# Modern comprehensive study of the W UMa system TY Boo 

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#### Abstract

New three color light curves of TY Boo were acquired during five nights from February to May 2006 in the $B V R$ bandpass using a $50-\mathrm{cm}$ F/8.4 RitcheyChrétien telescope (Ba50) at the Baja Astronomical Observatory (Hungary), with a $512 \times 512$ Apogee AP-7 CCD camera. A photometric solution of these light curves was obtained by means of the Wilson-Devinney code. The results showed that the less massive component is hotter than the more massive one, and the temperature difference between the components is $\Delta T \sim 249 \mathrm{~K}$. Long term investigation of the system based on all available data shows two stages of increase and a similar trend for decrease, which appears to be periodic behavior. A set of new light elements yields a new period $\left(P=0.3171506^{\mathrm{d}}\right)$ and shows a periodic decrease with the rate $d P / d E=5.858 \times 10^{-12} \mathrm{~d} \mathrm{cycle}^{-1}, 6.742 \times 10^{-9} \mathrm{~d} \mathrm{yr}^{-1}$ or 0.058 s century ${ }^{-1}$. The evolutionary status of the system is discussed.


Key words: binaries: eclipsing — stars: evolution

## 1 INTRODUCTION

The eclipsing binary system TY Boo was discovered to be a variable star and classified as a W UMa type by Guthnick \& Prager (1926), with a period of $0.31730^{\text {d }}$. A cyclic period variation of about 400 orbital revolutions (127 days) was found by Szafraniec (1953). Carr (1972) suggested that the system was an A-type system consisting of two main sequence components (G3 and G7). The published data by Carr (1972) were re-analyzed by Niarchos (1978) using frequency domain techniques. The results suggested that the system is a W UMa system with a mass ratio of 0.22 . A new $B V$ light curve was published by Samec \& Bookmyer (1987); they concluded that the system has become redder since Carr's observations were acquired, but the amplitude of the eclipse curves did not show any apparent changes. Their study of the period shows no indication of the cyclic period variation, which was suggested by Szafraniec (1953).

The first spectroscopic observations of the system TY Boo were carried out by Rainger et al. (1990). They used their spectroscopic observations together with $B$ light curves published by Samec \& Bookmyer (1987) to yield a combined orbital solution, which gave the masses and absolute dimensions for the components. Their results show that the system is a normal W UMa type contact binary, with a main sequence primary star and a secondary component larger than expected by $\sim 1.4$ considering its zero age main sequence (ZAMS) mass. They confirmed the orbital period change of the system, and calculated the first radial velocities for the system.

Photometric and spectroscopic observations were carried out for the system TY Boo by Milone et al. (1991) in three observing sessions. They calculated the mass ratio of the system ( $q=M_{\mathrm{h}} / M_{\mathrm{c}}=0.465$ ), which is consistent with the value derived using light curve analysis ( $q=0.481$ ). Christopoulou et al. (2012) observed the system in a four color bandpass and derived a long term light curve solution.

In this work we present a new CCD light curve in the $B V R$ band for the system TY Boo which was analyzed using an advanced version of the Wilson-Devinney (W-D) code. Long term stability for both the period and observed light curve is investigated by considering a possible connection between.

The structure of the paper is as follows: Section 2 describes the observations. Section 3 deals with the orbital period analysis. Light curve stability is outlined in Section 4. In Section 5, we perform the light curve modeling. Section 6 presents the evolutionary status of the system. Finally, the discussion is outlined in Section 7.

## 2 OBSERVATIONS

The present CCD observations of TY Boo were acquired on five nights from February to May 2006 in the $B V R$ bandpass using a $50-\mathrm{cm} \mathrm{F} / 8.4$ Ritchey-Chrétien telescope ( $\mathrm{Ba50}$ ) at the Baja Astronomical Observatory (Hungary), and a $512 \times 512$ Apogee AP-7 CCD camera. The observed frames were processed by the photometry software AIP4WIN (Berry \& Burnell 2000) which applied aperture photometry, including bias and dark subtraction and flat field correction. Star GSC 02568-00997 ( $V=11.59$ mag, $B-V=0.37$ ) was used as a comparison star, while GSC 02568-00991 ( $V=$ 11.67 mag ) was used as a check. The original data are listed in Table 1. A total of 962 individual observations were obtained in the $B V R$ bandpass (240 in $B, 293$ in $V$ and 429 in $R$ ). The $B V R$ light curves displayed in Figure 1 show the difference in magnitude (DM, the variable minus the comparison star) versus the phase in the $B V R$ bands. The orbital phases were computed according to the following ephemeris by Kreiner et al. (2001)

$$
\begin{equation*}
\operatorname{Min} \mathrm{I}=2447612.6035+0.3171490 \tag{1}
\end{equation*}
$$

Figure 1 indicates that the light curve variation of the system TY Boo is typical of W UMa type and the data collected on all days can be joined smoothly. New values for 19 times of minima were derived (12 primary and 7 secondary), which were estimated by means of the Minima V2.3 package


Fig. $1 B V R$ light curves of TY Boo.
(Nelson 2006) based on the Kwee \& Van Woerden (1956) fitting method. The new times of light minima appear in Table 2 and values are given in Table 3 for visual (vis), photometric (pe) and CCD (ccd) observations.

Table 1 The Magnitude Differences in the $B V R$ Bands of TY Boo Together with the Heliocentric Julian Dates and Phases

