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Physical and geometrical parameters of CVBS XIV: the two nearby systems HIP 19206 and HIP 84425

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Abstract Data release 2 (DR2) from the Gaia mission was of great help in precise determination of fundamental parameters of Close Visual Binary and Multiple Systems (CVBMSs), especially masses of their components, which are crucial parameters in understanding formation and evolution of stars and galaxies. This article presents the complete set of fundamental parameters for two nearby close visual binary systems (CVBSs), which are HIP 19206 and HIP 84425. We utilised a combination of two methods; the first one is Tokovinin's dynamical method to solve the orbit of the system and to estimate orbital elements and the dynamical mass sum, and the second one is Al-Wardat's method for analysing CVBMSs to estimate the physical parameters of the individual components. The latest method employs grids of Kurucz lineblanketed plane parallel model atmospheres to build synthetic Spectral Energy Distributions (SEDs) of the individual components. Trigonometric parallax measurements given by Gaia DR2 and Hipparcos catalogues are used to analyse the two systems. The difference in these measurements yielded slight discrepancies in the fundamental parameters of the individual components, especially masses. So, a new dynamical parallax is suggested in this work based on the most convenient mass sum as given by each of the two methods. The new dynamical parallax for the system HIP 19205 of 22.97 ± 0.95 mas coincides well with the trigonometric one reported recently (in December 2020) by Gaia EDR3 of 22.3689 ± 0.4056 mas. The positions of the components of the two systems on the evolutionary tracks and isochrones are plotted, which suggest that all components are solar-type main sequence stars. Their most probable formation and evolution scenarios are also discussed.

Key words: binaries: close — binaries: visual- stars: fundamental parameters — stars: individual: HIP 19206 and HIP 84425

1 INTRODUCTION

The study of the physical and geometrical parameters, especially masses, of close visual binary systems (CVBSs) plays an important role in revealing the secrets of formation and evolution of such systems, and hence the formation and evolution of the Galaxy. It also represents a direct tool for investigating dynamical properties of astrophysics.

The preciseness of such studies is highly enhanced by the latest measurements of distances to such systems, which were dramatically advanced by the Gaia astrometric mission (Gaia Collaboration 2018; Al-Wardat et al. 2021).

The two systems under study fulfill the following specific requirements; The two components of the system are visually close enough that they cannot be observed and studied individually, and the system has available accurate measurements of its colours, colour indices and magnitude difference between its components.

HIP HD	19206 26040	84425 155826	Source of data
α_{2000}	$04^{\rm h}07^{\rm m}00^{\rm s}566$	$17^{\rm h}15^{\rm m}35^{\rm s}902$	$SIMBAD^1$
δ_{2000}	$-10^{\circ}00'01.''857$	$-38^{\circ}35'38.''902$	-
Sp. Typ.	G1/2V	G0V	-
A_V	0.0	0.0062	Lallement et al. (2018)
$V_{I}(\text{Hip})$	6.88	5.95	ESA (1997)
$(V-I)_J$	0.65 ± 0.00	0.64 ± 0.02	-
$(B-V)_J$	0.576 ± 0.004	0.580 ± 0.004	-
B_T	7.566 ± 0.008	6.67 ± 0.013	-
V_T	6.957 ± 0.006	6.015 ± 0.006	-
$\pi_{\rm Hip}$ (mas)	24.00 ± 0.92	32.6 ± 1.7	-
$\pi_{\rm Hip}$ (mas)	24.49 ± 0.83	32.69 ± 0.59	Van Leeuwen 2007
π_{Gaia} (mas)	23.4039 ± 0.4727	30.4039 ± 0.4728	Gaia Collaboration (2018)

 Table 1
 Observational Data for HIP 19206 and HIP 84425

¹ http://simbad.u-strasbg.fr/simbad/sim-fid.

The study relies on two complementary methods; Tokovinin's dynamical method for the orbital solutions and Al-Wardat's method for analysing binary and multiple stellar systems (BMSSs).

Al-Wardat's method is an indirect computational spectrophotmetrical method that uses the available observations (magnitudes and magnitude differences) of a binary or a multiple system to build a synthetic Spectral Energy Distribution (SED) for each individual component. It employs grids of Kurucz's line-blanketed plane parallel atmospheres to build these synthetic SEDs (Kurucz 1994). Then it combines these SEDs depending on some geometrical information like the system's parallax and the radii of the components to get the entire SED of the system, from which we can calculate the synthetic magnitudes and colour indices. This process is subject to iteration until the best fit between the synthetic and observational magnitudes and colour indices is achieved. Whereupon, input parameters, both those of the model atmospheres and the geometrical calculations, represent the fundamental parameters of the system adequately enough within the error values of the measured ones.

