



# The “Bi-drifting” Subpulses of PSR J0815+0939 Observed with the Five-hundred-meter Aperture Spherical Radio Telescope

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## Abstract

We report the “Bi-drifting” subpulses observed in PSR J0815+0939 using the Five-hundred-meter Aperture Spherical radio Telescope (FAST). The observation at band from 1050 to 1450 MHz is evenly divided into two bands, i.e., the bands at center frequencies of 1150 and 1350 MHz. The mean pulse profiles and the “Bi-drifting” subpulses at these two bands are investigated. It is found that the pulse profiles at these two frequencies show four emission components, and the peak separations between four emission components decrease with the increase of frequency. In addition, the ratio of peak intensity of each component to the intensity of component IV at 1150 MHz is larger than that at 1350 MHz. We carry out an analysis of the longitude-resolved fluctuation spectrum and two-dimensional fluctuation spectrum for each emission component, and find that the  $P_3$  of components I, II and III is about 10.56, 10.57 and 10.59 s at 1150 and 1350 MHz. However, the reliable measurements of  $P_3$  of component IV and  $P_2$  for these four components were not obtained due to the low signal-to-noise ratio of observation data. The pulse energy distributions at frequencies 1150 and 1350 MHz are presented, and it is found that no nulling phenomenon has been found in this pulsar. With our observation from the FAST, the “Bi-drifting” subpulse phenomenon of PSR J0815+0939 is expanded from 400 to 1350 MHz, which is helpful for the relevant researchers to test and constrain the pulsar emission model, especially the model of “Bi-drifting” subpulse.

*Key words:* (stars:) pulsars: general – (stars:) pulsars: individual (PSR J0815+0939) – radiation mechanisms: non-thermal

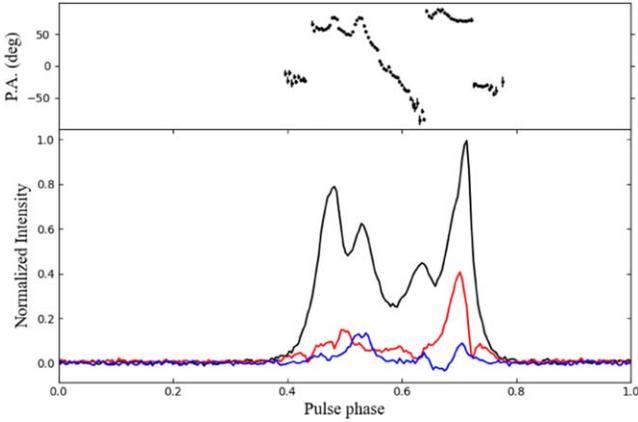
## 1. Introduction

The pulsar is known for its highly periodic pulse emission. Generally, the single pulses consist of one or more subpulses. Usually, the phase of the subpulse in a periodic radiation window often changes randomly. However, for some pulsars, the phase of subpulse changes regularly, the so-called drifting subpulse. The drifting subpulse phenomenon was first observed by Drake & Craft (1968). Up to now, more than 100 pulsars have been observed to show this phenomenon (Weltevredé et al. 2006, 2007; Basu et al. 2016). The patterns of subpulse drifting are very diverse, and can be roughly classified as four groups according to their phase behaviors, i.e., coherent phase-modulated drifting, switching phase-modulated drifting, diffuse phase-modulated drifting and low-mixed phase-modulated drifting (Basu et al. 2019). Sometimes, the phenomena of mode changing and nulling often appear with the appearance of subpulse drifting (Hankins & Wolszczan 1987; Redman et al. 2005; Basu & Mitra 2018b).

The subpulse drifting has been a hot research topic with the phenomenon that was observed in more and more pulsars. The drifting subpulse phenomenon has been widely regarded as a powerful tool to probe the inner magnetospheric structure and radiation mechanism of the pulsar (Ruderman &

Sutherland 1975; Gil et al. 2003, 2006; Qiao et al. 2004). One of the models to explain the generation of subpulse drifting phenomenon is the inner gap spark model (or carousel model) (Ruderman & Sutherland 1975). This model assumes that in the inner gap acceleration region, there are sparks of localized discharges circulate around the magnetic axis. The subpulses were came from these localized discharge sparks, when the line of sight sweeps through these localized discharge sparks, they will be found. The drifting subpulse phenomenon is caused by the rotation of the spark region around the magnetic axis. Although this model has achieved success in the generation mechanism of drifting subpulse, it is facing more and more observation challenges from the complex phenomenon of subpule drifting, such as the changing drifting rate and direction, complex drifting patterns as well as switching drifting states of subpulse (Rankin et al. 2013; Rankin & Rosen 2014; Lu et al. 2019a; Zhang et al. 2019; Wang et al. 2021). Therefore, some alternative models have been developed to explain various special subpulse drifting phenomena (van Horn 1980; Gil & Sendyk 2000; Qiao et al. 2004; Gogoberidze et al. 2005; Szary & van Leeuwen 2017).

The “bi-drifting” pulsar, PSR J0815+0939, was discovered in the Arecibo drift-scan searches (Champion et al. 2005). The



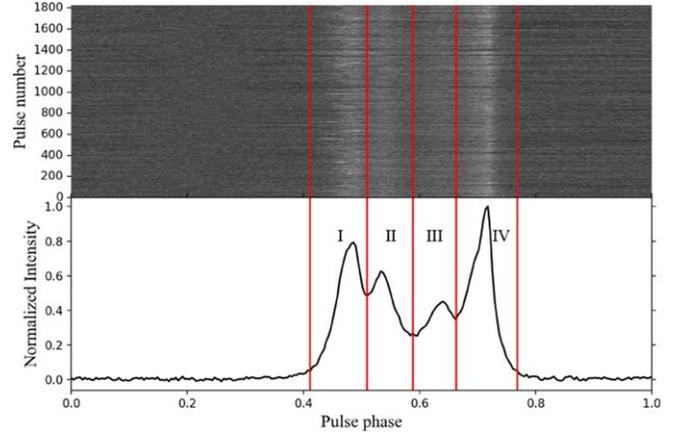
**Figure 1.** Polarization profile for PSR J0815+0939. In the bottom panel, the black, red and blue lines are the total intensity, linear polarized intensity and circular polarized intensity, respectively. The upper panel shows the position angles and corresponding uncertainties of the linear polarized emission.