|  | $B$-ban |  |  | -band |  |  |  | -band |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Phase | $\Delta B$ | Error | JD | P | $\Delta V$ | Erro | JD | Phase | $\Delta R$ | Er |
| 2453 | 0.0132 | -0.621 | 0.025 | 2453794. | 0.7794 | -0.863 | 0.035 | 2453794 | 0.9810 | 0.087 | 0.004 |
| 2453796.4342 | 0.0215 | -0.640 | 0.026 | 2453794.4942 | 0.7845 | -0.872 | 0.036 | 2453794.5163 | 0.9741 | 0.114 | 5 |
| 2453796.4369 | 0.0299 | -0.649 | 0.027 | 2453794.4974 | 0.7946 | -0.860 | 0.035 | 2453794.5179 | 0.9791 | 0.128 | 0.005 |
| 53796.4395 | 0.0383 | -0.712 | 0.029 | 2453794.4990 | 0.7997 | -0.863 | 0.035 | 2453794.5200 | 857 | . 158 | 0.007 |
| 2453796.4422 | 0.0 | -0. | 0.032 | 153794500 | 0.8048 | -0. | 0.035 | 2453794.5216 | 7 | 46 | 0.006 |
| 2453796.4448 | 0.0549 | -0. | 0.034 | 245 | 0.8099 | -0. | 0. | 24 | 0.0051 | 58 | 0.007 |
| 5 | 0.0633 | -0.903 | 37 | 453794.5039 | 0.8149 | -0 | 0.034 | 2453794.5309 | 0.0203 | 40 | 0.006 |
| 2453796.4501 | 0.0717 | -0.955 | 0.039 | 2453794.5055 | 0.8200 | -0.850 | 0.0 | 2453794.5325 | 0.0253 | 0.120 | 05 |
| 53796.4528 | 0.0800 | -0.968 | 0.040 | 2453794.5071 | 0.8251 | -0.828 | 0.034 | 2453794.5341 | 0.0304 | 0.088 | 0.004 |
| 53796.4554 | 0.0883 | -1.056 | 0.043 | 2453794.5087 | 0.8302 | -0.821 | 0.034 | 2453794.5358 | 0.0355 | 0.073 | 0.003 |
|  | 0.0 | -1.040 | 0.043 | 2453794.5103 | 0.8352 | -0. | 0.033 |  | 6 | 0.052 | 2 |
| 3796.4607 | 0.1051 | -1.066 | 0.044 | 245 | 0.8403 | -0. | 0.034 | 24 | . 0456 | 0.017 | 0.001 |
| 2453796.4634 | 0.1134 | -1.097 | 0.045 | 2453794.513 | 0.8453 | -0.78 | 0.0 | 2453794.5406 | 0.0507 | -0.016 | 0.001 |
| 2453796.4660 | 0.1218 | -1.153 | 0.047 | 2453794.5 | 0.8504 | -0.8. | 0.03 | 24537 | 0.0558 | -0.038 | 02 |
| 2453796.4687 | 0.1302 | -1.170 | 0.048 | 2453794.5167 | 0.8555 | -0.798 | 0.033 | 2453794.5452 | 0.0654 | -0.096 | 0.004 |
| 3796.4713 | 0.1385 | -1.147 | 0.047 | 453794.5183 | 0.8606 | -0.78 | 0.032 | 2453794.5469 | 0.0705 | -0.122 | 0.005 |
| 53796.4740 | 0.1469 | -1.198 | 0.0 | , | 0.8656 | -0. | 0.03 | 2453794.5485 | 0.0756 | -0.159 | 0.007 |
| 2453796 | 0.1552 | -1.201 | 0.049 | 245 | 0.8707 | -0.7 | 0.0 | 2453794.5501 | . 0807 | -0.186 | 0.008 |
| 2453796.4793 | 0.1635 | -1.208 | 0.049 | 2453794.523 | 0.8758 | -0.76 | 0.0 | 2453794. | 0.0857 | -0.200 | 8 |
| 2453796.4819 | 0.1719 | -1.283 | 0.052 | 2453794.5248 | 0.8808 | -0.763 | 0.031 | 2453794.5533 | 0.0908 | -0.221 | 0.009 |
| 53796.4846 | 0.1803 | -1.263 | 0.052 | 2453794.5 | 0.8859 | -0.733 | 0.0 | 2453794.5549 | 0.0958 | -0.237 | 0.010 |
| 453796.4872 | 0.1886 | -1.266 | . 052 | 2453794.5 | 0.8910 | -0.7 | 0.0 | 24 | 0.1668 | -0.399 | 0.016 |
| 2453796.4899 | 0.1970 | -1.266 | 0.052 | 2453794.529 | 0.8961 | -0.72 | 0.03 | 2453794.579 | 0.1719 | -0.414 | 1 |
| 2453796.4925 | 0.2054 | -1.290 | 0.053 | 2453794.5 |  | -0.702 | 0.029 | 2453794 | 0.1820 | -0.419 | 17 |
| 2453796.4952 | 0.2137 | -1.333 | 0.054 | 2453794.5328 | 0.9062 | -0.686 | 0.028 | 2453794.583 | 0.1871 | -0.436 | 0.018 |
| 53796.4978 | 0.2220 | -1.344 | 0.055 | 2453794.534 | 0.9113 | -0.665 | 0.027 | 2453794.5855 | 0.1922 | -0.436 | 0.018 |
| 53796.5005 | 0.2304 | -1.301 | 0.053 | 453794.5360 | 0.9164 | -0.63 | 0.026 | 2453794.587 | 0.1973 | -0.451 | 0.018 |
| 453796.5031 | 0.2388 | -1.332 | 0.054 | 2453794.537 | 0.9215 | -0.62 | 0.02 | 2453794.588 | 0.2023 | -0.453 | 0.0 |
| 2453796.5058 | 0.2472 | -1.332 | 0.054 | 2453794.539 | 0.9265 | -0.592 | 0.02 | 2453794.5903 | 0.2074 | -0.461 | 9 |
| 2453796.5084 | 0.2555 | -1.330 | 0.054 | 2453794.5409 | 0.9315 | -0.582 | 0.02 | 2453794.5919 | 0.2125 | -0.47 | 0.019 |
| 53796.5111 | 0.2639 | -1.350 | 0.055 | 2453794.5425 | 0.9366 | -0.542 | 0.02 | 24537945935 | 0.2176 | -0.463 | 0.019 |
| 53796.5137 | 0.2722 | -1.336 | . 055 | 453794.542 | 0.0625 | -0.439 | 0.01 | 2453794.595 | . 2227 | -0.477 | 0.020 |
| 453796.5164 | 0.2806 | -1.326 | 0.054 | 2453794.545 | 0.0721 | -0.495 | 0.02 | 2453794.601 | . 2430 | -0.474 | 0.019 |
| 2453796.5293 | 0.3213 | -1.288 | 0.053 | 2453794.547 | 0.0772 | -0.521 | 0.021 | 2453794.6031 | 0.2480 | -0.48 | 0.020 |
| 2453796.5319 | 0.3297 | -1.289 | 0.053 | 2453794.5490 | 0.0822 | -0.543 | 0.02 | 2453794.6047 | 0.2530 | -0.480 | 0.020 |
| 2453796.5346 | 0.3381 | -1.283 | 0.052 | 2453794.5506 | 0.0873 | -0.578 | 0.024 | 2453794.6063 | 0.2581 | -0.480 | 0.020 |
| 453796.5373 | 0.3464 | -1.266 | 0.052 | 2453794.5522 | 0.0924 | -0.594 | 0.024 | 2453794.6080 | 0.2632 | -0.479 | 0.020 |
| 53796.5425 | 0.3630 | -1.250 | . 051 | 453794.553 | 0.0974 | -0.625 | 0.02 | 2453794.609 | . 2682 | -0.473 | 0.019 |
| 2453796.5452 | 0.3714 | -1.237 | 0.051 | 2453794.555 | 0.1025 | -0.62 | 0.02 | 2453794.612 | 0.2784 | -0.477 | 0.020 |
| 2453796.5478 | 0.3798 | -1.236 | 0.051 | 2453794.5570 | 0.1076 | -0.649 | 0.027 | 2453794.614 | 0.2835 | -0.469 | 0.019 |
| 2453796.5505 | 0.3881 | -1.198 | 0.049 | 2453794.5586 | 0.1126 | -0.666 | 0.027 | 2453794.6176 | 0.2937 | -0.472 | 0.019 |
| 153796.5531 | 0.3965 | -1.183 | 0.048 | 2453794.5602 | 0.1177 | -0.661 | 0.027 | 2453794.6209 | 0.3039 | -0.458 | 0.019 |
| 453796.5558 | 0.4048 | -1.177 | 0.048 | 453794.5605 | 0.9937 | -0.238 | 0.01 | 2453794.6225 | 0.3089 | -0.467 | 0.019 |
| 453796.5584 | 0.4132 | -1.139 | 0.047 | 2453794.5619 | 0.1228 | -0.707 | 0.02 | 2453794.624 | 0.3140 | -0.448 | 0.018 |
| 2453796.5611 | 0.4215 | -1.071 | 0.044 | 2453794.5622 | 0.9988 | -0.229 | 0.009 | 2453796.432 | 0.0160 | 0.150 | 0.006 |
| 2453796.5637 | 0.4299 | -1.021 | 0.042 | 2453794.5635 | 0.1279 | -0.713 | 0.029 | 2453796.435 | 0.0243 | 0.133 | 0.005 |
| 2453796.5664 | 0.4382 | -1.007 | 0.041 | 2453794.5651 | 0.1329 | -0.738 | 0.03 | 2453796.4378 | 0.0327 | 0.098 | 0.004 |
| 153796.5690 | 0.4466 | -0.968 | 0.040 | 2453794.5667 | 0.1380 | -0.759 | 0.031 | 2453796.4404 | 0.0410 | 0.049 | 0.002 |
| 2453796.5717 | 0.4549 | -0.930 | 0.038 | 2453794.5683 | 0.1430 | -0.765 | 0.031 | 2453796.4431 | 0.0494 | 0.005 | 0.000 |
| 2453796.5743 | 0.4632 | -0.878 | 0.036 | 2453794.5699 | 0.1481 | -0.783 | 0.032 | 2453796.4457 | 0.0577 | -0.046 | 0.002 |
| 2453796.5770 | 0.4716 | -0.850 | 0.035 | 2453794.5715 | 0.1532 | -0.762 | 0.031 | 2453796.4484 | 0.0661 | -0.090 | 0.004 |
| 2453796.5796 | 0.4800 | -0.807 | 0.033 | 2453794.5715 | 0.0283 | -0.224 | 0.009 | 2453796.4510 | 0.0744 | -0.132 | 0.005 |
| 2453796.5823 | 0.4883 | $-0.775$ | 0.032 | 2453794.5731 | 0.1582 | -0.782 | 0.032 | 2453796.4537 | 0.0828 | -0.176 | 0.007 |

