination shock of the wind can be determined by $R_t = (E_s/4\pi n_{\text{ism}} v^2 ct_s)^{1/2}$. In any case, the value of R_t would not substantively influence the dynamics of SGRB outflows.

2.2 A Structured SGRB Jet

The relativistic outflows producing SGRBs are considered to be highly anisotropic and even collimated. The specific structure of these gamma-ray burst (GRB) jets is unclear and a simple ‘‘top-hat’’ structure has usually been adopted in the literature (e.g., Lamb et al. 2005). However, very recently, observations of GRB 170817A showed that its afterglow light curves in all of the radio, optical and X-ray bands share an identical behavior, i.e., continuously increasing from 2.3 d and reaching a peak at around 150 d (Margutti et al. 2017, 2018; Troja et al. 2017, 2018; D’Avanzo et al. 2018). This behavior cannot be explained by the ‘‘top-hat’’ jet, but requires an angularly distributed jet that was observed off-axis (Lamb & Kobayashi 2017; Mooley et al. 2018b,a; Granot et al. 2018; Lazzati et al. 2018). More specifically, the primary energy of the jet should be concentrated within a small cone having a half

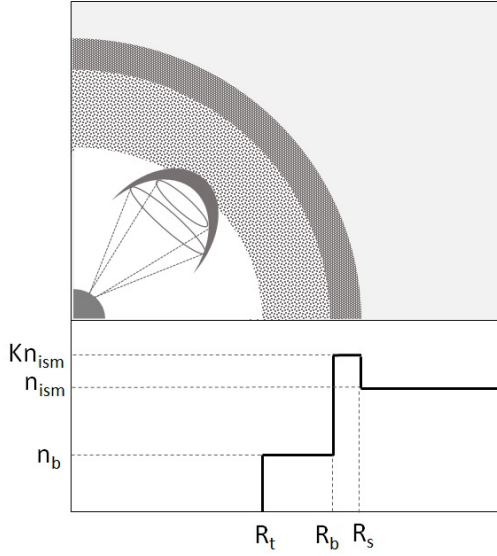


Fig. 1 Illustration of a wind bubble environment for a double NS merger. The *solid line* represents the corresponding density profile of the bubble.

opening angle of θ_c . With an increasing angle relative to the jet axis, the energy density decreases gradually, accompanied by a decrease in Lorentz factor. Such a jet structure could be caused when the jet passes through and breaks out from an intense sub-relativistic outflow (i.e., the merger ejecta responsible for kilonova emission). According to previous simulations of jet propagation and fittings to the afterglow of GRB 170817A, we adopt the following distributions for the kinetic energy and Lorentz factor of an SGRB jet (Dai & Gou 2001; Zhang & Mészáros 2002; Kumar & Granot 2003):

$$\varepsilon(\theta) \equiv \frac{dE_{\text{jet}}}{d\Omega} = \begin{cases} \varepsilon_c, & \theta \leq \theta_c, \\ \varepsilon_c \left(\frac{\theta}{\theta_c}\right)^{-k}, & \theta_c < \theta < \theta_m, \end{cases} \quad (4)$$

and

$$\Gamma_0(\theta) = \begin{cases} \eta, & \theta \leq \theta_c, \\ \eta \left(\frac{\theta}{\theta_c}\right)^{-k} + 1, & \theta_c < \theta < \theta_m, \end{cases} \quad (5)$$

where θ_m is defined as the maximum angle of the jet. The index k is a constant that can be deduced from the luminosity distribution of local event rate density (Pescalli et al. 2015; Xiao et al. 2017). The interaction of such a structured jet with a pre-merger wind bubble is the focus of this paper.