main feature of “bi-drifting” phenomenon is that the drift direction is different in different subpulse component. Its integrated pulse profile contains of four pulse components, the subpulse drifting direction of the two leading components is opposite to that of the two trailing components. For most subpulse-drifting pulsars, the subpulse-drifting direction for each subpulse is the same. But, to date, there are only three interesting pulsars, including PSR J0815+0939, have been found to exhibit clear “bi-drifting” phenomenon, the other two pulsars are PSRs J1034–3224 and J1842–0359 (Basu et al. 2019; Szary et al. 2020). The “bi-drifting” phenomenon of these pulsars challenges the traditional carousel model. It can be understood by some modified models (Szary & van Leeuwen 2017; Wright & Weltevrede 2017).

In this paper, we report the “bi-drifting” subpulse phenomenon of PSR J0815+0939 observed with the Five-hundred-meter Aperture Spherical radio Telescope (FAST) of China. The paper is organized as follows. In Section 2, we introduce the  $L$ -band observation of PSR J0815+0939 with the FAST. In Section 3, the properties of subpulse drifting and mean pulse profiles of this pulsar are presented. In Section 4, we present the discussions and conclusions of this paper.

## 2. Observations

The FAST is a national major scientific project built by the Chinese Academy of Science (CAS) operated by the National Astronomical Observatories, CAS. It is located in Guizhou province, China (Nan 2006; Jiang et al. 2019, 2020; Qian et al. 2020). The longitude and latitude of the FAST are  $106.9^\circ\text{E}$   $25.7^\circ\text{N}$ , respectively. The aperture of the telescope is 500 m and the effective aperture is 300 m. One of the scientific goals of the FAST is to discover more than one thousand pulsars, establish a pulsar timing array, and study the emission physics



**Figure 2.** The pulse stack of 1825 pulses of PSR J0815+0939 at center frequency 1250 MHz with a bandwidth of 400 MHz is shown in the upper panel. Average pulse profile is shown in the bottom panel and divided into four components labeled as I, II, III and IV by the five vertical lines.

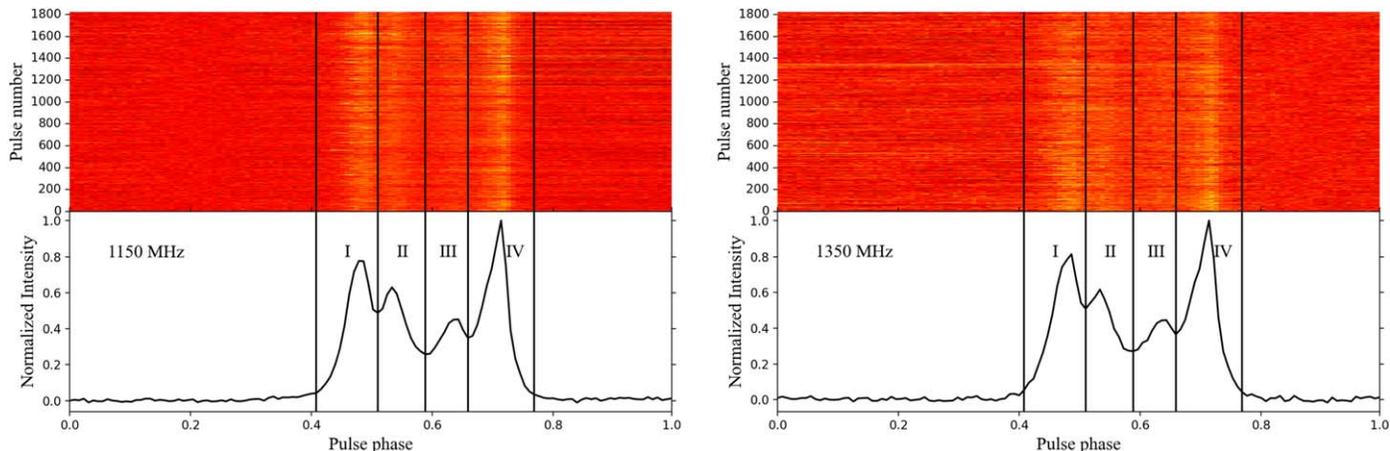
of pulsars (Li et al. 2019; Lu et al. 2019a, 2019b, 2020; Wang et al. 2019). We used the 19-beam receiver of FAST to observe the PSR J0815+0939 on 2020 October 8. The 19-beam receiver covers a frequency range of 1050–1450 MHz with a system temperature below 20 K (Jiang et al. 2019). During the observations, the signal from the central beam was Nyquist sampled at 8 bit resolution and then a Roach2 board was used to divide the overall band into 4096 channels. In observation, the search model with four polarizations,  $49.152\ \mu\text{s}$  time resolution was used. The data files were recorded in PSRFITS format. We fold the individual pulse from the FITS files using the DSPSR software package (van Straten & Bailes 2011) with the ephemeris provided by PSRCAT.<sup>4</sup> The radio-frequency interference are manually removed using “pazi” of PSRCHIVE software package (Hotan et al. 2004). Polarization calibration was achieved by correcting for the differential gain and phase between the receptors through separate measurements using a noise diode signal. Flux across the band is averaged. Finally, the PSRSALSA package was used to carry out fluctuation analysis (Weltevrede 2016).