Table 1 - Continued

|  | Phase | $\Delta B$ | Error | ID | Phase | $\Delta V$ | Error | ID | Phase | $\Delta R$ | Error |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2453 | 0.4966 | -0.775 | 0.032 | 794. | 0.0334 | -0.25 | 0.01 | 796. | 0.0911 | 209 | 0.009 |
| 2453796.5876 | 0.5050 | -0.7 | 0.032 | 245 | 0. | -0. | . 032 | 245 | 0.0995 | -0.240 |  |
| 2453796.5902 | 0.5 | -0.8 | 0.03 |  | 0.0384 | -0.2 | 0.011 |  | 0.1079 | -0.267 |  |
| 245 | 0. | -0.81 | 0.033 |  |  |  | 0.032 |  | 0.1162 |  |  |
| 2453 | . |  | 0.034 |  |  |  | 0.012 |  |  |  |  |
| 2453 | 0.5384 | -0. | 0.037 |  | 0.1735 |  | . 032 |  |  |  |  |
|  | 0.5468 | -0 | 0.038 | 245 | 0.048 |  | . 014 | 2453796.4722 |  | -0.342 |  |
|  | 0.555 | -0 | 0.040 |  |  |  |  |  |  |  |  |
| 2453796.60 | 0. | -1. | 0.041 | 2453794.57 | 0.053 | -0 | . 013 | 2453796.4775 | 0.1580 | -0.367 | 0.015 |
| 2453796.6088 | 0.5719 | -1.03 | . 42 | 245 | 0.18 | -0.7 | . 032 | 245 | 0.1663 | -0 |  |
| 537 | 0.5802 | -1.092 | 0.045 | 2453794.5812 | 0.05 | $-0.37$ | 0.01 | 2453 | 0.1747 | -0.399 | 0.016 |
| 537 | 0.5885 | -1.095 | 0.045 | 245 | 0.18 | -0.8 | 0.03 | 2453796. | 0.3158 | -0.445 | 0.018 |
| 2453796.6167 | 0.596 | -1.163 | 0.04 | 245 | 0.0 | -0.403 | 0.01 | 2453796.53 | 0.3241 | -0.437 | 0.018 |
| 2453796.6194 | 0.605 | -1.207 | 0.049 | 245 | 0.1938 | -0.8 | 0.0 | 453 | 0.332 | -0.427 | . 17 |
| 2453796.6220 | 0.6 | -1.180 | 0.048 | 245 | 0.1989 | -0.8 | 0.0 | 2453796.5355 | 0.34 | -0.417 | 17 |
| 2453796.6247 | 0.6 | -1.208 | 0.049 | 245 | 0.20 | $-0.87$ | 0.0 | 2453796.5381 | 0.34 | -0.4 | 0.017 |
| 2453796.627 | 0. | -1.22 | 0.050 | 245 | 0.209 | $-0.86$ | . 03 | 2453796.5408 | . 35 | -0.39 | 0.016 |
|  |  | -1.23 | 0.050 |  | 0.2141 | -0.8 | 0.036 |  | . 36 | -0.3 |  |
|  |  | -1.256 | 0.051 |  |  |  |  |  |  |  |  |
|  | 0.6554 | -1 |  |  |  | -0 |  |  |  | -0.347 |  |
|  | 0.65 | -1.27 | 0.052 |  |  | -0.904 |  |  |  |  |  |
| 2453796.6406 | 0 | -1 | 0.052 | 2453794.6069 | 0.2648 | -0.894 | 0.037 | 2453796.5540 | 0.3992 | -0.306 |  |
| 2453796.6432 | 0.6 | -1 | 0.053 | 2453794.6117 | 0.2801 | -0.890 | 0.036 | 2453796.5567 | 0.4076 | -0.277 |  |
| 2453796.6459 | 0. | -1. | 0.054 | 2453794.6133 | 0.285 | -0. | 0.036 | 2453796.5593 | 0.4160 |  | 0.010 |
| 2453796.6485 | 0. | -1.32 | 0.054 | 24 | 0.0 | -0. | 0.009 | 24 | 0.4243 | -0.222 | 0.009 |
| 2453796.6512 | 0.7 | -1.31 | 0.054 | 245 | 0.0 | -0. | 0.01 | 245 | 0.4327 | -0 | 0.007 |
| 2453796.6597 | 0. | -1.32 | 0.054 | 245 | 0.0335 | -0.30 | 0.0 | 245 | 0.4 | -0. | 0.006 |
| 2453911.376 | 0. | -0.99 | 0.041 | 245 | 0.041 | -0.34 | 0.0 | 6.56 | . 44 | -0.1 | . 005 |
| 2453911.379 | 0. | -0.94 | 039 | 245 | 0.05 | -0.41 | 0.017 | 仿 | 0.45 | -0.076 | 0.003 |
| 2453911.3821 | 0.4627 | -0.92 | . 038 | - | 0.0585 | -0. | 0.019 | 2453796.5752 | d | -0.029 | 0.001 |
| 2453911.384 | 0.4716 | -0 | 36 | 2453796.4492 | 0.066 | -0. | 0.021 | 2453796.5778 | 0.4744 |  | 0.000 |
| 2453911.3878 | 0 | -0 | 0.034 | 2453796.4519 | 0.0752 | $-0.550$ | 0.023 | 2453796.5805 | 0.4828 |  |  |
| 2453911.390 |  | -0 | 0.033 | 2453796.4545 |  | -0.589 |  | 2453796.5831 |  |  |  |
| 2453911.393 |  | -0. | 0.032 | 2453796.4572 | 0.0920 | -0.608 |  | 2453796.5858 |  |  |  |
| 2453911.396 |  |  |  | 2453796.45 | 0.1003 |  |  | 2453796.5884 |  |  |  |
|  | 0 | -0. |  | 2453796.4625 |  |  |  |  |  |  |  |
| 2453911.4019 | 0.5252 | -0. |  |  |  |  | 0.029 | 24 | 0.5 |  |  |
|  | 0.5 | $-0.863$ | . | 2453796. | 0.12 | -0.71 | 0.02 | 2453796. | 0.5328 | -0.021 |  |
| 2453911.4076 |  | -0.941 | . 03 | 2453796. | 0.13 | -0.73 | 0.03 | 2453796.59 | 0.5412 | -0.05 |  |
| 2453911.4104 | 0.55 | -0.96 | 0.039 | 2453796. | 0.14 | -0.74 | 0.03 | 2453796.60 | 0.54 | -0.090 | . 004 |
| 2453911.4133 | 0.56 | -1.00 | 0.041 | 245379 | . 1 | -0.762 | 0.03 | 5 | . 55 | -0.131 | 0.005 |
| 2453911.4161 | 0.569 | -1.063 | 0.043 | 245 | 0.15 | -0.78 | . 03 | 2453 | . 56 | -0.169 | 07 |
| 2453911.4189 | 0.578 | -1.093 | 0,045 | 2453 | 0.16 | -0.79 | 0.03 | 24537 | . 57 | -0.204 | 0.008 |
| 2453911.4218 | 0.58 | -1.122 | 046 | 245 | 0.175 | -0.800 | . 033 | 2453 | . 58 | -0.239 | 0.010 |
| 2453911.4246 | 0.5967 | -1.153 | . 47 | 245 | 0.1838 | -0.819 | . 033 | 2453796.6149 | 0.5914 | -0.271 |  |
| 2453911.4275 |  | -1.17 |  | 2453796.4890 |  | -0. |  |  |  | -0.3 |  |
| 2453911.4303 |  | -1 |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | -0. |  |  |  |  |  |
| 2453911.4360 | 0.63 | -1.24 | 0.051 | 2453796. | . | -0.8 |  | 24537 | . 62 | -0.358 |  |
| 2453911 | 0.64 | -1.28 | 0.0 | 2453796.4996 | 0.2 | $-0.868$ | . 03 | 2453796. | 0.6331 | -0.375 | , 15 |
| 2453911. | 0.6504 | -1.264 | 0.05 | 2453796.5023 | 0.234 | -0.880 | 0.03 | 2453796.63 | 0.6415 | -0.391 | . 016 |
| 2453911.4456 | 0.6629 | -1.332 | 0.054 | 2453796.5049 | 0.242 | -0.89 | 0.036 | 2453796.633 | 0.6499 | -0.404 | 0.017 |
| 2453911.448 | 0.6718 | -1.318 | 0.054 | 2453796.5076 | 0.2507 | $-0.885$ | 0.03 | 2453796.63 | 0.6582 | -0.418 | 0.017 |
| 2453911.4513 | 0.6807 | -1.336 | 0.055 | 2453796.5102 | 0.259 | -0.885 | 0.036 | 2453796.63 | 0.6666 | $-0.421$ | 0.017 |
| 2453911.4541 | 0.6896 | -1.347 | 0.055 | 2453796.5129 | 0.2675 | -0.888 | 0.036 | 2453796.6415 | 0.6749 | -0.440 | 0.018 |
| 53911.4569 | 0.6985 | -1.319 | 0.054 | 2453796.5155 | 0.2758 | -0.882 | 0.036 | 2453796.6441 | 0.6832 | -0.442 | 018 |
| 53911.4598 | 0.7075 | -1.319 | 0.054 | 2453796.5284 | 0.3165 | -0.858 | 0.035 | 2453796.6467 | 0.6916 | -0.458 | . 019 |
| 53911.4626 | 0.7164 | -1.315 | 0.054 | 2453796.5311 | 0.3249 | -0.834 | . 034 | 2453796.649 | . 7000 | -0.460 | . 019 |
| 2453911.4654 | 0.7254 | -1.332 | 0.054 | 2453796.5337 | 0.3332 | -0.832 | 0.034 | 2453796.652 | 0.7084 | -0.471 | 0.019 |
| 53911.468 | . 73 | -1.315 | 0.054 | 2453796.53 | 0.34 | -8823 | 0.034 | 2453835.3 | 0.8453 | -0.363 | 0.015 |