This method was successfully applied to several CVBMSs. Some of them are solar type stars, while the others were found to be subgiant stars.

The criterion for the judgement of Al-Wardat's method is the best fit between all the observational colours and colour indices with the synthetic ones. In case the entire observational SED exists, it is usually employed as an additional judgement tool by achieving the best fit with the synthetic one.

Among the solar type CVBSs which were studied using Al-Wardat's method, we mention here: ADS 11061, COU 1289, COU 1291, HIP 11352, HIP 11253, HIP 70973, HIP 72479, Gliese 150.2, Gliese 762.1, COU 1511, FIN 350 and HIP 109951 (see, e.g., Al-Wardat 2002, 2007, 2009, 2012; Al-Wardat et al. 2014a, 2016; Masda et al. 2016; Al-Wardat et al. 2017; Masda et al. 2019). Of course, the method can deduce if the system is evolved or not. Here are some evolved (subgiant) CVBSs which were analysed using the method: HD 25811, HD 375 and HD 6009 (see i.e. Al-Wardat et al. 2014b; Al-Wardat 2014; Al-Wardat et al. 2014a for full details and references).

This paper presents the analysis of two nearby CVBSs; these are HIP 19206 (HD 26040) and HIP 84425 (HD 155826).

2 ARCHIVED DATA

The observational photometric data are taken from various reliable sources, such as the old Hipparcos Catalogue (ESA 1997), new Hipparcos reduction (van Leeuwen 2007) and Gaia Data Release 2 (DR2) (Gaia Collaboration 2018).

These data are utilised to calculate the preliminary input parameters and as reference for the best fit with the synthetic photometry. Table 1 contains the catalogued data for HIP 19206 and HIP 84425. These data were taken from the SIMBAD database, the Hipparcos and Tycho Catalogues and Gaia DR2. For the orbital solutions, we relied on data from the Fourth Catalog of Interferometric Measurements of Binary Stars (INT4) (Hartkopf et al. 2001).

3 METHODS AND ANALYSIS

3.1 Orbital Solutions

For the orbital solution and modification of the orbital elements of the systems, we follow Tokovinin's dynamical method applying the ORBITX code of Tokovinin et al. (2016). We considered the relative position measurements: angular separations (ρ) in (") and position angles (θ) in (deg) obtained by different observational techniques and listed in INT4. The program performs a least-squares adjustment to all available relative position observations, with weights inversely proportional to the square of their standard errors.

The orbital solution involves the orbital period P (in years), the eccentricity e, the semi-major axis a (in arcsec), the inclination i (in deg), the argument of periastron ω (in



Fig. 1 The modified orbit of the HIP 19206 system as determined from our analysis (*solid line*) and last orbit from ORB6 (*dotted line*). The bottom left panel displays the fit residuals, showing the difference between the observed and model values for the angular separation $(\Delta \rho)$ and position angle $(\Delta \theta)$ of the orbit. The bottom right panel features the distribution of data based on a fivenumber summary ("minimum," first quartile (Q1), median, third quartile (Q3) and "maximum") and outliers.

deg), the position angle of nodes Ω (in deg) and the time of periastron passage T_0 (in yr).

HIP 19206: the preliminary orbital parameters of the system were calculated by Balega et al. (2006a), then modified two times by Tokovinin et al. (2015) and Tokovinin (2019).

In this work, we use 41 points of positional measurements (ρ) and (θ) covering the period from 1991 to 2019. The latest points are published by: Tokovinin et al. (2015) (one point), Mason et al. (2018) (3-points) and Tokovinin (2019) (one point). The modified orbit of the system HIP 19206 is shown in Figure 1 against the orbit given by the Sixth Catalog of Orbits of Visual Binary Stars (ORB6, http://www.astro.gsu.edu/wds/orb6.html)

HIP 84425: the preliminary orbital parameters of the system were calculated by Söderhjelm (1999) then modified two times by Rica Romero (2010) and Tokovinin et al. (2015).

In this work, we consider 16 points of the relative positional measurements (ρ) and (θ) from 1959 to 2015. The latest point was published by Tokovinin et al. (2016)



Fig. 2 The modified orbit of the HIP 84425 system as determined from our analysis (*solid line*) and last orbit from ORB6 (*dotted line*). The bottom left panel displays the fit residuals, showing the difference between the observed and model values for the angular separation $(\Delta \rho)$ and position angle $(\Delta \theta)$ of the orbit. The bottom right panel features the distribution of data based on a five-number summary ("minimum," first quartile (Q1), median, third quartile (Q3) and "maximum") and outliers.

and is used for the first time in this work. The modified orbit of the system HIP 84425 is shown in Figure 2 against the orbit given by ORB6.