2.3 Dynamics of the Jet's External Shock

In order to calculate the dynamical evolution of a structured jet, we separate the jet into a series of differential

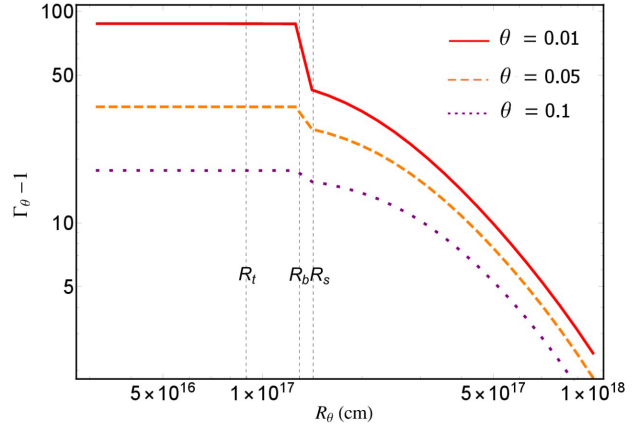


Fig. 2 Lorentz factors as functions of r_θ for different jet rings. The model parameters are taken as $\theta_c = 0.02$, $\theta_m = 0.1$, $k = 1$, $\varepsilon_c = 10^{50.5} \text{ erg s}^{-1}$, $\eta = 88$, $n_{\text{ism}} = 0.01$, $E_s = 4.1 \times 10^{46} \text{ erg}$, $R_s \simeq 1.42 \times 10^{17} \text{ cm}$ and $R_b \simeq 1.29 \times 10^{17} \text{ cm}$.

rings. The energy per solid angle and Lorentz factor of these rings are given according to Equations (4) and (5) respectively. For simplicity, the dynamical evolution of the rings is considered to be independent from each other by ignoring their possible lateral expansion/motion. Then, the following equation can be used (Huang et al. 2000)

$$\frac{d\Gamma_\theta}{d\Sigma_{\text{sw},\theta}} = -\frac{\Gamma_\theta^2 - 1}{\Sigma_{\text{ej},\theta} + 2\Gamma_\theta \Sigma_{\text{sw},\theta}}, \quad (6)$$

where $\Sigma_{\text{ej},\theta} = dM_{\text{ej}}/d\Omega = \varepsilon_\theta/\Gamma_{\theta,0}$ is the jet mass per solid angle at angle θ and the corresponding swept-up ISM mass is determined by

$$\frac{d\Sigma_{\text{sw},\theta}}{dr_\theta} = n m_p r_\theta^2. \quad (7)$$

Here r_θ is the radius of the external shock front driven by the propagation of the SGRB jet. Numerical results of the dynamical calculations are presented in Figure 2 for different differential rings of the jet. The sharp decay of the Lorentz factors at $r_\theta = R_b$ is due to the collision of the jet rings with the compressed bubble shell.

2.4 Shock Synchrotron Emission

For a differential element of mass $\Sigma_{\text{sw}}(r, \theta, \varphi) d\varphi d\theta$, the synchrotron luminosity contributed by electrons in this mass can be calculated by an analytical method published by Sari et al. (1998) as

$$\ell'_{\nu'}(r, \theta, \varphi) d\varphi d\theta = \frac{\Sigma_{\text{sw}}(r, \theta, \varphi) d\varphi d\theta}{m_p} \times \frac{m_e c^2 \sigma_T B'(r, \theta, \varphi)}{3e} S'(\nu'), \quad (8)$$

where the superscript prime indicates the quantities are measured in the comoving frame of the shocked region,

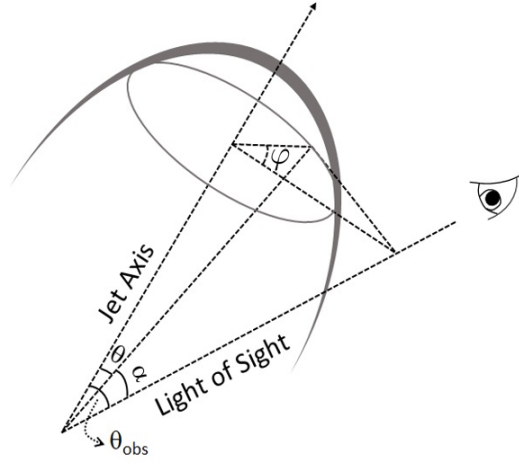


Fig. 3 The relation between angles θ , φ , θ_{obs} and α for a differential swept-up ISM element.

