LETTERS

Short-living Supermassive Magnetar Model for the Early X-ray Flares Following Short GRBs *

Wei-Hong Gao1 and Yi-Zhong Fan2,3,4

1 Department of Physics and Institute of Theoretical Physics, Nanjing Normal University, Nanjing 210008; gaowei@njnu.edu.cn
2 The Racah Inst. of Physics, Hebrew University, Jerusalem 91904, Israel; yizhongfan@phys.huji.ac.il
3 Purple Mountain Observatory, Chinese Academy of Sciences, Nanjing 210008
4 Lady Davis Fellow

Received 2006 April 22; accepted 2006 August 14

Abstract We suggest a short-lived supermassive magnetar model to account for the X-ray flares following short \( \gamma \)-ray bursts. In this model the central engine of the short \( \gamma \)-ray bursts is a supermassive millisecond magnetar, formed in coalescence of double neutron stars. The X-ray flares are powered by the dipole radiation of the magnetar. When the magnetar has lost a significant part of its angular momentum, it collapses to a black hole and the X-ray flares cease abruptly.

Key words: Gamma-rays: bursts — radiation mechanisms: nonthermal — magnetic fields — stars: neutron — stars: rotation

1 INTRODUCTION

So far, X-ray flares following short GRBs have been detected in GRB 050709 and GRB 050724 (Villasenor et al. 2005; Barthelmy et al. 2005). In GRB 050709, a short GRB localized by HETE-II, two X-ray flares occurred, one \( \sim 10 \) s, and one \( \sim 16 \) days after the GRB (Fox et al. 2005). Details of the flares are unclear owing to paucity of data. Much better X-ray flare data are available for GRB 050724, a short GRB localized by Swift. The data have been summarized in Barthelmy et al. (2005; see also Zhang et al. 2006). The X-ray telescope (XRT) observation started at \( \sim 79 \) s after the trigger. An extended flare-like episode ended at \( \sim 200 \) s, after which the light curve decayed rapidly (with a temporal slope index \( \sim -10 \)). A second, less energetic flare episode peaked at \( \sim 300 \) s, and was followed by another steep decay with a slope \( \sim -7 \). In this work, we call these two flares the “early X-ray flares”. A third, significant flare started at \( \sim 2 \times 10^4 \) s and the decay slope after the peak was \( \sim -2.8 \). We call the third one the “late X-ray flare”.

X-ray flares following short GRBs, like those detected in the long GRB X-ray afterglows, may indicate long-lived activity of the central engine (e.g., Barthelmy et al. 2005; cf. MacFadyen et al. 2006), but the actual mechanism for the long activity of the short GRB central engine is still unclear (Proga & Zhang 2006; Perna et al. 2006; Dermer & Atoyan 2006). The difficulty is that, in the double neutron star coalescence scenario (i.e., the favoured model of short GRBs, Eichler et al. 1989), typical energy input episode is of the same order of the duration of the short burst, provided that after the merger a black hole is formed (e.g., Rosswog & Davis 2002; Lee et al. 2004).

In this work, we suggest that the X-ray flares following short GRBs could be understood if what is formed after the merger of two neutron stars is a millisecond rotating magnetized supermassive neutron star (SMNS), rather than a black hole.

* Supported by the National Natural Science Foundation of China.
2 THE MODEL

After the merger of two neutron stars, an SMNS with a mass \( \sim 2.5 M_\odot \), differentially rotating with a period of \( P \sim 1 \) ms, can be formed (Kluźniak & Ruderman 1998; Rosswog & Davis 2002). The maximum stable mass of a slowly rotating neutron star is \( 1.8 \sim 2.3 M_\odot \) (Akmal et al. 1998), and the uniform rotation could increase these values by at most \( \sim 20\% \) (Cook et al. 1992, 1994, and references therein). The SMNS therefore could survive before it has lost a significant part of the angular momentum, if the state equation of the nuclear material is stiff enough (cf. Shibata et al. 2006).

Though the initial surface magnetic field of the nascent SMNS, \( B_s \), may be only of the order of \( 10^{12} \) G or lower\(^1\), a much higher surface dipole magnetic field \( B_{\text{dip}} \) may be generated by several dynamo actions in a very short time: (i) Currently, the Rossby number \( R_\alpha \leq 1 \) (Rosswog, Ramirez-ruiz & Davis 2003), both the \( \alpha^2 \) and the \( \alpha - \Omega \) dynamos could amplify the initial field effectively and \( B_{\text{dip}} \sim 10^{15} \) G is expected (Duncan & Thompson 1992; Thompson & Duncan 1993). (ii) The convective dynamo can also generate a very strong dipole filed (Duncan & Thompson 1992). (iii) If soon after the sudden formation of the SMNS, the convective and hydrodynamical instabilities are greatly diminished, then the magnetic field could be amplified by the linear amplification process (Kluźniak & Ruderman 1998) and that \( B_{\text{dip}} \sim 10^{15} \) G or stronger is still expected within a timescale \( \sim 10^4 R_s^{-1} P_0 \) second (Spruit 1999). Here and throughout this letter, the convention \( Q_x = Q/10^x \) (in cgs units) is adopted.