Table 1 - Continued

| JD | Phase | $\Delta B$ | Error | JD | Phase | $\Delta V$ | Error | JD | Phase | $\Delta R$ | Error |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2453911.4711 | 0. | -1 | 0 | 2453796.5390 | 0. | -0 | 0.0334 | 2453835.3938 | 0.8546 | -0.347 | 0.014 |
| 2453911.4711 | 0.7 | -1.3 | 0.0 | 24 | 0.3 | -0. | 0.033 | 2453835.3975 | 2 | -0 | 0.013 |
| 553911.4739 | 0.7522 | -1.340 | 0.055 | 245 | 0.3 | -0. | 0.032 | 2453835.4012 | 0.8899 | -0. | 0.012 |
| 2453911.4739 | 0.7522 | -1.340 | 0.055 | 2453796.5470 | 0.3750 | -0.768 | 0.031 | 2453835.4049 | 0.9015 | -0.2 | 0.010 |
| 2453911.4768 | 0.761 | -1.369 | 0.056 | 2453796.5496 | 0.3833 | -0.752 | 0.031 | 2453835.4086 | 0.9132 | -0.198 | 0.008 |
| 553911.4796 | 0.7 | -1.376 | 0.056 | 2453796.5523 | 0.39 | -0.7 | , | 2453835.4123 | 0.9248 | -0.146 | 006 |
| 2453911.4851 | 0.7 | -1. | 0.054 | 2453796.5549 | 0.4000 | -0 | 0.029 | 2453835.4159 | 61 | -0. | 03 |
| 9 | 0.7 | -1. | 0.0 | 24 | 0.4083 | -0. | 0.028 | 2453835.4196 | 0.9479 | -0 | 0.001 |
| 53911.4908 | 0.8 | -1.265 | 0.05 | 24 | 0. | -0. | 0.027 | 2453835.4233 | 0.9595 | , 42 | 0.002 |
| 53911.4936 | 0.8 | -1.253 | 0.0 | 2453796.5629 | 0. | -0. | 0.025 | 2453835.4270 | 0.9712 | 0.096 | 0.004 |
| 53911.4964 | 0.8230 | -1.263 | 0.052 | 2453796.5655 | 0.4334 | -0.567 | 0.023 | 2453835.5332 | 0.3040 | -0.464 | 0.019 |
| 53911.4992 | 0.8319 | -1.274 | 0.052 | 2453796.5682 | 0. | -0.545 | 0.022 | 2453835.5369 | 0.3157 | -0.450 | 0.018 |
| 1.5021 | 0.8409 | $-1.281$ | . 0 |  |  | -0. | 0.021 | 6 | 0.3274 | -0. | 8 |
| 53911.5049 | 0.8 | -1.2 | 0.0 | 24 | 0.4585 | -0. | 0.019 | 24 | 0.3390 | -0. | 7 |
| 53911.5077 | 0.8587 | -1. | 0.05 | 2453796.5 | 0.4 | -0.441 | 0.0 | 2453835 | 0.3507 | -0. | 6 |
| 53911.5105 | 0.8676 | -1.182 | 0.048 | 2453796.5787 | 0.4751 | -0.385 | 0.016 | 2453835.5516 | 0.3623 | -0.389 | 0.016 |
| 53911.5133 | 0.876 | -1.138 | 0.047 | 2453796.5814 | 0.4 | -0.365 | 0.015 | 2453835.5554 | 0.3740 | -0.37 | 0.015 |
| 53911.5162 | 0.88 | -1.147 | 0.04 | 2453796.5 | 0.4919 | -0.352 | 0.014 | 2453835.5591 | 0.3857 | $-0.35$ | 014 |
| 53911.5190 | 0.8943 | -1.149 | 0.0 | 2453796.5893 | 0.5085 | -0.361 | 0.015 | 2453835.562 | 0.3973 | -0.31 | 析 |
| 53911.5219 | 0.9033 | -1.087 | 0.0 | 2453796.5920 | 0.5169 | -0.377 | 0.015 | 245 | 0.7585 | -0.442 | 8 |
| 53911.5247 | 0.9122 | -1. | 0.0 | 24537 | 0.5253 | -0.412 | 0.017 | 245 | 0.7669 | -0.43 | 18 |
| 53911.5275 | 0.9211 | -1.046 | 0.043 | 2453796.5973 | 0.5337 | -0.437 | 0.018 | 2453850.5886 | 0.7753 | -0.437 | 0.018 |
| 53911.5303 | 0.930 | -0.966 | 0.039 | 2453796.5999 | 0.5420 | -0.469 | 0.019 | 2453850.593 | 0.7920 | -0.43 | 0.018 |
| 553911.5332 | 0.939 | -0.963 | 0.03 | 2453796.6 | . 5 | -0.49 | 0.02 | 24 | 0.8004 | -0.42 | 0.017 |
| 453911.5360 | 0.947 | -0.863 | 0.03 | 2453796.6052 | . 55 | -0.55 | 0.023 | 2453850.599 | 0.8088 | -0.426 | 17 |
| 53911.5388 | 0.9568 | -0.780 | 0.03 | 2453796.6079 |  | -0.585 | 0.0 | 245 | 0.8172 | -0. | 0.017 |
| 453911.5417 | 0.9658 | -0.698 | 0.029 | 2453796.6105 | 0.5755 | -0.629 | 0.026 | 2453850.6046 | 0.8256 | -0.40 | 0.017 |
| 53911.5445 | 0.9747 | -0.66 | 0.02 | 2453796.6132 | . 583 | -0.675 | 0.028 | 453850.607 | 0.8340 | -0.38 | . 016 |
| 53911.5474 | 0.9837 | $-0.66$ | 0.02 | 2453796.6158 | . 592 | -0.679 | 0.028 | 2453878.5321 | 0.8956 | -0.31 | . 013 |
| 453911.5502 | 0.9926 | -0.66 | 0.02 | 2453796.6185 | 0.600 | -0.72 | 0.03 | 2453878. | 0.9030 | -0.22 | 0.009 |
| 2453911.5530 | 0.00 | -0.618 | 0.025 | 2453796 | 0.608 | -0.753 | 0.03 | 2453878. | 0.9113 | -0.20 | 0.008 |
| 453911.5559 | 0.0105 | -0.606 | 0.025 | 2453796.6238 | 0.6172 | -0.769 | 0.031 | 2453878.5397 | 0.9197 | -0.230 | 0.009 |
| 53911.5587 | 0.0194 | -0.652 | 0.027 | 2453796.6264 | 0.6256 | -0.778 | 0.032 | 2453878.5530 | 0.9614 | 0.006 | 0.000 |
| 53911.5615 | 0.0283 | -0.66 | 0.02 | 2453796.6 | . 63 | -0.79 | 0.032 | 8.555 | 0.9698 | 0.060 | . 003 |
| 553911.5643 | 0.0372 | -0.74 | 0.03 | 2453796.6 | 0.642 | -0.802 | 0.033 | 2453878.5583 | 0.9782 | 0.086 | 0.004 |
| 2453911.5672 | 0.0 | -0.752 | 0.03 | 2453796 | 0.6507 | -0.830 | 0.03 | 2453878.5609 | 0.9745 | 0.124 | . 005 |
| 453911.5700 | 0.0551 | -0.880 | 0.036 | 2453796.6370 | 0.6590 | -0.836 | 0.034 | 2453878.5636 | 0.9829 | 0.147 | 0.006 |
| 53911.5728 | 0.0640 | -0.983 | 0.040 | 2453796.6397 | 0.6673 | -0.857 | 0.035 | 2453878.5662 | 0.9912 | 0.155 | 0.006 |
| 53911.5756 | 0.0729 | -0.970 | 0.040 | 2453796.6423 | . 675 | -0.85 | . 035 | 911.373 | 0.8968 | -0.18 | 0.008 |
| 53911.5785 | 0.0818 | -1.112 | 0.045 | 2453796.6450 | 0.684 | -0.866 | 0.035 | 2453911.37 | 0.9099 | -0.15 | 0.006 |
| 553911.5813 | 0.0908 | -1.070 | 0.04 | 2453796.6476 | 0.692 | -0.87 | 0.036 | 2453911.3803 | 0.9188 | -0.10 | . 004 |
| 2453911.5841 | 0.0997 | -1.042 | 0.043 | 2453796.6503 | 0.7007 | -0.883 | 0.036 | 2453911. | 0.9278 | -0.067 | 0.003 |
| 2453911.5870 | 0.1086 | -1.121 | 0.046 | 2453796.6589 | 0.7728 | -0.865 | 0.035 | 2453911.3859 | 0.9367 | -0.034 | 0.001 |
| 53911.5898 | 0.1175 | -1.083 | 0.044 | 2453796.6615 | 0.7811 | -0.852 | 0.035 | 2453911.4437 | 0.6570 | -0.43 | 0.018 |
| 453911.5926 | 0.1265 | -1.184 | 0.048 | 2453911.5264 | 0.937 | -0.525 | 0.021 | 2453911.4466 | 0.6660 | -0.425 | 0.017 |
| 2453911.5955 | 0.1354 | -1.234 | 0.050 | 2453911.5293 | 0.9467 | -0.469 | 0.019 | 2453911.4522 | 0.6838 | -0.450 | 0.018 |
| 2453911.5983 | 0.1444 | -1.270 | 0.052 | 2453911.5321 | 0.9556 | -0.437 | 0.018 | 2453911.4579 | 0.7016 | -0.478 | 0.020 |
| 2453911.6012 | 0.1533 | -1.240 | 0.051 | 2453911.5349 | 0.9646 | -0.367 | 0.015 | 2453911.4607 | 0.7106 | -0.475 | 0.019 |
| 2453911.6040 | 0.1622 | -1.243 | 0.051 | 2453911.5378 | 0.9735 | -0.292 | 0.012 | 2453911.4636 | 0.7195 | -0.476 | 0.019 |
| 2453911.6068 | 0.1711 | -1.285 | 0.053 | 2453911.5406 | 0.9825 | -0.253 | 0.01 | 2453911.5455 | 0.9778 | 0.129 | 0.005 |