$B'(r, \theta, \varphi)$ is the magnetic field strength and $S'(\nu')$ represents the dimensionless synchrotron spectrum. This spectrum can be approximately expressed by a multi-broken power law as

$$S'(\nu') = \begin{cases} (\nu'/\nu'_1)^{1/3}, & \nu' \leq \nu'_1, \\ (\nu'/\nu'_1)^{-(q-1)/2}, & \nu'_1 < \nu' < \nu'_h, \\ (\nu'_h/\nu'_1)^{-(q-1)/2} (\nu'/\nu'_h)^{-p/2}, & \nu'_h \leq \nu', \end{cases} \quad (9)$$

where the broken frequencies $\nu'_l(r, \theta, \varphi)$ and $\nu'_h(r, \theta, \varphi)$ are determined by the energy distribution of electrons, p is the power-law index of shock-accelerated electrons, and $q = 2$ or $q = p$ for the rapid and slow cooling cases, respectively. Then, the observed flux at an observational time t can be obtained by integrating over the whole solid angle of the jet as

$$F_\nu(t) = \frac{1}{4\pi D_L^2} \int_0^{\theta_m} \int_0^{2\pi} \frac{\ell'_{\nu'}(r, \theta, \varphi)}{\Gamma_\theta^3 (1 - \beta_\theta \cos \alpha)^3} d\varphi d\theta, \quad (10)$$

where D_L is the luminosity distance of the SGRB, θ_{obs} is the viewing angle with respect to the jet axis, and the angle α which is defined between the emitting differential element and the light of sight can be determined by

$$\cos \alpha = \frac{\cos \theta_{\text{obs}}}{2 \cos \theta} \left(1 + \frac{\cos^2 \theta}{\cos^2 \theta_{\text{obs}}} - \sin^2 \theta - \cos^2 \theta \tan^2 \theta_{\text{obs}} + 2 \cos \theta \sin \theta \tan \theta_{\text{obs}} \cos \varphi \right). \quad (11)$$

The relation between the angles θ , φ , θ_{obs} and α is illustrated in Figure 3. Finally, the radius r of emitting material can be connected with the observational time by $r = ct/(1 - \beta_\theta \cos \alpha)$, where $\beta_\theta = (1 - \Gamma_\theta^{-2})^{1/2}$.

3 RESULTS

In Figure 4, we present an example afterglow light curve observed on-axis, where an X-ray frequency is considered. The contributions from different differential rings are represented by the dashed lines. As the early afterglow emission is dominated by contribution from the core of the jet, the emission from large angles would become more and more important at late times. In comparison with previous afterglow calculations, an abrupt jump appears in our light curve at time t_{jp} , which arises from the abrupt jump in environmental density at R_b . For an on-axis observation, we have $t_{\text{jp}} \approx R_b/(2\eta^2 c)$. Therefore, this light curve jump can be regarded as an observational signature of the wind bubble environment. Furthermore, since the velocity of the jet material decreases with increasing θ , different jet rings collide with the bubble shell at different times. Therefore, for off-axis observations, the light curve jump time would be delayed. Specifically, we have $t_{\text{jp}} \approx R_b/[c(1 - \beta_{\theta_{\text{obs}}})]$. Such off-axis observation and environment density effects are presented in Figures 5 and 6 respectively.