When the surface magnetic field strength reaches \( \geq 10^{15} \) G, the differential rotation will be terminated in a very short time by magnetic braking (e.g., Shapiro 2000; Shibata et al. 2006)

\[
\tau \sim 10^2 \frac{B_{\text{dip}}}{10^{15}\text{G}}^{-1} \left( \frac{R_s}{15 \text{ km}} \right)^{-1/2} \left( \frac{M_s}{2.5 M_\odot} \right)^{1/2} \text{ms},
\]

where \( R_s \) and \( M_s \) are the radius and mass of the differentially rotating SMNS, respectively. That means the differentially rotating SMNS is estimated to evolve to a uniform rotation profile on a timescale much shorter than the spindown time of a uniformly rotating star (Eq. (3), derived below). So an SMNS is mainly supported by the rapid uniform rotation rather than by the differential rotation.

The millisecond magnetar will lose their angular momentum quickly through the dipole radiation, and strong Poynting flux dominated outflow is ejected. As a significant part of its angular momentum has been lost, the SMNS is very likely to collapse to a black hole. Before that time, the magnetic dissipation of the Poynting flux dominated outflow may be able to power detectable X-ray flares, which is of interest to us. The dipole radiation luminosity is (e.g., Usov 1994)

\[
L \sim 3 \times 10^{50} \text{ erg s}^{-1} B_{\text{dip},15}^2 P_{s,6}^6 \Omega_4^4,
\]

where \( \Omega \) is the angular velocity. The corresponding spin-down timescale is

\[
t_{\text{sd}} \sim 4 \times 10^2 \frac{M_s}{2.5 M_\odot} \left( \frac{R_s}{15 \text{ km}} \right)^{-6} \Omega_4^{-4} B_{\text{dip},15}^{-2} \text{ ms},
\]

where \( j_s \) is the specific angular momentum. In this letter we focus on the case of the SMNS spinning down exclusively via a magnetospheric wind, but it is also possible that significant spindown can also occur through gravitational wave emission, such as those driven by \( r \)-mode instabilities (Andersson 1998). A rough estimation of this timescale is within a year (Vietri & Stella 1998), much longer than the timescale through magnetic dipole radiation. On the other hand, many aspects of the present theoretical calculations regarding gravitational waves are uncertain (Fryer & Woosley 2001). So in this letter we just take into account the electromagnetic spindown.

In the Poynting-flux dominated outflow, the X-ray flare emission could be due to dissipation of the magnetic field (Usov 1994; Thompson 1994) or internal shocks with magnetization (Fan et al. 2004). For

\(^1\) After the submission of this work, several relevant papers appeared. Dai et al. (2006) proposed a post-merger millisecond differential rotating neutron star model to account for the X-ray flares following short GRBs. Price & Rosswog (2006) found that a magnetar might be formed in their MHD simulation of the double neutron star coalescence. Fan & Xu (2006) suggested that the long-term X-ray flat segment detected in the short GRB 051221A could be well accounted for, provided that the central engine was a magnetar. These last two findings are consistent with our model.
paring with the pair density (illustration, here we take the global MHD condition breakdown model to calculate the emission. By comparing with the pair density (proportional to the distance from the central source) and the density required for co-rotation (proportional to the distance), one can estimate the radius at which the MHD condition breaks down (Usov 1994; Zhang & Mészáros 2002):

\[ r_{\text{MHD}} \sim 2 \times 10^{16} \left( \frac{v_{\text{in}}}{50} \right)^{1/2} \sigma^{-1} t^{-1}_{v,m} \Gamma^{-1/2} \text{cm,} \]

where \( \sigma \) is the ratio of the magnetic energy flux to the particle energy flux, \( \Gamma \) is the bulk Lorentz factor of the outflow, \( t_{v,m} \) is the minimum variability timescale of the central engine. Beyond this radius, intense electromagnetic waves are generated and outflowing particles are accelerated (e.g. Usov 1994). Such a significant magnetic dissipation process converts electromagnetic energy into radiation. The radiation should be delayed on a timescale (relative to the initial hard \( \gamma \)-ray spike)

\[ \tau_{\text{delay}} \sim \frac{r_{\text{MHD}}}{2 \Gamma^2 c} = 33 s \left( \frac{v_{\text{in}}}{50} \right)^{1/2} \sigma^{-1} t^{-1}_{v,m} \Gamma^{-3/2} \text{cm,} \]

which matches the observation of GRB 050709 and GRB 050724.