We calculate the total dynamical mass applying Kepler's third law, where we utilise the semi-major axis and the period from the orbital solution and the parallax measurements from either Hipparcos (ESA 1997), Hipparcos 2007 (van Leeuwen 2007) or Gaia DR2 (Gaia Collaboration 2018).

Kepler's third law for binary stars can be expressed as follows

$$M_{\rm dyn} = M_A + M_B = (\frac{a^3}{\pi^3 P^2}) M_{\odot}$$
 (1)

and the formal error is given by

$$\frac{\sigma_M}{M} = \sqrt{9(\frac{\sigma_\pi}{\pi})^2 + 9(\frac{\sigma_a}{a})^2 + 4(\frac{\sigma_P}{P})^2}.$$
 (2)

3.2 Physical Parameters

The first step in applying the analysis using Al-Wardat's method is to determine correctly the magnitude difference between the two components. For the system HIP 19206,

			System HIP 1	9206	
Parameters	Units	(1)	(2)	(3)	This work
$P \pm \sigma_P$	(yr)	21.33 ± 0.44	21.42 ± 0.037	21.06	21.103 ± 0.00
$T_0 \pm \sigma_{T_0}$	(yr)	1996.77 ± 0.08	1996.78 ± 0.06	2017.94	1996.91 ± 0.00
$e\pm\sigma_{ m e}$	-	0.686 ± 0.011	0.687 ± 0.009	0.711	0.7019 ± 0.00
$a \pm \sigma_{\mathrm{a}}$	(arcsec)	0.223 ± 0.006	0.225 ± 0.006	0.229	0.226 ± 0.000
$i\pm\sigma_{ m i}$	(deg)	122.2 ± 1.2	122.9 ± 1	121.7	122.68 ± 0.00
$\Omega \pm \sigma_{\Omega}$	(deg)	255.6 ± 1.1	219.0 ± 1.8	220.4	219.00 ± 0.08
$\omega\pm\sigma_{\Omega}$	(deg)	38.2 ± 1.7	76.4 ± 0.5	77.3	76.40 ± 0.05
$M_{dvn} \pm \sigma_M^1$	(M_{\odot})	1.763 ± 0.258	1.796 ± 0.252	1.959	1.873 ± 0.215
$M_{dvn} \pm \sigma_M^2$	(M_{\odot})	1.659 ± 0.226	1.690 ± 0.219	1.843	1.762 ± 0.179
$M_{dyn} \pm \sigma_M^3$	(M_{\odot})	1.965 ± 0.215	2.001 ± 0.202	2.183	2.087 ± 0.128
$rms(\theta)$	(deg)	0.9	0.2335		0.10
$\operatorname{rms}(\rho)$	(arcsec)	0.002	0.9268		0.0002

Table 2 Modified orbital elements, mass sums and quality controls of the system HIP 19206 obtained in this work, along with previous ones of (1) Balega et al. (2006a), (2) Tokovinin et al. (2015) and (3) Tokovinin (2019).

¹ Using (π_{Hip1997}) ; ² Using (π_{Hip2007}) ; ³ Using (π_{Gaia2018}) .

Table 3 Modified orbital elements, mass sums and quality controls of the system HIP 84425, along with previous ones of (1) Söderhjelm (1999), (2) Rica Romero (2010) and (3) Tokovinin et al. (2015).

		System HIP 84425			
Parameter	Units	(1)	(2)	(3)	This work
$P \pm \sigma_{\rm P}$	(yr)	23.3	14.215 ± 0.050	14.23 ± 0.03	14.247 ± 0.057
$T_0 \pm \sigma_{T_0}$	(yr)	1986.5	1985.98 ± 0.17	1985.97 ± 0.06	1985.98 ± 0.15
$e \pm \sigma_{ m e}$	-	0.5	0.491 ± 0.005	0.476 ± 0.01	0.465 ± 0.008
$a \pm \sigma_{\rm a}$	(arcsec)	0.28	0.253 ± 0.004	0.249 ± 0.02	0.253 ± 0.002
$i \pm \sigma_{ m i}$	(deg)	123	115.2 ± 1.1	115.3 ± 0.6	115.05 ± 0.75
$\Omega \pm \sigma_{\Omega}$	(deg)	4	190.41 ± 0.62	191.81 ± 0.47	192.06 ± 0.37
$\omega \pm \sigma_{\omega}$	(deg)	349	135.2 ± 2.5	137.2 ± 1.0	137.24 ± 2.04
$M_{dvn} \pm \sigma_M^{-1}$	(M_{\odot})	1.17	2.305 ± 0.379	2.201 ± 0.632	2.307 ± 0.364
$M_{dyn} \pm \sigma_M^2$	(M_{\odot})	1.16	2.286 ± 0.171	2.183 ± 0.539	2.287 ± 0.133
$M_{dyn} \pm \sigma_M^3$	(M _☉)	1.45	2.841 ± 0.197	2.713 ± 0.666	2.842 ± 0.146
$rms(\theta)$	(deg)		0.2	1.26	0.06
$rms(\rho)$	(arcsec)		1.0	0.93	0.0001