4 DISCUSSION

Following confirmation of the origin of SGRBs from double NS mergers by the GW 170817-GRB 170817A association, it has become a cutting-edge topic to answer how these mergers happen and how GRB outflows form and evolve. In particular, the electromagnetic radiation from inspiraling NS binaries is still completely unknown, which however can influence the orbital decay of the binaries and modify the environments where SGRBs occur. By supposing a wind bubble driven by the binary electromagnetic radiation, we calculate the dynamics and synchrotron radiation of an external shock arising from the interaction

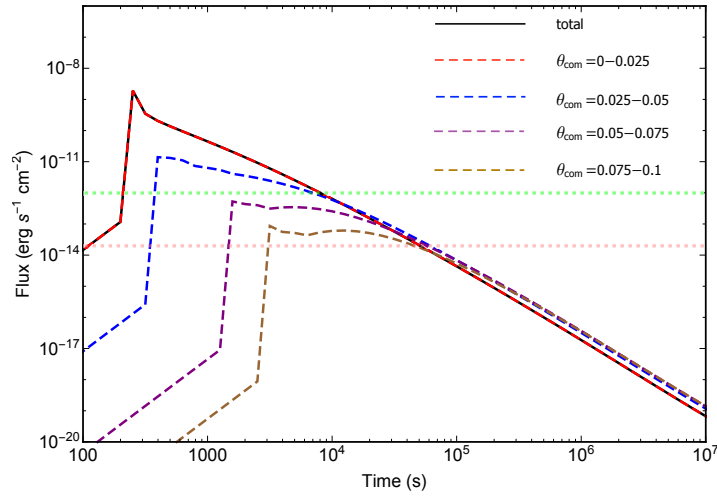


Fig. 4 An X-ray (1 keV) afterglow light curve (*solid line*) arising from an SGRB jet interacting with a binary wind bubble. The *dashed lines* represent the contributions of the material within the θ ranges as labeled. The green and pink dotted lines represent the sensitivities of *Swift X-ray telescope (XRT)* and *Einstein Probe (EP)* at 10^4 s respectively.

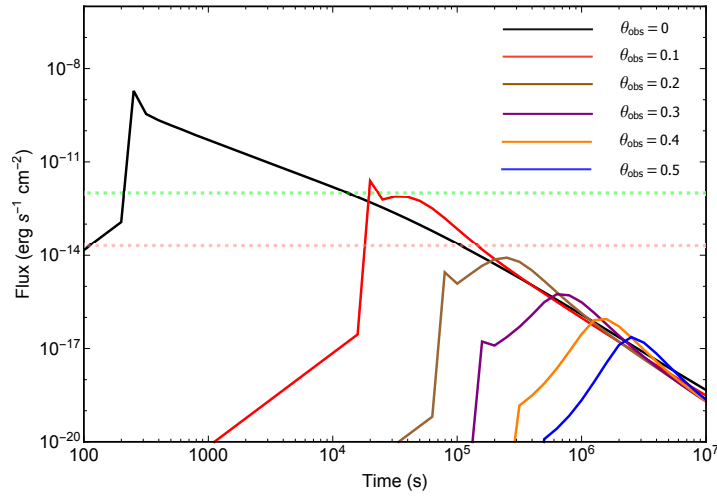


Fig. 5 X-ray (1 k) afterglow light curves for different viewing angles as labeled.

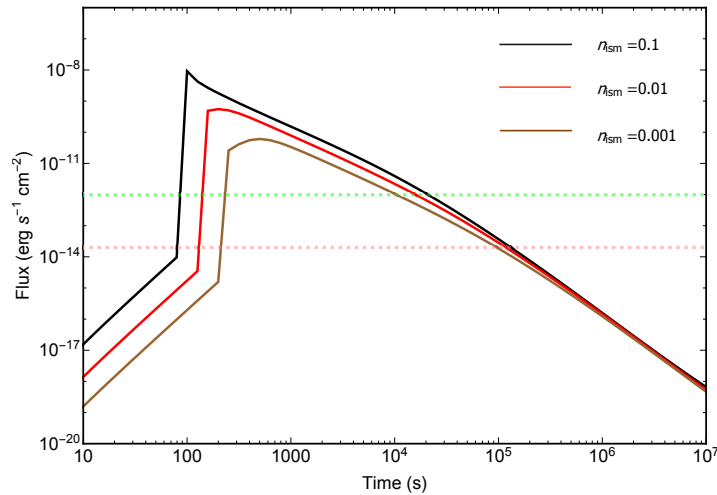


Fig. 6 X-ray (1 keV) afterglow light curves for different environment medium densities.

between a structured SGRB jet and the bubble. As a result, it is revealed that an abrupt jump could appear in the afterglow light curves of SGRBs and the observational time of the jump is dependent on the viewing angle. Therefore, the discovery of this light curve jump can be used to constrain the radius of the wind bubble and then the power of the electromagnetic radiation of the binary, after the viewing angle has been fixed by the peak time of the afterglow and by the GW detection.