## 3. Data Analysis

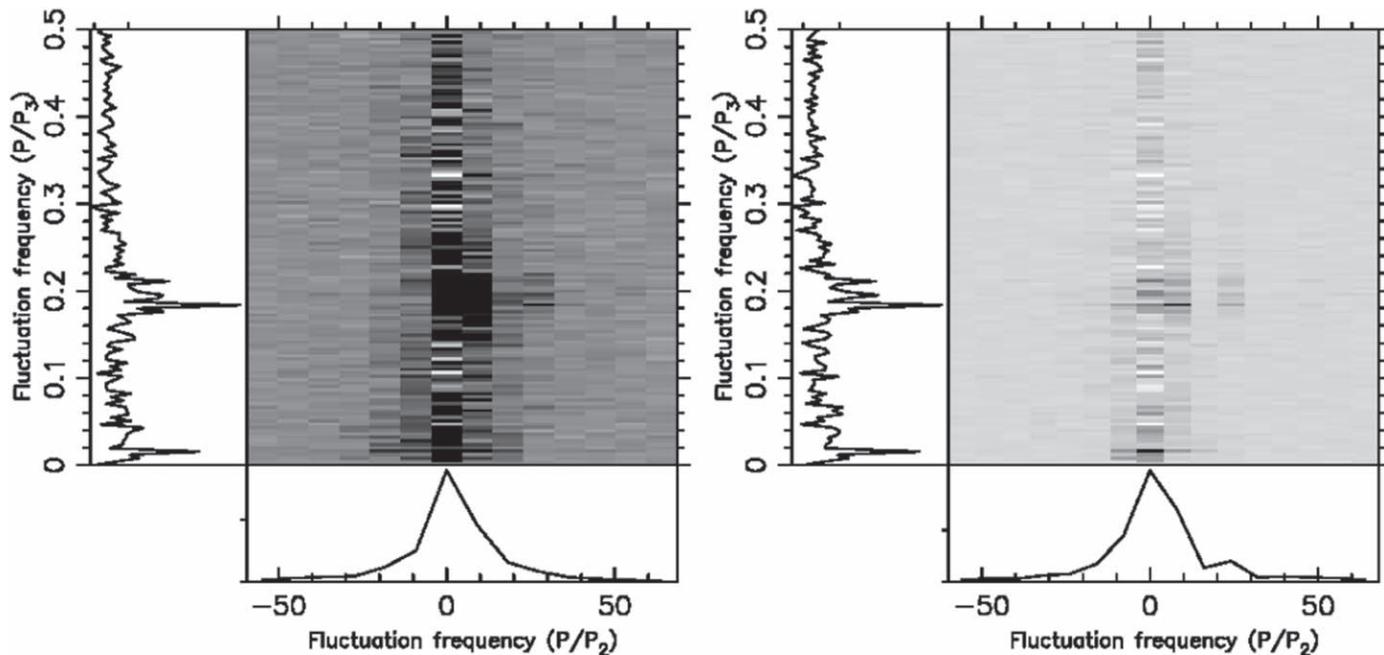
### 3.1. The Mean Pulse Profiles

The period  $P$  and period derivative  $\dot{P}$  of PSR J0815+0939 are  $\sim 645.16\ \text{ms}$  and  $0.139 \times 10^{-15}\ \text{ss}^{-1}$ , respectively. It is located at the position of RAJ (08:15:08.776) DECJ (+09:39:50.7) in the Sky. The DM is  $52.66\ \text{cm}^{-3}\ \text{pc}$ , and the flux density  $S_{400} = 3.7\ \text{mJy}$  at center frequency of 400 MHz is very small. The characteristic age  $\tau$  derived from the  $P$  and  $\dot{P}$  is  $7.35 \times 10^7\ \text{yr}$ . The rotation energy loss and surface magnetic

<sup>4</sup> <https://www.atnf.csiro.au/research/pulsar/psrcat/>



**Figure 3.** The pulse stack of 1825 pulses of PSR J0815+0939 at center frequencies of 1150 MHz and 1350 MHz with bandwidth of 200 MHz are shown in the upper-left and -right panels, respectively. The corresponding average pulse profiles are shown in the bottom-left and -right panels, respectively. Each pulse profile is divided into four components labeled as I, II, III and IV by the five vertical lines.



**Figure 4.** The left and right panels are the 2DFS for components I and II at frequency 1150 MHz, respectively. Each panel has two side panels, the horizontally (left) and vertically (bottom) integrated power show the fluctuation frequencies of  $P/P_3$  and  $P/P_2$ , respectively. Here,  $P$  is three times of period of J0815+0939.

field derived from the  $P$  and  $\dot{P}$  are  $2.0 \times 10^{31} \text{ erg s}^{-1}$  and  $3.3 \times 10^{11} \text{ G}$ , respectively. The relatively small rotation energy loss rate and old age place it close to the graveyard region in the  $P-\dot{P}$  diagram (Champion et al. 2005).

The polarization profile of PSR J0815+0939 is shown in Figure 1. The overall pulse width is  $\sim 0.44$  spin period,

containing of four components. Previous observations show that the separations of the four components are 41, 58 and 54 ms at 400 MHz band (Rankin 1983). The separations was measured by using four single Gaussian components to fit the pulse profiles at center frequency 1250 MHz with a bandwidth of 400 MHz (the component fitting method, see citations (Lu et al. 2016;