¹ Using (π_{Hip1997}) ; ² Using (π_{Hip2007}) ; ³ Using (π_{Gaia2018}) .

Table 4 Magnitude difference between the components ofboth systems, HIP 19206 and HIP 84425. We list here onlythe values taken under filters close to the V-band filter.

HIP	Δm (mag)	$\sigma_{\Delta m}$	Filter $(\lambda/\Delta\lambda)$ (nm)	Reference
HIP 19206	$1.39 \\ 1.40$	0.02 *	$545/20 \\ 541/88$	Balega et al. (2007) Horch et al. (2008)
	1.43	*	550/40	_
	$1.45 \\ 1.48$	*	$\frac{550}{40}$	-
	1.4	*	551/22	Tokovinin et al. (2010)
	1.5	*	543/22	Tokovinin et al. (2016)
HIP 84425	1.6	*	551/22	Tokovinin et al. (2010)
	1.6	*	543/22	Tokovinin et al. (2015)
	1.7	*	543/22	Tokovinin et al. (2016)

we find $\Delta m = 1.4 \pm 0.02$ mag, which is the average measurements under the V-band filter (541-551) nm (see Table 4). While for HIP 84425, we find $\Delta m = 1.6 \pm 0.16$ mag to be the average value of the V-band filter (543–551 nm) measurements listed in Table 4.

Utilising the values of Δm along with the apparent visual magnitudes of the systems ($m_{v(HIP19206)} = 6.88$ mag, $m_{v(HIP84425} = 5.95$ mag) (see Table 1), we calculate the apparent visual magnitudes of individual

components by employing Equations (3) and (4). The results are $m_v^A = 7^m.14 \pm 0.01$ and $m_v^B = 8^m.54 \pm 0.02$ for HIP 19206, and $m_v^A = 6^m.17 \pm 0.03$ and $m_v^B = 7^m.77 \pm 0.16$ for HIP 84425.

$$m_v^A = m_v + 2.5 \log(1 + 10^{-0.4\Delta m}),$$
 (3)

$$m_v^B = m_v^A + \Delta m. \tag{4}$$

where we applied the following relations to calculate the error values of the apparent visual magnitudes of the individual components of the system:

$$\sigma_{m_v^A}^2 = \sigma_{m_v}^2 + (\frac{1}{1+10^{+0.4\Delta m}})^2 \sigma_{\Delta m}^2, \tag{5}$$

$$\sigma_{m_v^B}^2 = \sigma_{m_v^A}^2 + \sigma_{\Delta m}^2. \tag{6}$$

As a result, it is found that the absolute visual magnitudes for the primary and secondary components of the system HIP 19206 are $M_V^A = 3^m.96\pm0.04$ and $M_V^B = 5^m.36\pm0.05$ respectively, and those for the system HIP 84425 are $M_V^A = 3^m.58\pm0.05$ and $M_V^B = 5^m.17\pm0.03$ using the following equation (Heintz 1978)

$$M_V = m_v + 5 - 5\log(d) - A_V.$$
 (7)

Here, the interstellar extinction A_V of HIP 19206 is neglected because this system is nearby.

The errors of the absolute visual magnitudes of components A and B of the system are calculated by using the following equation

$$\sigma_{M_V^*}^2 = \sigma_{m_v^*}^2 + (\frac{\log e}{0.2\pi})^2 \sigma_{\pi}^2 ; \quad * = A, B.$$
(8)

where $\sigma_{m_v^*}$ are the errors of the apparent magnitudes of the A and B components expressed in Equations (5) and (6).

Based on the estimated preliminary absolute magnitudes (M_V) of the individual components of the two systems, we can find the preliminary values of the effective temperature and the bolometric correction for each component as taken from the tables of Gray (2005) and Lang (1992). For HIP 19206 $T_{eff}^A = 6160$ K, $T_{eff}^B = 5550$ K and $(B.C.)_A = -0.12$, $(B.C.)_B = -0.30$, and for HIP 84425 $T_{eff}^A = 6520$ K, $T_{eff}^B = 5650$ K and $(B.C.)_A = -0.12$, $(B.C.)_B = -0.21$, for the primary and secondary components of the two systems, respectively.