## 3 ORBITAL PERIOD ANALYSIS

Issues related to stability of the orbital period for the system TY Boo were first recognized by Szafraniec (1953), who found a cyclic period variation of about 127 d . A cubic equation for the ephemeris was obtained by Wood \& Forbes (1963) with a rate of period increase of $d P / d E=$ $+7.79 \times 10^{-10} \mathrm{~d}^{2}$ cycle ${ }^{-1}\left(d P / d t=+1.79 \times 10^{-6} \mathrm{~d} \mathrm{yr}^{-1}\right)$. Their study was based on only 22 times

Table 2 Newly Observed Times of Light Minima for TY Boo in the $B V R$ Bands

| HJD | Error | Min | Filter |
| :--- | :---: | :---: | :---: |
| 2453794.47770 | 0.0003 | I | $B$ |
| 2453794.48280 | 0.0006 | I | $V$ |
| 2453794.49470 | 0.0002 | I | $R$ |
| 2453796.55590 | 0.0005 | II | $B$ |
| 2453796.55630 | 0.0002 | II | $V$ |
| 2453796.55640 | 0.0001 | II | $R$ |
| 2453835.39900 | 0.0013 | I | $B$ |
| 2453835.39902 | 0.0001 | I | $V$ |
| 2453835.39903 | 0.0002 | I | $R$ |
| 2453850.46370 | 0.0005 | I | $V$ |
| 2453850.46670 | 0.0015 | II | $B$ |
| 2453850.47210 | 0.0003 | II | $V$ |
| 2453850.62220 | 0.0004 | II | $R$ |
| 2453878.53750 | 0.0005 | I | $V$ |
| 2453878.53780 | 0.0011 | I | $R$ |
| 2453911.36400 | 0.0004 | I | $B$ |
| 2453911.52300 | 0.0006 | I | $V$ |
| 2453911.52360 | 0.0004 | I | $R$ |
| 2453911.52370 | 0.0010 | II | $B$ |

of light of minima. Carr (1972) confirmed the period $\left(P=0.317146^{\mathrm{d}}\right)$ given by Wood \& Forbes (1963).

A study of the period by Samec \& Bookmyer (1987) gives no indication of the cyclic period variation which was suggested by Szafraniec. A noncontinuous period variation was reported by Milone et al. (1991). They recorded a rapidly developing Ca II flare in the system. Li et al. (2005) found two periodic variations ( 31.5 and 11.76 yr ) superimposed on a continuous increase ( $d P / d t=$ $+6.28 \times 10^{-8} \mathrm{~d} \mathrm{yr}^{-1}$ ). They indicate there is a continuous increase in the mass transfer from the secondary to the primary, rather than an expansion of the primary due to its dynamical instability. Yang et al. (2007) concluded there was a secular period decrease superimposed on a cyclic variation. They attributed this decrease to the mass transfer from the more massive component to the less massive component, which appears as a shrinking of the inner and outer critical Roche lobes, which caused the degree of contact to increase. A study of the period based on published minima up to 2011 by Christopoulou et al. (2012) showed a long term period decrease.

In the present work, we used the list collected by Christopoulou et al. which covers the interval from 1926 to 2011 together with our new 19 minima, all published from 2011 to 2014. In addition, we added published minima before 2011 that were not included in the Christopoulou et al. list. An additional 76 minima were added in our study, which results in a total of 454 light minima timings, spanning over 88 years ( $\sim 101277$ revolutions). These data were used to follow and update the long term orbital behavior of the system TY Boo by means of an observed minus calculated ( $O-C$ ) diagram. $(O-C)$ for the eclipse timings have been calculated using a linear ephemeris (Kreiner et al. 2001 eq. (1)) and are listed in Table 3.

Table 3 Times of Light Minima for TY Boo (2011-2014)

| HJD | Method | $E$ | $O-C$ | $(O-C) \mathrm{p}$ | References |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 2432688.5390 | vis | -47057 | 0.0160 | 0.0038 | Szafraniec (1948) |
| 2432688.5390 | vis | -47057 | 0.0160 | 0.0038 | Szafraniec (1948) |
| 2433082.4350 | vis | -45815 | 0.0129 | 0.0009 | Szafraniec (1948) |
| 2433362.4660 | vis | -44932 | 0.0014 | -0.0102 | Szafraniec (1948) |
| 2443587.8020 | vis | -12690.5 | -0.0221 | -0.0057 | Samolyk (1992) |
| 2444334.7090 | vis | -10335.5 | -0.0010 | 0.0132 | Samolyk (1992) |

Table 3 - Continued

| HJD | Method | $E$ | O-C | $(O-C) \mathrm{p}$ | References |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2444402.7250 | vis | -10121 | -0.0135 | 0.0005 | Samolyk (1992) |
| 2445173.7150 | vis | -7690 | -0.0127 | -0.0016 | Samolyk (1992) |
| 2445492.7770 | vis | -6684 | -0.0026 | 0.0072 | Samolyk (1992) |
| 2446210.7980 | vis | -4420 | -0.0069 | -0.0005 | Samolyk (1992) |
| 2446210.8000 | vis | -4420 | -0.0049 | 0.0015 | Samolyk (1992) |
| 2446226.8110 | pe | -4369.5 | -0.0100 | -0.0036 | Milone et al. (1991) |
| 2446227.7629 | pe | -4366.5 | -0.0095 | -0.0031 | Milone et al. (1991) |
| 2446231.7266 | pe | -4354 | -0.0102 | -0.0038 | Milone et al. (1991) |
| 2446600.7230 | vis | -3190.5 | -0.0166 | -0.0121 | Samolyk (1992) |
| 2446606.7660 | vis | -3171.5 | 0.0006 | 0.0051 | Samolyk (1992) |
| 2446678.6020 | vis | -2945 | 0.0023 | 0.0065 | Samolyk (1992) |
| 2446875.7160 | vis | -2323.5 | 0.0082 | 0.0114 | Samolyk (1992) |
| 2446951.6690 | vis | -2084 | 0.0040 | 0.0069 | Samolyk (1992) |
| 2447010.6550 | vis | -1898 | 0.0003 | 0.0028 | Samolyk (1992) |
| 2447219.8060 | vis | -1238.5 | -0.0085 | -0.0070 | Samolyk (1992) |
| 2447263.5774 | vis | -1100.5 | -0.0036 | -0.0024 | Agerer (1988) |
| 2447263.5781 | vis | -1100.5 | -0.0029 | -0.0017 | Agerer (1988) |
| 2447299.7430 | vis | -986.5 | 0.0070 | 0.0081 | Samolyk (1992) |
| 2447316.7060 | vis | -933 | 0.0025 | 0.0035 | Samolyk (1992) |
| 2447612.6025 | vis | 0 | -0.0010 | -0.0015 | Hubscher et al. (1989) |
| 2447612.6032 | vis | 0 | -0.0003 | -0.0008 | Hubscher et al. (1989) |
| 2447681.7510 | vis | 218 | 0.0090 | 0.0082 | Samolyk (1992) |
| 2448161.5940 | vis | 1731 | 0.0056 | 0.0023 | Samolyk (1992) |
| 2448330.6410 | vis | 2264 | 0.0122 | 0.0081 | Samolyk (1992) |
| 2448331.7410 | vis | 2267.5 | 0.0021 | -0.0020 | Samolyk (1992) |
| 2448661.8970 | vis | 3308.5 | 0.0060 | 0.0004 | Samolyk (1992) |
| 2448690.5994 | vis | 3399 | 0.0065 | 0.0006 | Hubscher et al. (1989) |
| 2448717.7150 | vis | 3484.5 | 0.0058 | -0.0001 | Samolyk (1992) |
| 2448724.8440 | vis | 3507 | -0.0010 | -0.0070 | Samolyk (1992) |
| 2448770.6700 | vis | 3651.5 | -0.0031 | -0.0093 | Samolyk (1992) |
| 2453794.4777 | ccd | 19492 | 0.0059 | -0.0096 | This paper |
| 2453794.4828 | ccd | 19492 | 0.0110 | -0.0045 | This paper |
| 2453794.4947 | ccd | 19492 | 0.0229 | 0.0074 | This paper |
| 2453796.5559 | ccd | 19498.5 | 0.0226 | 0.0071 | This paper |
| 2453796.5563 | ccd | 19498.5 | 0.0230 | 0.0075 | This paper |
| 2453796.5564 | ccd | 19498.5 | 0.0231 | 0.0076 | This paper |
| 2453835.3990 | ccd | 19621 | 0.0150 | -0.0004 | This paper |
| 2453835.3990 | ccd | 19621 | 0.0150 | -0.0004 | This paper |
| 2453835.3990 | ccd | 19621 | 0.0150 | -0.0004 | This paper |
| 2453850.4637 | ccd | 19668.5 | 0.0151 | -0.0003 | This paper |
| 2453850.4667 | ccd | 19668.5 | 0.0181 | 0.0027 | This paper |
| 2453850.4721 | ccd | 19668.5 | 0.0235 | 0.0081 | This paper |
| 2453850.6222 | ccd | 19669 | 0.0150 | -0.0003 | This paper |
| 2453878.5375 | ccd | 19757 | 0.0212 | 0.0059 | This paper |
| 2453878.5378 | ccd | 19757 | 0.0215 | 0.0062 | This paper |
| 2453911.3640 | ccd | 19860.5 | 0.0228 | 0.0076 | This paper |
| 2453911.5230 | ccd | 19861 | 0.0232 | 0.0080 | This paper |
| 2453911.5236 | ccd | 19861 | 0.0238 | 0.0086 | This paper |
| 2453911.5237 | ccd | 19861 | 0.0239 | 0.0087 | This paper |
| 2454958.7319 | vis | 23163 | 0.0061 | -0.0051 | Bialozynski (2009) |
| 2454958.7420 | vis | 23163 | 0.0162 | 0.0050 | Bialozynski (2009) |
| 2455232.9082 | vis | 24027.5 | 0.0071 | -0.0026 | Menzies (2010) |
| 2455642.3477 | vis | 25318.5 | 0.0072 | 0.0000 | Hubscher (2011) |
| 2455642.5067 | vis | 25319 | 0.0077 | 0.0004 | Hubscher (2011) |
| 2455648.3732 | ccd | 25337.5 | 0.0069 | -0.0003 | Hubscher et al. (2012) |
| 2455664.0717 | ccd | 25387 | 0.0065 | -0.0006 | Shiokawa (2011) |
| 2455664.2305 | ccd | 25387.5 | 0.0068 | -0.0003 | Shiokawa (2011) |
| 2455681.5158 | vis | 25442 | 0.0074 | 0.0005 | Parimucha et al. (2013) |
| 2455992.6392 | ccd | 26423 | 0.0077 | 0.0029 | Honkova (2012) |
| 2455992.6395 | ccd | 26423 | 0.0080 | 0.0032 | Honkova (2012) |