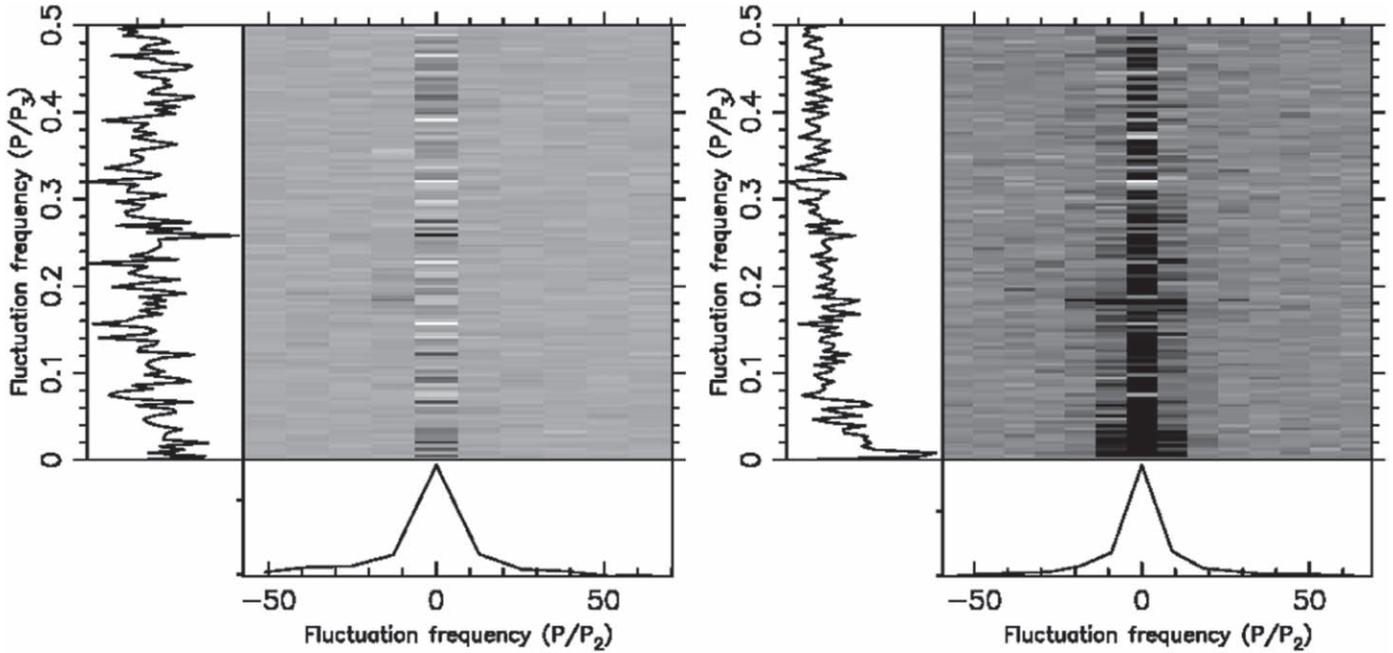


Figure 5. The left and right panels are the 2DFS for components III and IV at frequency 1150 MHz, respectively. See Figure 4 for further details.

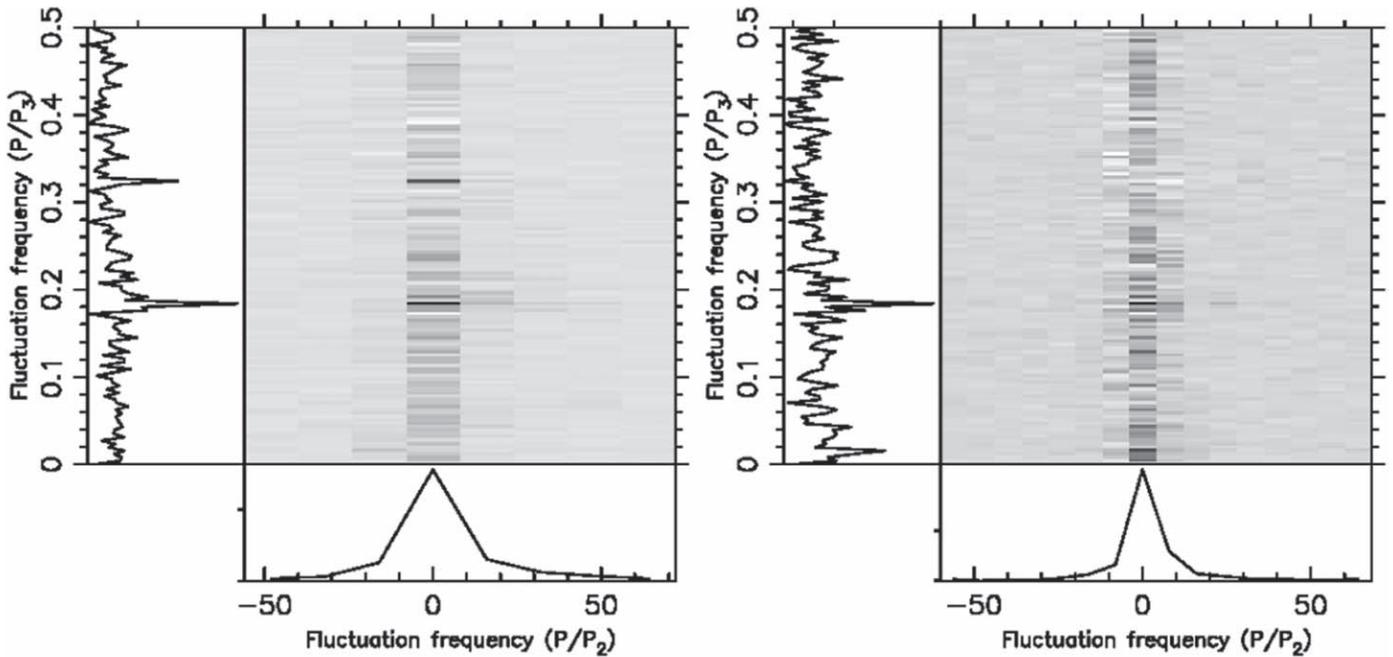


Figure 6. As Figure 4, but for frequency 1350 MHz.

Shang et al. 2017, 2021) for details), and find that the separations of the four components are  $38.29 \pm 0.66$  ms,  $69.88 \pm 1.60$  ms and  $41.16 \pm 1.15$  ms at the 1250 MHz band, respectively. This is different from that in previous observation of 400 MHz.

### 3.2. The Drift Characteristics of Subpulse

The drifting is generally characterized by the drift rate and two drift periods ( $P_2$  and  $P_3$ ) (Backer 1973). The drift rate is defined as the drifted longitude of pulse phase of each subpulse