Furthermore, we rely on Equtions (9), (10), (11) and (12) to calculate the input parameters and to double check them after getting the best fit between the synthetic and observed photometry.

$$M_{\rm bol} = M_V + B.C.,\tag{9}$$

$$\log \frac{L}{L_{\odot}} = \frac{M_{\rm bol}^{\odot} - M_{\rm bol}}{2.5},\tag{10}$$

$$\log \frac{R}{R_{\odot}} = 0.5 \log \frac{L}{L_{\odot}} - 2 \log \frac{T}{T_{\odot}},\tag{11}$$

$$\log g = \log \frac{M}{M_{\odot}} - 2\log \frac{R}{R_{\odot}} + 4.43.$$
 (12)

where $T_{\odot} = 5777 \,\mathrm{K}, R_{\odot} = 6.69 \times 10^8 \,\mathrm{m}$ and $M_{\mathrm{bol}}^{\odot} = 4^{\mathrm{m}}.75$.

In order to obtain the best stellar parameters, as we mentioned above, Al-Wardat's method is used to build a synthetic SED of the system based on the input parameters and on grids of line-blanketed model atmospheres (ATLAS9) (Kurucz 1994). This parameter could not be built unless we are fully aware of the information about its distance d and radius R (see Figs. 2 and 3). Hence, the entire synthetic SED as it would appear at the Earth's surface for the binary system is related to the individual synthetic SEDs of the components according to the following equation (Al-Wardat 2002, 2012)

$$F_{\lambda} \cdot d^2 = H_{\lambda}^A \cdot R_A^2 + H_{\lambda}^B \cdot R_B^2, \tag{13}$$

where F_{λ} is the flux for the entire synthetic SED of the binary system at the Earth, H_{λ}^{A} and H_{λ}^{B} are the





(b) HIP 84425

Fig. 3 The entire flux and individual synthetic SEDs of the binary system HIP 19206 (Fig. 3(a)) and HIP 84425 (Fig. 3(b)) using Kurucz blanketed models (Kurucz 1994) (ATLAS9).

fluxes of the primary and secondary components, in units of erg cm⁻² s⁻¹ Å⁻¹, while R_A and R_B are the radii of the primary and secondary components in solar units respectively.

Since we do not have the observational SED for the systems, we depend on the magnitudes and colour indices as a reference for the best fit with the synthetic ones, which ensures the reliability of the estimated parameters. This technique is a part of Al-Wardat's complex method for analysing CVBSs.

4 SYNTHETIC PHOTOMETRY

Stellar parameters depend mainly on the best fit of the magnitudes and colour indices between the entire observational and synthetic SED of the system. Therefore, we calculate the individual and total synthetic magnitudes and colour indices of the systems by integrating the total

Table 5	Magnitudes and	d Colour Indices	of the Entire	Synthetic Sp	ectrum and l	Individual (Components of	of HIP	19206 and
HIP 844	25			•			-		

Sys.	Filter	H	IIP 19206		Н	IP 84425	
		Entire Synth.	А	В	Entire Synth.	А	В
		$\sigma = \pm 0.03$			$\sigma = \pm 0.03$		
Joh-	U	7.55	7.73	9.62	6.63	6.77	8.95
Cou.	B	7.45	7.67	9.33	6.53	6.71	8.58
	V	6.88	7.14	8.58	5.95	6.17	7.79
	R	6.56	6.84	8.18	5.63	5.87	7.37
	U - B	0.09	0.05	0.29	0.10	0.06	0.37
	B - V	0.58	0.53	0.75	0.58	0.54	0.79
	V - R	0.32	0.93	0.40	0.32	0.93	0.40
Ström.	u	8.72	8.89	10.76	7.80	7.94	10.10
	v	7.78	7.97	9.73	6.86	7.02	9.01
	b	7.21	7.44	8.98	6.28	6.48	8.22
	y	6.86	7.11	8.54	5.92	6.14	7.75
	u - v	0.94	0.92	1.04	0.95	0.93	1.08
	v - b	0.56	0.53	0.74	0.58	0.54	0.79
	b-y	0.35	0.33	0.44	0.36	0.34	0.47
Tycho	B_T	7.59	7.79	0.86	6.67	6.84	8.79
	V_T	6.95	7.20	8.66	6.02	6.23	7.87
	$B_T - V_T$	0.65	0.59	0.86	0.65	0.60	0.92

Table 6Comparison between the Observational andSyntheticMagnitudes and Colour Indices for BothSystems