The corresponding synchrotron radiation frequency at \( r_{\text{MHD}} \) can be estimated as (Fan et al. 2005)

\[ \nu_{\text{m,MHD}} \sim 6 \times 10^{16} \sigma^{-2} C_{p}^{2} \Gamma^{2} t^{-1}_{v,m} (1 + z)^{-1} \text{Hz,} \]

where \( C_{p} \equiv \left( \frac{\epsilon_{e}}{5.5} \right) \frac{13}{3} \left( \frac{p}{1} \right) \), \( \epsilon_{e} \) is the fraction of the dissipated comoving magnetic field energy converted to the comoving kinetic energy of the electrons, and the accelerated electrons are distributed in a single power-law \( \frac{dn}{d\gamma_e} \sim \gamma_{e}^{-p} \). So most energy is radiated in the soft X-ray band.

For the magnetic-dominated \( e^{+}e^{-} \) plasma, the diamagnetic relativistic pulse accelerator (DRPA) mechanism can convert most of the initial magnetic energy into the ultrarelativistic energy of a fraction of the surface particles. In the numerical simulation of such a plasma, Liang & Nishimura (2004) discovered that the plasma pulse bifurcated repeatedly, leading to a complex multiprobe structure at later times. So the flares from the magnetic dissipation can show repeated, multiple structures. Alternatively, the multiple flares may suggest that the magnetic dissipation takes place just locally rather than globally. The emission from different dissipation region arrives at different time and so gives rise to multiple flares (Giannios 2006).

Our model is based on the double neutron star merger model for short gamma-ray bursts (e.g. Eichler et al. 1989), which seems to be supported by the current host galaxy and afterglow observations (Barthelmy et al. 2005; Fox et al. 2005; Gehrels et al. 2005). The double neutron star merger model is also consistent with the rate and the luminosity function of short GRBs detected by HETE-2/Swift (Piran & Guetta 2006, and the references therein). The neutron star-black hole merger model is an important alternative. In the black hole and neutron star merger scenario, however, it is very hard to produce the X-ray flares. Therefore, if X-ray flares following a short GRB have been detected and the short GRB is found to be outside of the galaxy, the double neutron star merger model is strongly supported (note that just double neutron star and black hole-neutron star merger can occur outside of the host galaxy, see Fryer et al. (1999) for details). The X-ray flares then could play an additional role. When the double neutron star merger occurring outside of their host galaxy, the X-ray afterglow emission seems to be very weak and may be undetectable for the XRT in a long time, as in the case of GRB 050709 (Gehrels et al. 2005). However, the energetic X-ray flares provide us the chance of obtaining a much better location.

3 DISCUSSION

*Swift* XRT has revealed a new, rich and unexpected phenomenology of early X-ray afterglow observations. The most important one can be the energetic flares observed hundreds to thousands of seconds after the initial burst signal in both long and short GRBs (e.g. Burrows et al. 2005; Barthelmy et al. 2005). All these X-ray flares can be well interpreted by the “inner energy dissipation model”, for example, the late internal shock model (Fan & Wei 2005; Zhang et al. 2006) and/or the late magnetic energy dissipation model (Fan et al. 2005). In this model, a long-lived activity of the central engine is needed, however, and a proper model for a long activity in short GRBs is still unavailable.

In this letter we suggest a magnetized central engine model for the X-ray flares in short GRBs. We take the popular model of coalescence of two neutron stars (e.g., Eichler et al. 1989) but to assume that after
the merger a differentially rotating neutron star rather than a black hole is formed. Soon after its sudden formation, the initial magnetic field is amplified significantly by several possible dynamos (e.g., Duncan & Thompson 1992; Thompson & Duncan 1993; Kluźniak & Ruderman 1998; Spruit 1999), and the dipole magnetic field could be as strong as \(10^{15}\) G. The differential rotation of the SMNS is terminated by the magnetic braking. The early X-ray flares are powered by the dipole radiation of the nascent neutron star. They turn off when the supermassive neutron star collapses to a black hole. If this scenario is correct, then X-ray flares much more energetic than that detected in GRB 050724 may be detectable in the coming months and years by Swift. The other speculation is that some short GRBs with X-ray flares would occur outside of the host galaxies.

The outflow powering the X-ray flares are Poynting-flux dominated, so the emission should be linearly polarized, as suggested by Fan et al. (2005). In this model, no strong MeV-GeV photons accompanying the X-ray flare (due to the synchrotron self inverse Compton effect) are expected, in contrast to the baryon-rich internal shock model (see Wei et al. 2006 for a primary suggestion).

Acknowledgements Y. Z. Fan is supported by US-Israel BSF, the National Natural Science Foundation of China (Grants 10225314 and 10233010), and the National 973 Project on Fundamental Researches of China (NKBRSF G19990754).

References

Akmal A., Pandharipande V. R., Ravenhall D. G., 1998, PRC, 58, 1804
Burrows D. N., et al., 2005, Science, 309, 1833
Piran T., Guetta D., 2006, AIPC, 836, 58
Price D., Rosswog S., 2006, Science, 312, 719