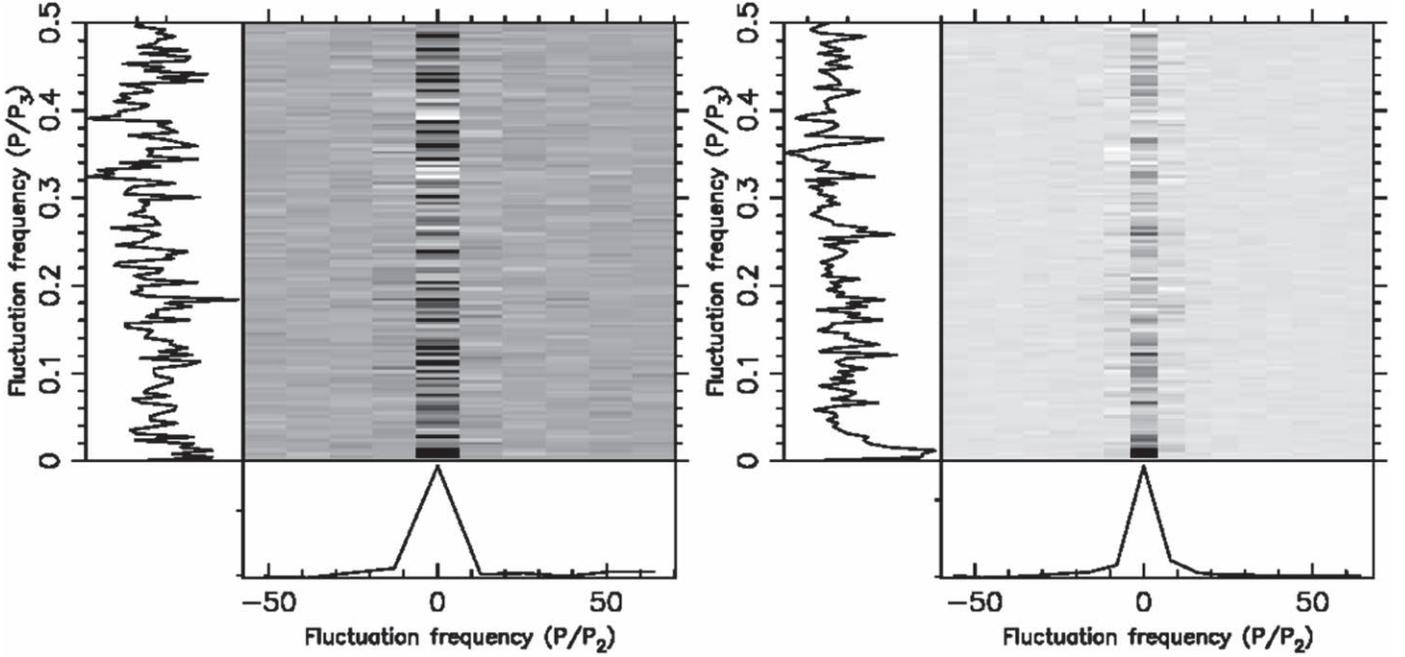


Figure 7. As Figure 5, but for frequency 1350 MHz.

**Table 1**

Parameters Obtained from LRFS and 2DFS Analyses of the Single-pulse Observations of PSR J0815+0939 with the FAST

Frequency (MHz)	Component	Drift Rate (deg. s <sup>-1</sup> )	$P_3$ (s)	Notes
327	I	...	8.72(16)	Champion et al. (2005)
	II	-2.3(5)	8.72(16)	
	III	3.2(8)	8.72(16)	
	IV	2.68(18)	8.72(16)	
430	I	...	10.87(16)	Champion et al. (2005)
	II	-1.60(13)	10.87(16)	
	III	2.46(19)	10.87(16)	
	IV	1.57(16)	10.87(16)	
1150	I	...	10.54(19)	this paper
	II	...	10.57(16)	
	III	...	10.59(23)	
	IV	...	...	
1350	I	...	10.56(19)	this paper
	II	...	10.57(18)	
	III	...	10.6(4)	
	IV	...	...	

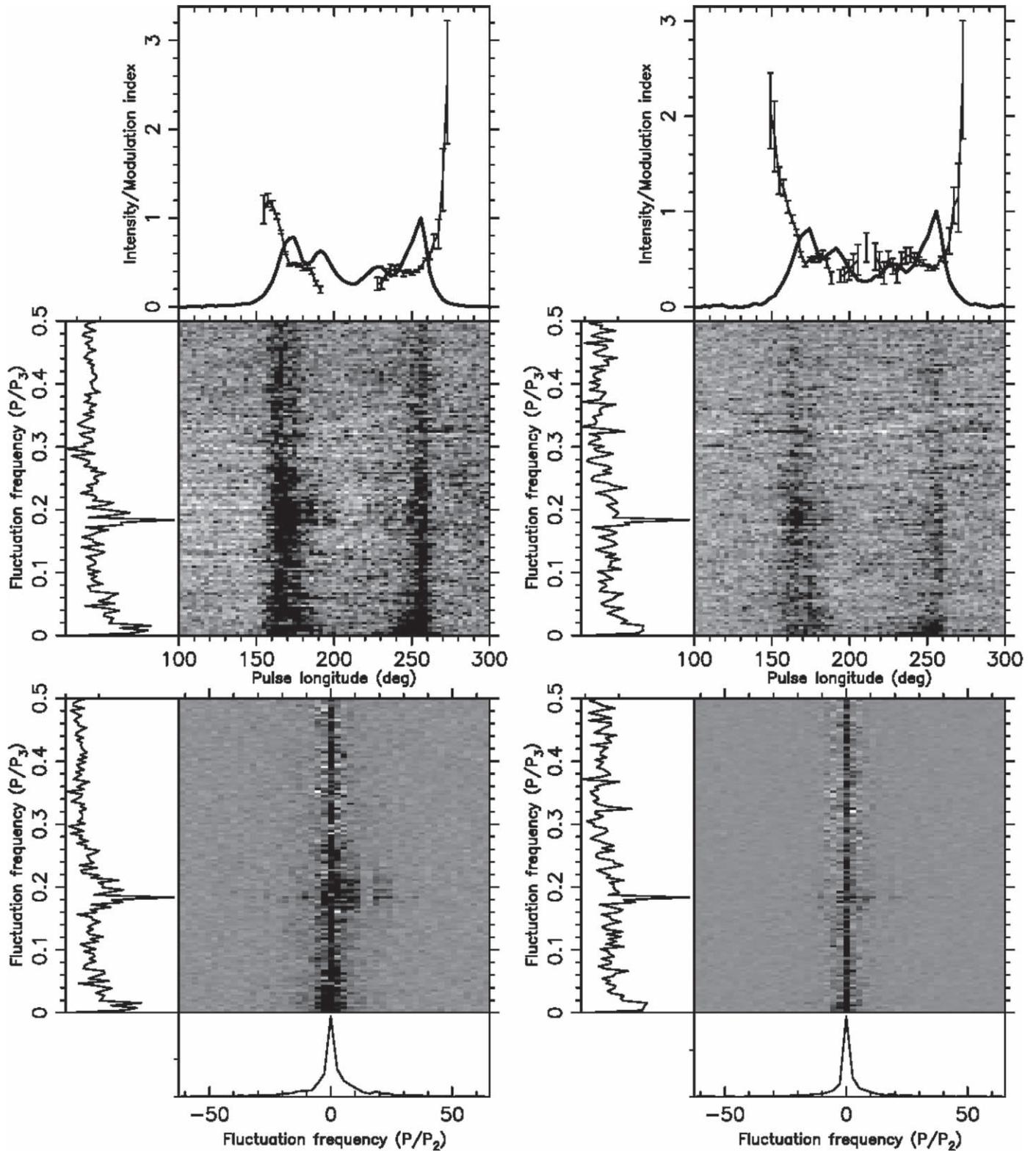
**Note.** The column “Notes” represents where the parameters are obtained.