Table 3 - Continued

| HJD | Method | $E$ | $O-C$ | $(O-C) \mathrm{p}$ | References |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 2456023.8779 | vis | 26521.5 | 0.0072 | 0.0027 | Diethelm (2012) |
| 2456062.7300 | vis | 26644 | 0.0085 | 0.0043 | Sabo (2012) |
| 2456069.3859 | vis | 26665 | 0.0043 | 0.0001 | Hubscher \& Lehmann (2013) |
| 2456069.5470 | vis | 26665.5 | 0.0068 | 0.0026 | Hubscher \& Lehmann (2013) |
| 2456078.4252 | vis | 26693.5 | 0.0049 | 0.0007 | Parimucha et al. (2013) |
| 2456085.7218 | vis | 26716.5 | 0.0070 | 0.0030 | Diethelm (2012) |
| 2456382.7220 | vis | 27653 | -0.0028 | -0.0045 | Menzies (2010) |
| 2456399.6891 | ccd | 27706.5 | -0.0032 | -0.0048 | Poklar (2013) |
| 2456408.4154 | vis | 27734 | 0.0015 | 0.0002 | Hubscher (2013) |
| 2456408.5742 | vis | 27734.5 | 0.0018 | 0.0003 | Hubscher (2013) |

For a more accurate result, we discarded some uncertain minima times that were collected (i.e. the first visual minimum taken in 1926) which do not agree with the others in the $(O-C)$ diagram. Scattering of the minima in the $(O-C)$ diagram may result from cycle to cycle variation in the observed light curves, which leads to asymmetry and also uncertainty in times of minima calculations. The $(O-C)$ values are presented in Figure 2 versus the integer cycle E; no distinctions have been made between primary and secondary minima. It is clear that the behavior of the $(O-C)$ points in Figure 2 cannot adequately represent any light elements derived by a linear fit. In order to follow the periodic behavior of the system TY Boo through the 88 years since its discovery, we divided the $(O-C)$ variation into four intervals, $E_{i}-E_{i-1}, i=1,2,3,4$.

Table 4 summarizes the intervals and the best fit data with standard deviations SD, correlation coefficients $r$ and residual sum of squares. The time interval $\Delta E$ and the corresponding changes in the period $\Delta P$ for each interval according to the best fit of the $(O-C)$ residuals are also listed in Table 4. It is clear from the table that the period of the system TY Boo shows two stages of increase and a similar trend of decrease, which looks like periodic behavior. The $(O-C)$ residuals in Figure 2 show two peaks, representing the turning points from the phase of period increase to decrease. The first peak is at HJD $\sim 24329961949$ (1949) while the second one is at HJD $\sim 2452362$ (2002), with an interval of about 53 yr between them. The general trend of the $(O-C)$ diagram can be represented by a sixth degree polynomial with a residual sum of squares $=0.0094$ and correlation coefficient $=0.89$ as follows

$$
\begin{align*}
\operatorname{Min} \mathrm{I}= & 2447612.6040+0.3171506 \cdot E-2.929 \times 10^{-12} \cdot E^{2}-2.051 \times 10^{-15} \cdot E^{3} \\
& -7.491 \times 10^{-21} \cdot E^{4}+4.049 \times 10^{-25} \cdot E^{5}-9.218 \times 10^{31} \cdot E^{6} . \tag{2}
\end{align*}
$$

The new light elements in Equation (2) can be used to estimate minimum times in the next few years. The equation yields a new period $\left(P=0.3171506^{\mathrm{d}}\right)$. The period shows a decrease with the rate $d P / d E=5.858 \times 10^{-12} \mathrm{~d}$ cycle $^{-1}, 6.742 \times 10^{-9} \mathrm{~d} \mathrm{yr}^{-1}$ or 0.058 s century ${ }^{-1}$. The $(O-C)$ p residuals calculated using polynomial ephemeris (Eq. (2)) are listed in Table 3 and displayed in Figure 3.

## 4 LIGHT CURVE STABILITY

The light curve variation of the system TY Boo was noted through the historical survey of published light curves since its discovery in 1926. Observations by Carr (1972) in 1969 were brighter than those of Samec \& Bookmyer (1987). Li et al. (2005) suggested that the more massive component was brighter in 1969 than in 1986, which might be caused by star spot(s) or as a result of the stellar activity. Large scatter was clearly seen in the light curves reported by Samec \& Bookmyer (1987) and Milone et al. (1991), and a rapid light variation occurring night by night was observed near the two maxima and two minima. This phenomenon has been observed in many contact binaries (i.e. KN Per Goderya et al. (1997), CN And Keskin (1989), and AQ Tuc Hilditch \& King (1986)),


Fig. 2 Periodic behavior of TY Boo.


Fig. 3 Calculated residuals from the quadratic ephemeris.
which might be caused by the pulsation of a common envelope due to mass transfer between two components (Li et al. 2002). Studying the light curve variation together with the orbital period of W UMa systems is very important in understanding the evolution of structure in these systems. Applegate (1992) predicts a relation between the orbital period changes and light variations during the same cycle. We studied the possibility of applying the prediction by Applegate to the system

Table 4 Comprehensive Periodic Behavior for the System TY Boo

|  | Intervals $(2400000+)$ |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Parameters | $E_{0}$ to $E_{1}$ | $E_{1}$ to $E_{2}$ | $E_{2}$ to $E_{3}$ | $E_{3}$ to $E_{4}$ |
|  | $29348-32996$ | $32996-40370$ | $40370-52452$ | $52452-56408$ |
| $\Delta E(\mathrm{~d})$ | 3648 | 7374 | 12082 | 3956 |
| $P(\mathrm{~d})$ | 0.3171519 | 0.3171476 | 0.3171502 | 0.3171477 |
| $\Delta P(\mathrm{~d})$ | $2.858 \times 10^{-6}$ | $-1.3949 \times 10^{-6}$ | $1.1849 \times 10^{-6}$ | $-1.2620 \times 10^{-6}$ |
| $\Delta P / P$ | $9.012 \times 10^{-6}$ | $-4.398 \times 10^{-6}$ | $3.7360 \times 10^{-6}$ | $-3.9790 \times 10^{-6}$ |
| $\Delta P / \Delta E($ d/cycle $)$ | $2.485 \times 10^{-10}$ | $-5.999 \times 10^{-11}$ | $3.1103 \times 10^{-10}$ | $-1.0120 \times 10^{-10}$ |
| Epoch $(2400000+)$ | 47612.7507 | 47612.5531 | 47612.6040 | 47612.5643 |
| SD | 0.00559 | 0.00624 | 0.00503 | 0.00303 |
| $r$ | 0.94300 | 0.85700 | 0.84700 | 0.82620 |
| Residual sum of squares | 0.00041 | 0.00261 | 0.01134 | 0.00172 |
| $R^{2}$ | 0.88980 | 0.73450 | 0.71720 | 0.68260 |