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References

- Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2017a, *ApJ*, 848, L13
- Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2017b, *Physical Review Letters*, 119, 161101
- Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2017c, *ApJ*, 848, L12
- Berger, E. 2014, *ARA&A*, 52, 43
- Dai, Z. G., & Gou, L. J. 2001, *ApJ*, 552, 72
- D’Avanzo, P., Campana, S., Salafia, O. S., et al. 2018, *A&A*, 613, L1
- Eichler, D. 1989, *Physical Review Letters*, 63, 2440
- Granot, J., Gill, R., Guetta, D., & De Colle, F. 2018, *MNRAS*, 481, 1597
- Guetta, D., & Piran, T. 2006, *A&A*, 453, 823
- Huang, Y. F., Gou, L. J., Dai, Z. G., & Lu, T. 2000, *ApJ*, 543, 90
- Kong, S. W., Wong, A. Y. L., Huang, Y. F., & Cheng, K. S. 2010, *MNRAS*, 402, 409
- Kumar, P., & Granot, J. 2003, *ApJ*, 591, 1075
- Lamb, D. Q., Donaghy, T. Q., & Graziani, C. 2005, *ApJ*, 620, 355
- Lamb, G. P., & Kobayashi, S. 2017, *MNRAS*, 472, 4953
- Lazzati, D., Perna, R., Morsony, B. J., et al. 2018, *Physical Review Letters*, 120, 241103
- Margutti, R., Berger, E., Fong, W., et al. 2017, *ApJ*, 848, L20
- Margutti, R., Alexander, K. D., Xie, X., et al. 2018, *ApJ*, 856, L18
- Medvedev, M. V., & Loeb, A. 2013a, *ApJ*, 768, 113
- Medvedev, M. V., & Loeb, A. 2013b, *MNRAS*, 431, 2737
- Mooley, K. P., Nakar, E., Hotokezaka, K., et al. 2018a, *Nature*, 554, 207
- Mooley, K. P., Deller, A. T., Gottlieb, O., et al. 2018b, *Nature*, 561, 355
- Nakar, E., Gal-Yam, A., Piran, T., et al. 2006, *ApJ*, 640, 849
- Narayan, R., Paczynski, B., & Piran, T. 1992, *ApJ*, 395, L83
- Paczynski, B. 1986, *ApJ*, 308, L43
- Pe’er, A., & Wijers, R. A. M. J. 2006, *ApJ*, 643, 1036
- Pescalli, A., Ghirlanda, G., Salafia, O. S., et al. 2015, *MNRAS*, 447, 1911
- Ramirez-Ruiz, E., Dray, L. M., Madau, P., & Tout, C. A. 2001, *MNRAS*, 327, 829
- Ramirez-Ruiz, E., García-Segura, G., Salmonson, J. D., & Pérez-Rendón, B. 2005, *ApJ*, 631, 435
- Sari, R., Piran, T., & Narayan, R. 1998, *ApJ*, 497, L17
- Troja, E., Piro, L., van Eerten, H., et al. 2017, *Nature*, 551, 71
- Troja, E., Piro, L., Ryan, G., et al. 2018, *MNRAS*, 478, L18
- Virgili, F. J., Zhang, B., Nagamine, K., & Choi, J.-H. 2011, *MNRAS*, 417, 3025
- Wanderman, D., & Piran, T. 2015, *MNRAS*, 448, 3026
- Xiao, D., Liu, L.-D., Dai, Z.-G., & Wu, X.-F. 2017, arXiv:1710.00275
- Zhang, B., & Mészáros, P. 2002, *ApJ*, 571, 876