per second.  $P_2$  denotes the phase drifting of subpulse in longitude within a phase period.  $P_3$  denotes the separation of subpulse reappearance at a given longitude. Champion et al. (2005) measured the drift period  $P_3$  of PSR J0815+0939 with the observations of Arecibo, it was found that the  $P_3$  of the four

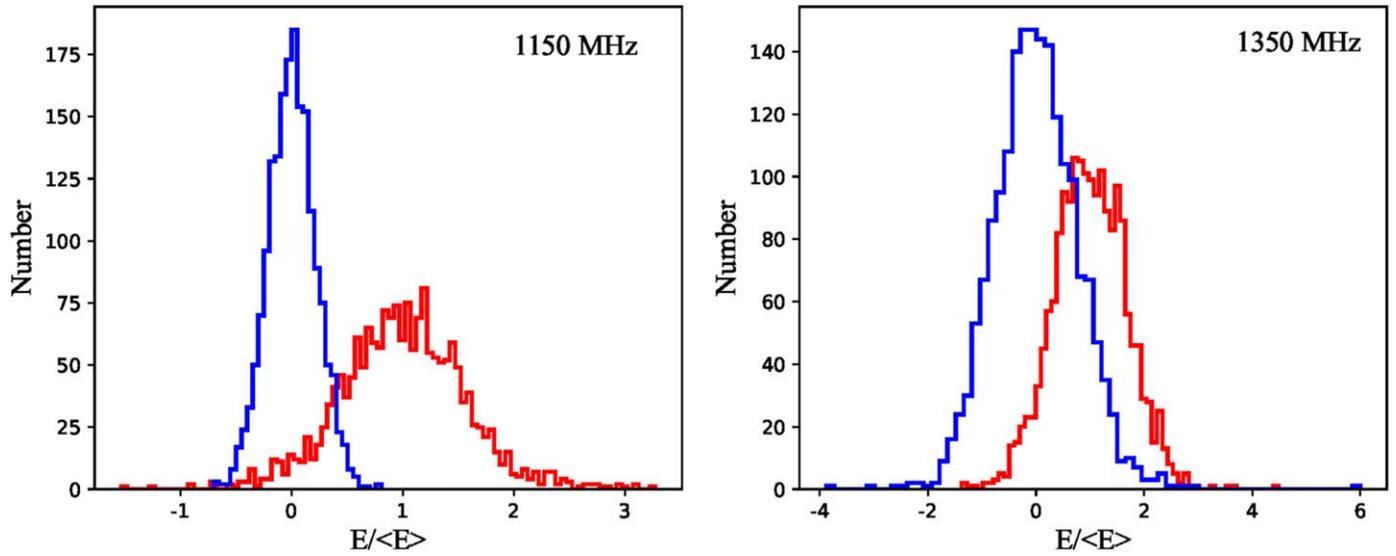
components is  $\sim 8.72$  and  $\sim 10.87$  s at 327 and 430 MHz, respectively. In addition, the drift rates of the four components are different. The drift rates of component II are different from components III and IV at 327 and 430 MHz bands, and they seem to decrease with the increase of frequency.

To investigate the pulse modulation behavior, we used the PSRSALSA package to carry out an analysis of the longitude-resolved fluctuation spectrum (LRFS, Backer 1970 and two-dimensional fluctuation spectrum (2DFS, Edwards & Stappers 2002) for each of pulse components. The single pulses at center frequency 1250 MHz with a bandwidth of 400 MHz from the observations of FAST 19 beam receiver of PSR J0815+0939 are shown in Figure 2. The detected periodic modulation of subpulse is shown in Figures 4–8 for the data at center frequencies 1150 and 1350 MHz. As the upper panel shown in Figure 2, although the FAST is the most sensitive radio telescope in the world, the drifting phenomenon of PSR J0815+0939 cannot be clearly seen by human eyes due to the weak emission flux of this pulsar at  $L$ -band.