Table 5 Light Curve Parameters for TY Boo

| HJD | Date | $D_{\max }$ <br> $(\mathrm{mag})$ | $D_{\min }$ <br> $(\mathrm{mag})$ | $A_{\mathrm{p}}$ <br> $(\mathrm{mag})$ | $A_{\mathrm{s}}$ <br> $(\mathrm{mag})$ | References |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 2441351 | 1972 | $0.009 \pm 0.001$ | $-0.119 \pm 0.006$ | $0.357 \pm 0.018$ | $0.476 \pm 0.024$ | Carr (1972) |
| 2446830 | 1987 | $-0.006 \pm 0.001$ | $0.146 \pm 0.007$ | $0.674 \pm 0.028$ | $0.398 \pm 0.020$ | Samec \& Bookmyer (1987) |
| 2447561 | 1989 | $0.005 \pm 0.001$ | $-0.070 \pm 0.004$ | $0.455 \pm 0.023$ | $0.385 \pm 0.019$ | Samec et al. (1989) |
| 2447926 | 1990 | $0.200 \pm 0.010$ | $0.160 \pm 0.008$ | $0.180 \pm 0.009$ | $0.340 \pm 0.017$ | Rainger et al. (1990) |
| 2448291 | 1991 | $0.030 \pm 0.002$ | $0.075 \pm 0.004$ | $0.460 \pm 0.023$ | $0.385 \pm 0.019$ | Milone et al. (1991) |
| 2453770 | 2006 | $0.010 \pm 0.001$ | $0.135 \pm 0.006$ | $0545 \pm 0.065$ | $0.680 \pm 0.028$ | This paper |
| 2454866 | 2009 | - | $0.089 \pm 0.005$ | - | - | Bialozynski (2009) |
| 2455596 | 2011 | $0.050 \pm 0.002$ | $0.211 \pm 0.010$ | $0.768 \pm 0.031$ | $0557 \pm 0.023$ | Christopoulou et al. (2012) |
| 2456326 | 2013 | - | $0.049 \pm 0.003$ | - | - | Menzies (2013) |

TY Boo. Using the historical published light curves together with our observations in the $V$ band, the light levels (Max I, Min I, Max II and Min II) were evaluated from the curves. The differences in magnitude between both maxima (O'Connell) $D_{\max }$ (Max I - Max II) and minima $D_{\min }$ (Min I - Min II) and amplitude of the primary $A_{\mathrm{p}}$ (Min I - Max I) and secondary $A_{\mathrm{s}}$ (Min II - Max I) have been calculated for each light curve and are listed in Table 5 with their corresponding observers and observational date in years.

Figure 4 displays the variation in magnitude differences $D_{\max }$ and $D_{\min }$, and the amplitude of the primary eclipse $A_{\mathrm{p}}$ and secondary one $A_{\mathrm{s}}$, for TY Boo in the $V$ band. From Figure 4(a), (c) and (d), we can note that the amplitude of the primary and secondary eclipses, $A_{\mathrm{p}}$, and $A_{\mathrm{s}}$ respectively, showed the same trend of variation, but with an opposite trend than what was shown by $D_{\max }$.

The tabulated results lead to a conclusion that the calculated parameters $D_{\max }, D_{\min }, A_{\mathrm{p}}$ and $A_{\mathrm{s}}$ show an oscillatory variation and wave-like behavior like a periodic function, which can be interpreted as periodic action by some physical mechanism. Synchronous periodic variation of both orbital period and light curve parameters ( $D_{\max }, D_{\min }, A_{\mathrm{p}}$ and $A_{\mathrm{s}}$ ) for the system TY Boo may be interpreted as the presence of magnetic activity cycles and/or a mass transfer mechanism.

## 5 LIGHT CURVE MODELING

Light curve solutions for the W UMa system TY Boo estimated by many authors (i.e. Rainger et al. 1990; Milone et al. 1991; Christopoulou et al. 2012) have shown that the less massive, but hotter, star is eclipsed at the primary minimum. Although the light curve solution by Carr (1972) has limited accuracy, it suggested that the system TY Boo can be classified as an A-type W UMa system which consists of two main-sequence components with spectral types G3 and G7 and a mass ratio of 0.88 . Niarchos (1978) re-analyzed Carr's (1972) observations using frequency domain techniques, and suggested that TY Boo was a W UMa system with a small mass ratio of 0.22 and indicated that the smaller component is the hotter one (Rainger et al. 1990).

Light curve analysis by Samec et al. (1989) shows that the system has a spectral type ranging between G4 and G8. Rainger et al. (1990) combined their spectroscopic observations together with photometric observations by Samec \& Bookmyer (1987) to compute the masses and absolute dimensions of the components. Their solution shows that the system TY Boo has components with spectral types G2 and F8. Milone et al. (1991) was the first to suggest a spotted solution with both hot and cold spots on a cooler component, and showed that the published light curves by Carr (1972) and Samec \& Bookmyer (1987) have minimal asymmetry and can be fitted without spots.

Christopoulou et al. (2012) confirmed the spotted model solution suggested by Milone et al. (1991) and produced a model that included a spot on both stellar components. They suggested that the spots were caused by cyclic magnetic activity rather than by an unseen companion. They compared the light curve parameters obtained from 1926 to 2011, and demonstrated that the system


Fig. 4 Variation of the magnitude differences $D_{\max }$ and $D_{\min }$, and the amplitude of the primary $A_{\mathrm{p}}$ and secondary $A_{\mathrm{s}}$ for TY Boo in the $V$ band.

TY Boo has been a difficult system to analyze because it yields widely divergent results in terms of mass ratio and size.

Our observations cover three bandpasses $(B V R)$ and have high accuracy compared to the previously published photometric data. In our modeling we use Mode 3 (overcontact) of the WDint56a Package (Nelson 2009), which is based on the W-D code. The surface temperature of the primary (less massive and hotter) star was fixed at 5732 K , which is compatible with its spectral classification of G3 (Cox 2000).

The individual observations were analyzed instead of complete light curves, which do not reveal a real light variation in the system. The bolometric limb darkening coefficients ( $x_{b}(h)=x_{b}(c)$ and $y_{b}(h)=y_{b}(c)$ ) were adopted and interpolated using the square-root law from van Hamme (1993). Tabulated values and a model atmosphere were applied. Gravity darkening and bolometric albedo were assumed according to the exponents appropriate for convective envelopes ( $T_{\text {eff }}<7500 \mathrm{~K}$ ) in a late spectral type. We adopted $g_{\mathrm{h}}=g_{\mathrm{c}}=0.32$ (Lucy 1967) and the albedo value $A_{\mathrm{h}}=A_{\mathrm{c}}=0.5$ (Ruciński 1969). Mode 3 (overcontact) was applied with a synchronous rotation and a circular orbit was assumed. Some parameters were kept fixed (i.e. $T_{\mathrm{h}}, g, A, X$ ), and the adjustable parameters were the temperature of the cool star $T_{\mathrm{c}}$ for star 2, the monochromatic luminosity L1 for star 1 (the luminosity of star 2 was calculated by the stellar atmosphere model), the surface potential $\Omega_{\mathrm{h}}=$ $\Omega_{\mathrm{c}}$, and the mass ratio $q=\left(M_{\mathrm{c}} / M_{\mathrm{h}}\right)$. The model solution without a spot (not shown here) does not fit the observed light curves well. The parameters of the accepted model are listed in Table 6 with the presence of a dark spot on the cooler component and a hot one on the hotter component, which confirms the spotted solution suggested by Christopoulou et al. (2012) and gives a credible uniform description for the TY boo system. The estimated parameters show that the less massive component is hotter than the more massive one, which verifies the results of Milone et al. (1991) and Christopoulou et al. (2012). The temperature difference between the components is $\Delta T \sim 249 \mathrm{~K}$, and the theoretical $B V R$ light curves for the system TY Boo are displayed in Figure 5. The absolute

Table 6 Photometric Solution for TY Boo

| Parameter | $B V R$ |
| :--- | :---: |
| $i\left(^{\circ}\right)$ | $78.76 \pm 0.16$ |
| $\mathrm{gh}=\mathrm{gc}$ | Fixed |
| $A_{\mathrm{h}}=A_{\mathrm{c}}$ | Fixed |
| $q=\left(M_{\mathrm{c}} / M_{\mathrm{h}}\right)$ | $2.2592 \pm 0.005$ |
| $\Omega_{\mathrm{h}}=\Omega_{\mathrm{c}}$ | $5.5935 \pm 0.010$ |
| $\Omega_{\mathrm{in}}$ | 5.6174 |
| $\Omega_{\text {out }}$ | 4.5571 |
| $T_{\mathrm{h}}(\mathrm{K})$ | 5732 Fixed |
| $T_{\mathrm{c}}(\mathrm{K})$ | $5483 \pm 2$ |
| $L_{\mathrm{h}} /\left(L_{\mathrm{h}}+L_{\mathrm{c}}\right)$ | Fixed |
| $L_{\mathrm{c}} /\left(L_{\mathrm{h}}+L_{\mathrm{c}}\right)$ | Fixed |
| $r_{\mathrm{h}}$ (pole) | $0.2920 \pm 0.0006$ |
| $r_{\mathrm{h}}$ (side) | $0.3048 \pm 0.0007$ |
| $r_{\mathrm{h}}$ (back) | $0.3385 \pm 0.0013$ |
| $r_{\mathrm{c}}$ (pole) | $0.4260 \pm 0.0002$ |
| $r_{\mathrm{c}}$ (side) | $0.4540 \pm 0.0003$ |
| $r_{\mathrm{C}}$ (back) | $0.4819 \pm 0.0006$ |
| Spot parameters for hot star |  |
| Co-latitude | 120 Fixed |
| Longitude | 350 Fixed |
| Spot radius | 16 Fixed |
| Temp. factor | 1.1076 Fixed |
| Spot parameters for cool star |  |
| Co-latitude | 140 Fixed |
| Longitude | 155 Fixed |
| Spot radius | 21 Fixed |
| Temp. factor | 0.7 Fixed |
| $\sum(O-C)^{2}$ | 0.08447 |