HIP	Filter	Observed (mag)	Synthetic (This work) (mag)
HIP 19206	$\begin{array}{c} V_J \\ B_T \\ V_T \\ (B-V)_J \\ \Delta m \end{array}$	$\begin{array}{c} 6.88 \\ 7.566 \pm 0.008 \\ 6.957 \pm 0.006 \\ 0.576 \pm 0.004 \\ 1.4 \end{array}$	$\begin{array}{c} 6.88 \pm 0.03 \\ 7.59 {\pm} 0.03 \\ 6.95 \pm 0.03 \\ 0.58 \pm 0.03 \\ 1.4 \end{array}$
HIP 84425	$\begin{array}{c} V_J \\ B_T \\ V_T \\ (B-V)_J \\ \Delta m \end{array}$	$\begin{array}{c} 5.95 \\ 6.67 \pm 0.013 \\ 6.015 \pm 0.006 \\ 0.58 \pm 0.002 \\ 1.6 \end{array}$	$\begin{array}{c} 5.95 \pm 0.03 \\ 6.67 {\pm} 0.03 \\ 6.02 \pm 0.03 \\ 0.58 \pm 0.03 \\ 1.6 \end{array}$

fluxes over each bandpass of the named photometrical system divided by that of the reference star (Vega), utilising the following equation (Al-Wardat 2012)

$$m_p[F_{\lambda,s}(\lambda)] = -2.5 \log \frac{\int P_p(\lambda) F_{\lambda,s}(\lambda) \lambda d\lambda}{\int P_p(\lambda) F_{\lambda,r}(\lambda) \lambda d\lambda} + \mathbb{ZP}_p$$
(14)

where m_p is the synthetic magnitude of the passband p, $P_p(\lambda)$ is the dimensionless sensitivity function of the passband p, $F_{\lambda,s}(\lambda)$ is the synthetic SED of the object and $F_{\lambda,r}(\lambda)$ is the SED of the reference star (Vega). Zero points (ZP_p) from Maíz Apellániz (2007) are used.

We applied the best fit between the entire observational and synthetic magnitudes, magnitude differences of the components ($\Delta m = V_J^B - V_J^A$) and colour indices to judge the accuracy of the estimated parameters.

The entire flux is calculated from the individual fluxes of the components utilising Equation (13) and depending on the parallax of the system.

As mentioned above, we get the colour indices of the individual components and entire synthetic SEDs of two

Table 7 The Fundamental Parameters of the IndividualComponents of HIP 19206 as Estimated Applying Al-Wardat's Method

		HIP 1	9206
Parameters	Units	HIP 19206 A	HIP 19206 B
$T_{\rm eff} \pm \sigma_{T_{\rm eff}}$	(K)	6300 ± 100	5600 ± 100
$R \pm \sigma_R$	(R_{\odot})	1.417 ± 0.06	0.978 ± 0.05
$\log g \pm \sigma_{\log g}$	$({\rm cm}{\rm s}^{-2})$	4.18 ± 0.11	4.40 ± 0.13
$L \pm \sigma_{\rm L}$	(L_{\odot})	2.842 ± 0.30	0.845 ± 0.10
$M_{\rm bol} \pm \sigma_{\rm M_{\rm bol}}$	(mag)	3.81 ± 0.08	4.87 ± 0.08
$M_V \pm \sigma_{M_V}$	(mag)	3.97 ± 0.13	5.08 ± 0.14
Sp. Type ¹		F7V	G6V
M	(M_{\odot})	1.23 ± 0.15	0.91 ± 0.10
$M_{\rm tot}$	$[M_{\odot}]$	2.14	= 0.15
$M_{dyn}^* \pm \sigma_M$	(M_{\odot})	$1.873 \pm$	0.0.215
$M_{dvn}^{**} \pm \sigma_M$	(M_{\odot})	$1.76 \pm$	0.133
$M_{dvn}^{***} \pm \sigma_M$	(M_{\odot})	2.087 ±	= 0.128
$\pi^2_{\rm dyn}$	(mas)	22.97 :	± 0.95
Age^2	(Gyr)	2.82 ±	= 0.35

¹Using the tables of Lang (1992) and Gray (2005).

²Depending on the the isochrones for low- and intermediate-mass stars with different metallicities of Girardi et al. (2000a) (see Fig. 5)

with different metallicities of Girardi et al. (2000a) (see Fig. 5). * Using ($\pi_{Hip1997}$); ** Using ($\pi_{Hip2007}$); *** Using ($\pi_{Gaia2018}$).

systems, in three photometrical systems, Johnson: U, B, V, R, U - B, B - V, V - R; Strömgren: u, v, b, y, u - v, v - b, b - y and Tycho: $B_T, V_T, B_T - V_T$, which are listed in Table 5.