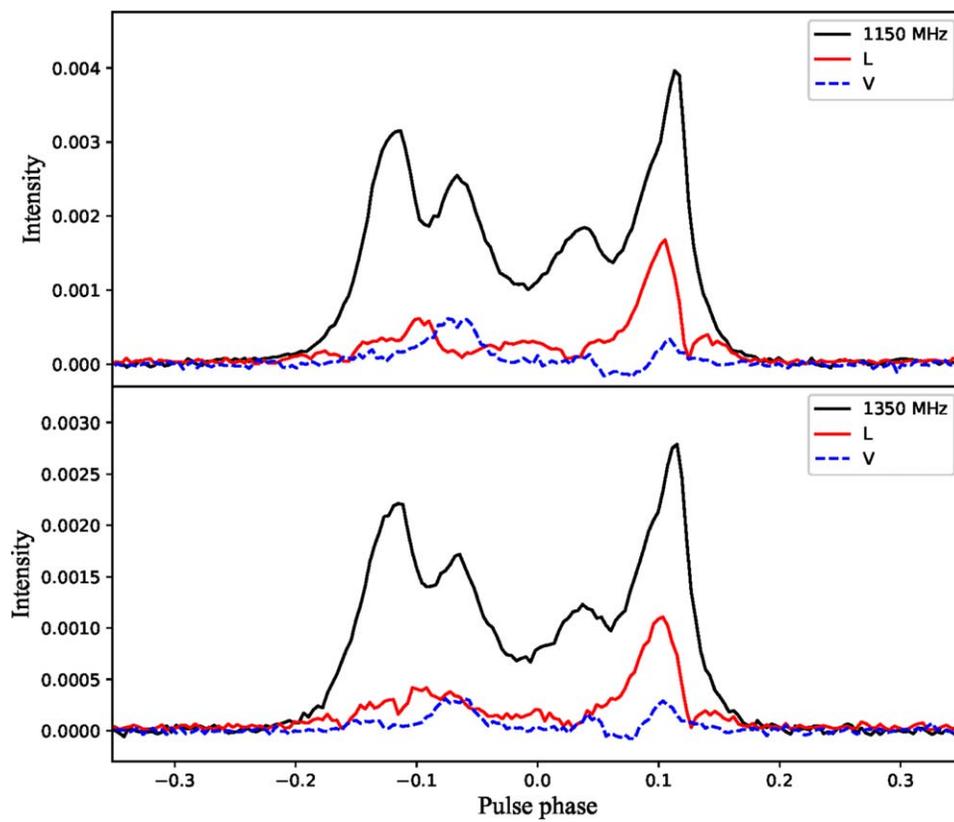
To measure the subpulse drifting of PSR J0815+0939, a phase period is binned into 128 bins and every three consecutive single pulses (the duration of each single pulse is a spin period of PSR J0815+0939) are integrated into a single pulse to make the subpulse reach a higher signal-to-noise rate. Previous measurements at 327 and 430 MHz indicated an evolution of the drift rate with frequency, i.e., the drift rate decreases with the increase of frequency Champion et al. (2005). To confirm this conclusion, we carry out a splitting-



**Figure 8.** Fluctuation analysis for PSR J0815+0939. The mean pulse profile (solid line) and longitude-resolved modulation index (points with error bars) are shown in the top panel. The LRFS with a side panel showing the horizontally integrated power is given below this panel. The 2DFS with side panels showing horizontally (left) and vertically (bottom) integrated power is plotted below the LRFS. The left and right columns are the results at frequencies 1150 and 1350 MHz, respectively.



**Figure 9.** The pulse energy distribution of PSR J0815+0939 at 1150 MHz (the left panel) and 1350 MHz (the right panel). The blue step lines are the distribution of energy at the off-pulse region. The red step lines are the distribution at the on-pulse region.



**Figure 10.** The mean pulse profiles at frequencies 1150 MHz (upper panel) and 1350 MHz (bottom panel). The black and red solid lines are the mean pulse profiles and linear polarizations, respectively. The blue dashed lines are the circular polarizations.

frequency analysis of LRFS and 2DFS for the four components. We split the FAST observation data with a frequency range from 1050 to 1450 MHz into two bands, i.e., 1050–1250 MHz (band1) and 1250–1450 MHz (band2). Then, the drift rate,  $P2$  and  $P3$  of the four components in the pulse profiles at band1 and band2 are measured with the PSRSALSA package, respectively. However, as the flux of PSR J0815+0939 at  $L$ -band is too weak to obtain the measurements of the drift rate and  $P2$ . Only the measurement of  $P3$  at band1 and band2 for components I, II and III are obtained, the measurements are listed in Table 1.

### 3.3. The Single Pulse and Mean Pulse Profiles

We study the frequency behaviors of radio emission of PSR J0815+0939 by dividing the  $L$ -band observation into two bands, i.e., the bands at center frequencies 1150 and 1350 MHz. Each band have a bandwidth of 200 MHz. The single pulses at these two bands are shown in Figure 3. We present the pulse energy distributions of the off-pulse and on-pulse regions for these two bands shown in Figure 9. It is found that no pulse nulling phenomenon has been discovered in this pulsar, and the energy distributions of on-pulse region at 1150 and 1350 MHz are basically similar. The mean pulse profiles at frequencies 1150 and 1350 MHz are shown in Figure 10. We find that the pulse profiles of PSR J0815+0939 not change significantly within 400 MHz at  $L$ -band. Previous observation show the pulse profile of this pulsar consisting of four components with separations of 41, 58 and 54 ms at 400 MHz band (Champion et al. 2005). We calculated these separations for the pulse profiles at 1150 MHz and 1350 MHz, and find that the separations are  $38.04 \pm 0.90$ ,  $68.93 \pm 2.3$  and  $42.18 \pm 1.60$  ms for the pulse profiles at 1150 MHz, respectively, while the separations are  $38.65 \pm 0.96$ ,  $69.35 \pm 2.22$  and  $41.56 \pm 1.59$  ms for the pulse profiles at 1350 MHz, respectively.

We investigate the change of intensity ratio of peak with frequency. Comparing the pulse profiles at 327 and 430 MHz shown in Figure 6 of Champion et al. (2005), we find that the change of intensity ratio of peak with frequency is irregular. As shown in Figure 6 of Champion et al. (2005), the largest peak is the component IV for the pulse profile at 430 MHz, while the largest peak is component III for the pulse profile at 327 MHz. This seems to show that the ratio of peak intensity of each component to the peak intensity of component IV increases with the increase of frequency. However, we calculate peak intensity ratio for the pulse profiles at 1150 MHz and 1350 MHz, and find that the ratios of the peak intensities of components I, II and III to the peak intensity of component IV are about 0.80, 0.64 and 0.47 for the pulse profile at 1150 MHz, respectively. While the ratios are about 0.79, 0.62 and 0.44 for the pulse profile at 1350 MHz, respectively, i.e., the ratio of peak intensity at lower frequency is larger than that at higher frequency.