Table 7 Absolute Physical Parameters for the System TY Boo

| $M_{\mathrm{h}}$ | $M_{\mathrm{C}}$ | $R_{\mathrm{h}}$ | $R_{\mathrm{C}}$ | $M_{\mathrm{h}}$ | $M_{\mathrm{C}}$ | $L_{\mathrm{h}}$ | $L_{\mathrm{c}}$ | $T_{\mathrm{h}}$ | $T_{\mathrm{C}}$ | Ref. |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\left(M_{\odot}\right)$ | $\left(M_{\odot}\right)$ | $\left(R_{\odot}\right)$ | $\left(R_{\odot}\right)$ | $($ bol $)$ | $($ bol $)$ | $\left(L_{\odot}\right)$ | $\left(L_{\odot}\right)$ | $\left(T_{\odot}\right)$ | $\left(T_{\odot}\right)$ |  |

$0.40 \pm 0.01 \quad 0.93 \pm 0.02 \quad 0.69 \pm 0.01 \quad 1.00 \pm 0.01 \quad 5.28 \pm 0.14 \quad 4.75 \pm 0.15 \quad 0.62 \pm 0.03 \quad 1.02 \pm 0.04 \quad 1.07 \pm 0.04 \quad 1.00 \pm 0.04$ [1]
$0.53 \pm 0.02 \quad 1.14 \pm 0.05 \quad 0.75 \pm 0.03 \quad 1.05 \pm 0.04 \quad 5.29 \pm 0.22 \quad 4.82 \pm 0.02 \quad 0.58 \pm 0.02 \quad 0.89 \pm 0.04 \quad 1.01 \pm 0.04 \quad 0.94 \pm 0.04 \quad$ [2]
$0.57 \pm 0.05 \quad 1.21 \pm 0.06 \quad 0.75 \pm 0.01 \quad 1.07 \pm 0.01 \quad 5.34 \pm 0.22 \quad 4.88 \pm 0.02 \quad 0.54 \pm 0.01 \quad 0.87 \pm 0.02 \quad 0.99 \pm 0.04 \quad 0.88 \pm 0.04 \quad$ [3] $0.53 \pm 0.021 .19 \pm 0.05 \quad 0.73 \pm 0.03 \quad 1.06 \pm 0.04 \quad 5.47 \pm 0.224 .85 \pm 0.20 \quad 0.52 \pm 0.02 \quad 0.92 \pm 0.04 \quad 0.99 \pm 0.040 .95 \pm 0.04 \quad$ [4]
Notes: Subscript ' $h$ ' and ' $c$ ' means hot and cool component respectively. Reference: [1] Rainger et al. (1990); [2] Milone et al. (1991); [3] Christopoulou et al. (2012); [4] This Paper.
physical parameters of the system TY Boo were calculated based on the results of the radial velocity data from Milone et al. (1991) and our new photometric solution. The calculated parameters together with those calculated by previous light curve solutions are listed in Table 7. A three dimensional geometrical structure for the system TY Boo was constructued using the software Package Binary Maker 3.03 (Bradstreet and Steelman, 2004) based on the calculated parameters resulting from our model and is displayed in Figure 6. It is clear from our results that the system TY Boo shows a rapid transformation in physical properties, which can have many interpretations, i.e. Milone et al. (1991) suggested that the system is chromospherically active and a rapidly developing Ca II flare was recorded in the system's spectrum. A shrinking of the inner and outer critical Roche lobes caused an increase in the degree of contact which results from the decrease in orbital period.


Fig. 5 Observed light curves. Observed light curves (filled circles) and fitted light curves (solid lines).


Fig. 6 Geometric structure of the binary system TY Boo.

## 6 EVOLUTIONARY STATUS

In order to investigate the current evolutionary status of the system, we used the physical parameters listed in Table 7. We used the evolutionary tracks computed by Girardi et al. (2000) for both ZAMS stars and terminal age main sequence (TAMS) stars with metallicity $z=0.019$. The components of TY Boo are plotted on mass-luminosity $(M-L)$ and mass-radius $(M-R)$ relations in Figures 7 and 8 respectively. As is clear from these figures, the primary component of the system is located above the TAMS for the $M-L$ relation but it is located on the TAMS for the $M-R$ relation. The secondary component is close to the ZAMS track for both the $M-L$ and $M-R$ relations. In the figures, we also plot the physical parameters computed by other authors listed in Table 7. The locations of both primary and secondary components have more or less the same behavior as in our solution. The same trend is obtained by Christopoulou et al. (2012) for a sample of W-type systems.


Fig. 7 The position of the components of TY Boo on the mass-luminosity diagram. The filled circle denotes the primary and the open circle represents the secondary. Filled and open star symbols represent the masses and luminosities of the other solutions presented in Table 7.


Fig. 8 The position of the components of TY Boo on the mass-radius diagram. The filled circle denotes the primary and the open circle represents the secondary.


Fig. 9 Position of the components of TY Boo on the empirical mass- $T_{\text {eff }}$ relation for lowintermediate mass stars by Malkov (2007).

The location of our physical parameters on the mass-effective temperature ( $M-T_{\text {eff }}$ ) relation is displayed in Figure 9. This shows the relation for intermediate and low mass stars based on data from detached double-lined eclipsing binaries (Malkov 2007). The location of our mass and radius on the diagram indicates there is a good fit for the secondary component but a poor fit for the primary one.

Some open questions have arisen related to the evolutionary status of the TY Boo system, including the mass transfer from the secondary to the primary and its relation with the period change of the system. As the system has a low degree of contact, many authors (i.e. Christopoulou et al. 2012) do not consider the mass transfer to be a possible reason for a period change.

Another open question is what influence does the magnetic activity have on the period change. Our investigation shows that the period change may be attributed to magnetic activity. However, as shown by Stȩpien et al. (2001), the X-ray flux (for the time interval 1990-1991) is weaker than that of single stars, so Christopoulou et al. (2012) excluded magnetic activity as the cause of period change.

## 7 DISCUSSION

New light curves of TY Boo were acquired with a CCD over five nights in the $B V R$ bandpass and 19 new times of light minima were calculated. The parameters calculated by a photometric solution of these light curves by means of the W-D code showed that the less massive component is hotter than the more massive one. The temperature difference between the components is $\Delta T \sim 249 \mathrm{~K}$. The periodic behavior of the system and the new light elements yield a new period ( $P=0.3171506^{\mathrm{d}}$ ) and show a period decrease with the rate $d P / d E=5.858 \times 10^{-12} \mathrm{~d}^{\text {cycle }}{ }^{-1}, 6.742 \times 10^{-9} \mathrm{~d} \mathrm{yr}^{-1}$ or 0.1 s century ${ }^{-1}$. The conclusion reached may be drawn from the following points.
(1) Light curve modeling is performed using the complete light curve from the $B V R$ bandpass. The curves were analyzed by means of the W-D code and the accepted solution confirms the presence of a hot spot on the hotter component and a dark spot on the cooler one. The absolute physical parameters were calculated and compared with those estimated by the previous light curve solutions for the system. The comparison showed that the physical properties of the system transform rapidly, which can be interpreted in terms of chromospheric activity and a rapidly developing Ca II flare recorded in the system's spectrum (Milone et al. 1991).
(2) We performed the first study of long term stability exhibited by this system's light curves and the possible connection with its periodic behavior, by using all published light curves. Long term stability in the system's light curves shows a periodic variation in the magnitude differences $D_{\text {max }}$ and $D_{\text {min }}$ and the amplitude of the primary $A_{\mathrm{p}}$ and secondary $A_{\mathrm{s}}$.
(3) Synchronous periodic variations of both orbital period and light curve parameters ( $D_{\max }, D_{\min }$, $A_{\mathrm{p}}$ and $A_{\mathrm{s}}$ ) for the system TY Boo may be correlated with the presence of magnetic activity cycles and/or a mass transfer mechanism. Future observations, particularly high resolution spectroscopic and photometric measurements, are needed to verify this behavior.
(4) We have investigated the evolutionary status of the system using stellar models. The primary component is near or on the TAMS track, but the secondary component is still on the ZAMS track.

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