5 RESULTS AND DISCUSSION

Table 5 lists the results of the synthetic magnitudes and colour indices of the entire systems and individual components under three photometric systems, Johnson: U, B, V, R, U - B, B - V, V - R; Strömgren: u, v,b, y, u - v, v - b, b - y and Tycho: $B_T, V_T, B_T - V_T$). In addition, Table 6 gives a comparison between



Fig. 4 The positions of the components of HIP 19206 and HIP 84425 on the evolutionary tracks of Girardi et al. (2000a) for the masses (0.6, 0.7, ..., 1.4 M_{\odot}). Fig. 4(b) depicts the positions of the components as estimated using the parallaxes supplied by Hipparcos and Gaia (See Table 1).

the entire synthetic magnitudes and colour indices of the two systems with the available observed ones within three photometric systems. The consistency between the synthetic and observed photometry indicates the reliability of the fundamental parameters of the two systems.

Hereafter we discuss the results of each system separately: **HIP 19206**: Table 2 lists the modified orbital elements as per the new orbital solution, which used a total of 41 relative positional measurements, along with the elements of the previous solutions of Balega et al. (2006b), Tokovinin et al. (2015) and Tokovinin (2019). The root mean square (rms) values of the new solution $\Delta \theta = 0.10^{\circ}$ and $\Delta \rho = 0.0002''$ are better than those of the previous solutions.



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Fig. 5 The positions of the components of HIP 19206 and HIP 84425 on the isochrones of low- and intermediate-mass stars with different metallicities. The isochrones were referenced from Girardi et al. (2000a).

Table 7 lists the final fundamental parameters of the system. It shows that the dynamical mass sum of the system using Gaia parallax (23.4039 ± 0.4727) is given by 2.087 ± 0.128 which is the closest to the mass sum given by Al-Wardat's method of 2.14 ± 0.15 . This means that Gaia parallax measurement is the best among the other measurements, but in order to achieve the best consistency between the dynamical mass sum and that of Al-Wardat's method, we propose a new dynamical parallax for the system of 22.97 ± 0.95 mas.

It is worthwhile to mention here that this work was done before Gaia Early Data Release 3 (EDR3) in December 2020 which gives a very close trigonometric parallax for the system of 22.3689 ± 0.4056 mas (Gaia Collaboration et al. 2020).

The reason why we introduced a new parallax measurement is that parallax measurements of binary and multiple systems are, in some cases, distorted by the orbital

Table 8	The Fundamental Parame	eters of the Individua	al Components of H	HIP 84425 as 1	Estimated Applying	g Al-Wardat's
Method						

		HIP 84425				
		HIP	2007	Gaia 2018		
Parameters	Units	HIP 84425 A	HIP 84425 B	HIP 84425 A	HIP 84425 B	
$T_{\rm eff} \pm \sigma_{T_{\rm off}}$	(K)	6220 ± 100	5650 ± 100	6220 ± 100	5650 ± 100	
$R \pm \sigma_R^{en}$	(R_{\odot})	1.63 ± 0.06	0.96 ± 0.05	1.74 ± 0.06	1.07 ± 0.05	
$\log g \pm \sigma_{\log q}$	$(cm s^{-2})$	4.09 ± 0.12	4.26 ± 0.10	4.137 ± 0.11	4.321 ± 0.12	
$L \pm \sigma_L$	(L_{\odot})	4.04 ± 0.30	1.05 ± 0.10	3.49 ± 0.30	0.91 ± 0.15	
$M_{\rm bol} \pm \sigma_{M_{\rm bol}}$	(mag)	3.23 ± 0.08	4.70 ± 0.09	3.393 ± 0.09	4.853 ± 0.09	
$M_V \pm \sigma_{M_V}$	(mag)	3.29 ± 0.13	4.89 ± 0.13	3.453 ± 0.13	5.043 ± 0.13	
Sp. Type ¹	-	F7.5V	G8V	F7.5V	G8V	
M	(M_{\odot})	1.31 ± 0.13	0.89 ± 0.12	1.29 ± 0.12	0.88 ± 0.12	
$M_{\rm tot}$	(M_{\odot})	$2.2 \pm$	0.15	2.17 =	± 0.15	
$M_{\rm dyn} \pm \sigma_{\rm M}$	(M_{\odot})	2.287 ± 0.133		2.842 =	± 0.146	
$\pi_{\rm dvn}$	(mas)	33.26 ± 1.5				
Age ²	(Gyr)	3.16	± 0.35			

¹Using the tables of Lang (1992) and Gray (2005).