## 4. Discussions and Conclusions

We report here “Bi-drifting” subpulses observed in PSR J0815+0939 using the FAST radio telescope. To investigate the pulse modulation behavior at different frequency. The 1250 MHz observation with a 400 MHz bandwidth from FAST are divided into two-band data, i.e., bands at center frequencies 1150 and 1350 MHz with a bandwidth of 200 MHz. Then, an analysis of the longitude-resolved fluctuation spectrum and two-dimensional fluctuation spectrum of each sub-pulse components for these two bands are carried out. It is found that the  $P3$  of the four components is 10.5–10.6 s at 1150 and 1350 MHz. This is close to the measurements at 430 MHz given by Champion et al. (2005). The peak separations between the four components are presented, we find that the peak separation decreases with the increase of frequency, which is consistent with the frequency evolution behavior of the pulse profile of most pulsars, i.e., the pulse width decreases with the increase of frequency. We measured the ratio of peak intensity of each component to the peak intensity of component IV for the pulse profiles at 1150 and 1350 MHz, and found the ratio at lower frequency is larger than that at higher frequency. Our analysis of pulse energy distribution for the two bands shows that no nulling phenomenon was found in this pulsar.

The first observation for this pulsar was from the Arecibo telescope at 327 and 430 MHz, and this was the first time to show the “Bi-drifting” subpulse phenomenon (Champion et al. 2005). Although FAST is the largest and most sensitive radio telescope in the world, it is also very difficult to obtain a clear image of “Bi-drifting” subpulse with the observation of FAST. Therefore, with the FAST observation, we expand the emission modulation phenomenon of PSR J0815+0939 from 400 to 1350 MHz. However, as the observed signal is so weak that only  $P3$  of components I, II and III are presented. By combining the observed results given in the previous works with the results of this paper, it is helpful for the relevant researchers to test and constrain the pulsar emission model and give a more perfect model.

## Acknowledgments

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4008, [2017]5726-37 and [2018]5769-02), the Foundation of Guizhou Provincial Education Department (No. KY(2020)003).

## References

- Backer, D. C. 1970, *Natur*, **227**, 692  
 Backer, D. C. 1973, *ApJ*, **182**, 245  
 Basu, R., & Mitra, D. 2018a, *MNRAS*, **475**, 5098  
 Basu, R., & Mitra, D. 2018b, *MNRAS*, **476**, 1345  
 Basu, R., Mitra, D., Melikidze, G. I., & Skrzypczak, A. 2019, *MNRAS*, **482**, 3757  
 Basu, R., Mitra, D., Melikidze, G. I., et al. 2016, *ApJ*, **833**, 29  
 Champion, D. J., Lorimer, D. R., McLaughlin, M. A., et al. 2005, *MNRAS*, **363**, 929  
 Drake, F. D., & Craft, H. D. 1968, *Natur*, **220**, 231  
 Edwards, R. T., & Stappers, B. W. 2002, *A&A*, **393**, 733  
 Gil, J., Melikidze, G., & Zhang, B. 2006, *ApJ*, **650**, 1048  
 Gil, J., Melikidze, G. I., & Geppert, U. 2003, *A&A*, **407**, 315  
 Gil, J. A., & Sendyk, M. 2000, *ApJ*, **541**, 351  
 Gogoberidze, G., Machabeli, G. Z., Melrose, D. B., & Luo, Q. 2005, *MNRAS*, **360**, 669  
 Hankins, T. H., & Wolszczan, A. 1987, *ApJ*, **318**, 410  
 Hotan, A. W., van Straten, W., & Manchester, R. N. 2004, *PASA*, **21**, 302  
 Jiang, P., Tang, N.-Y., Hou, L.-G., et al. 2020, *RAA*, **20**, 064  
 Jiang, P., Yue, Y., Gan, H., et al. 2019, *SCPMA*, **62**, 959502  
 Li, D., Dickey, J. M., & Liu, S. 2019, *RAA*, **19**, 016  
 Lu, J., Lee, K., & Xu, R. 2020, *SCPMA*, **63**, 229531  
 Lu, J., Peng, B., Liu, K., et al. 2019a, *SCPMA*, **62**, 959503  
 Lu, J., Peng, B., Xu, R., et al. 2019b, *SCPMA*, **62**, 959505  
 Lu, J. G., Du, Y. J., Hao, L. F., et al. 2016, *ApJ*, **816**, 76  
 Nan, R. 2006, *SCPMA*, **49**, 129  
 Qian, L., Yao, R., Sun, J., et al. 2020, *The Innovation*, **1**, 100053  
 Qiao, G. J., Lee, K. J., Zhang, B., et al. 2004, *ApJL*, **616**, L127  
 Rankin, J., & Rosen, R. 2014, *MNRAS*, **439**, 3860  
 Rankin, J. M. 1983, *ApJ*, **274**, 333  
 Rankin, J. M., Wright, G. A. E., & Brown, A. M. 2013, *MNRAS*, **433**, 445  
 Redman, S. L., Wright, G. A. E., & Rankin, J. M. 2005, *MNRAS*, **357**, 859  
 Ruderman, M. A., & Sutherland, P. G. 1975, *ApJ*, **196**, 51  
 Shang, L. H., Lu, J. G., Du, Y. J., et al. 2017, *MNRAS*, **468**, 4389  
 Shang, L. H., Xu, X., Dang, S. J., et al. 2021, *ApJ*, **916**, 62  
 Szary, A., & van Leeuwen, J. 2017, *ApJ*, **845**, 95  
 Szary, A., van Leeuwen, J., Weltevrede, P., & Maan, Y. 2020, *ApJ*, **896**, 168  
 van Horn, H. M. 1980, *ApJ*, **236**, 899  
 van Straten, W., & Bailes, M. 2011, *PASA*, **28**, 1  
 Wang, H. G., Qiao, G. J., Du, Y. J., et al. 2019, *RAA*, **19**, 021  
 Wang, S. Q., Wang, J. B., Wang, N., et al. 2021, *ApJ*, **913**, 67  
 Weltevrede, P. 2016, *A&A*, **590**, A109  
 Weltevrede, P., Edwards, R. T., & Stappers, B. W. 2006, *A&A*, **445**, 243  
 Weltevrede, P., Stappers, B. W., & Edwards, R. T. 2007, *A&A*, **469**, 607  
 Wright, G., & Weltevrede, P. 2017, *MNRAS*, **464**, 2597  
 Zhang, L., Li, D., Hobbs, G., et al. 2019, *ApJ*, **877**, 55