²Depending on the the isochrones for low- and intermediate-mass stars with different metallicities from Girardi et al. (2000a) (see Fig. 5).

motion of the components of such systems as noted by several other researchers (i.e. Shatskii & Tokovinin 1998).

The fundamental parameters of the systems' components, their positions on the evolutionary tracks of Girardi et al. (2000a) (Fig. 4(a)), and on the isochrones of Girardi et al. (2000b) (Fig. 5(a)), confirm that they are twin solar type main sequence stars with a metallicity of 0.019, which predicts that fragmentation is the most probable formation process for the system.

HIP 84425: Table 3 lists the modified orbital elements as per the new orbital solution, which used a total of 13 relative positional measurements, along with the elements of the previous solutions of Söderhjelm (1999), Rica Romero (2010) and Tokovinin et al. (2015). The RMS values of the new solution $\Delta \theta = 0.06^{\circ}$ and $\Delta \rho = 0.0001''$ are much better than those of the previous solutions.

Table 8 lists the fundamental parameters of the system as given by Al-Wardat's method incorporating two parallax measurements: Hipparcos 2007 and Gaia 2018. So, we have to decided which set of parameters better represent the system.

In order to do so, it should be remembered that the dynamical mass sum is strongly affected by parallax, while the masses estimated utilising Al-Wardat's method are not as highly affected by the change in parallax. This is clear in Figure 4(b) which shows the positions of the components of HIP 84425 on the evolutionary tracks when considering both the parallax given by Hipparcos 2007 and that provided by Gaia 2018.

Now, depending on the mass sum of Al-Wardat's method of 2.2 ± 0.15 mas, we estimate a new dynamical parallax of 33.26 ± 1.5 , which is closer to that of Hipparcos 2007 of 32.69 ± 0.59 . So, we adopt the fundamental parameters listed in Table 8 columns 3 and 4.

The fundamental parameters of the systems' components, their positions on the evolutionary tracks of Girardi et al. (2000a) (Fig. 4(b)) and on the isochrones of Girardi et al. (2000b) (Fig. 5(b)) affirm that they are twin solar type in their final main sequence stage with a metallicity of 0.019, which predicts that fragmentation is the most probable formation process for the system.

6 CONCLUSIONS

Using the recent parallax measurements supplied by Gaia (Gaia DR2), we were able to present a complete analysis for the two CVBSs HIP 19206 and HIP 84425.

The technique relies on a dynamical and a spectrophotometrical method in a complementary iterated way, to estimate the complete set of their fundamental parameters.

In order to get the precise fundamental parameters of the systems, we utilise a combination of a dynamical method (ORBITX) (Tokovinin et al. 2016), and a computational spectrophotometrical method (Al-Wardat's method for analysing CVBMSs, which employs grids of Kurucz (1994) line-blanketed plane-parallel model atmospheres (ATLAS 9) for single stars).

As is well known in astrophysics, masses of BS components represent one of the crucial parameters, either by being a common parameter between the dynamical method and the spectrophotometrical one, or for being one of the most important results from the analysis for their essential role in stellar evolution theories.

The analysis of the the systems under study displayed a good consistency between the mass sum using the dynamical solutions and the masses estimated applying Al-Wardat's method. But, in order to achieve a better consistency, a new dynamical parallax is given in this work for both systems. The results demonstrate that the components of the HIP 19206 system are main sequence stars, and the components of HIP 84425 have left the main sequence to the subgiant stage. The components of each system have quite similar parameters and the same age. Hence, fragmentation is the most probable process for the formation and evolution of both systems, where Bonnell (1994) concluded that fragmentation of a rotating disk around an incipient central protostar is possible, as long as there is continuing infall, and Zinnecker & Mathieu (2001) pointed out that hierarchical fragmentation during rotational collapse has been invoked to produce binaries and multiple systems.

As a consequence, the results of such studies would improve our understanding of the nature, formation and evolution of binary and multiple stellar systems.

Finally, synthetic photometry, consistency of the results between the two methods and consistency between some parameters with the available observational data give an indication about the accuracy of the applied methods, and hence the estimated stellar parameters for both systems.

Acknowledgements The data that support the findings of this study are openly available in The Gaia Data Release 2 (Gaia DR2) at https://gea.esac.esa.int/ archive. This research has made use of SAO/NASA, SIMBAD database, Fourth Catalog of Interferometric Measurements of Binary Stars, Sixth Catalog of Orbits of Visual Binary Stars, IPAC data systems, ORBITX code and Al-Wardat's complex method for analysing close visual binary and multiple systems with its codes.

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