

## The column density structure of Orion A depicted by N-PDF

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Received 2019 October 22; accepted 2019 December 10

**Abstract** We have conducted a large-field simultaneous survey of  $^{12}\text{CO}$ ,  $^{13}\text{CO}$  and  $\text{C}^{18}\text{O } J = 1 - 0$  emission toward the Orion A giant molecular cloud (GMC) with a sky coverage of  $\sim 4.4 \text{ deg}^2$  using the Purple Mountain Observatory (PMO)-13.7 m millimeter-wavelength telescope. We use the probability distribution function of the column density (N-PDF) to investigate the distribution of molecular hydrogen in the Orion A GMC. The  $\text{H}_2$  column density, derived from the  $^{13}\text{CO}$  emission, of the GMC is dominated by a log-normal distribution in the range from  $\sim 4 \times 10^{21}$  to  $\sim 1.5 \times 10^{23} \text{ cm}^{-2}$  with excesses both at the low-density and high-density ends. The excess of the low-density end is possibly caused by an extended and low-temperature ( $\sim 10 \text{ K}$ ) component with velocities in the range of  $5 - 8 \text{ km s}^{-1}$ . Compared with the northern sub-regions, the southern sub-regions of the Orion A GMC contain less gas with column density in  $N_{\text{H}_2} > 1.25 \times 10^{22} \text{ cm}^{-2}$ . The dispersions of the N-PDFs of the sub-regions are found to correlate with the evolutionary stages of the clouds across the Orion A GMC. The structure hierarchy of Orion A GMC is explored with the DENDROGRAM algorithm, and it is found that the GMC is composed of two branches. All structures except one in the tree have virial parameters less than 2, indicating self-gravity is important on the spatial scales from  $\sim 0.3$  to  $\sim 4 \text{ pc}$ . Although power-laws and departures from lognormal distributions are found at the high-density end of N-PDFs for active star-forming regions, the N-PDFs of structures in the Orion A GMC are predominantly lognormal on scales from  $R \sim 0.4$  to  $4 \text{ pc}$ .

**Key words:** ISM: clouds — ISM: individual objects (Orion A) — ISM: structure — stars: formation — surveys — turbulence

### 1 INTRODUCTION

Stars form in cold and dense molecular clouds. The cloud structure is affected by various physical processes, such as turbulence, cloud-cloud collisions, and feedbacks from massive stars. The probability distribution function (PDF) is a simple but potent tool to depict the structure of molecular clouds, therefore, providing an effective means to investigate the various physical processes that influence the structures of molecular clouds. Theoretical studies (Vazquez-Semadeni 1994; Padoan et al. 1997; Klessen 2000) of supersonic turbulence suggest that the volume density PDFs ( $\rho$ -PDFs) of molecular clouds exhibit lognormal shapes when self-gravity is not important. This characteristic has been attributed to the influence of some steady and multiple independent dynamical events that shape the molecular clouds (McKee & Ostriker 2007). When star

formation activities occur, the  $\rho$ -PDF is strongly affected by gravity in addition to turbulence, resulting in excess above the lognormal distribution at the high density end (Kainulainen et al. 2014; Federrath & Klessen 2013).  $\rho$ -PDF also proves to be a reliable indicator for the star formation rate and efficiency of molecular clouds in different star formation models (Elmegreen 2008; Padoan et al. 2014). However, it is challenging to constrain the underlying  $\rho$ -PDFs of molecular clouds with observations because of the projection effect along the line-of-sight. Instead, a lot of theoretical and observational studies focused on the column density PDFs (N-PDFs). Simulations have suggested an evolutionary trend of molecular clouds from the turbulence dominated stages to the gravity dominated star-forming stages (Ballesteros-Paredes et al. 2011; Kritsuk et al. 2011). The gravity first broadens the lognormal N-PDF at the beginning and then produces a power-law tail

in the N-PDF (Ballesteros-Paredes et al. 2011). The slope of the power-law tail develops over time and gets shallower as the star formation efficiency (SFE) increases.

Observationally, three tracers of column density are widely used, which are the near-infrared dust extinction, the far-infrared dust emission, and the optically thin molecular line emission. Comparatively, dust extinction probes the largest dynamic range of column density and less relies on models (Goodman et al. 2009a). However, the gas tracer can provide us with kinematic information on the molecular clouds, which helps to disentangle their structure. Lognormal shaped N-PDFs derived with the three tracers have been observed in the Perseus cloud (Goodman et al. 2009a), and power-law N-PDFs have been observed in active star-forming regions (Kainulainen et al. 2009; Schneider et al. 2013; Lombardi et al. 2015). In the observations mentioned above, quiescent clouds often exhibit lognormal N-PDFs in the whole dynamic range or only have modest excesses at the high density ends. In contrast, clouds active in star formation have N-PDFs with prominent non-lognormal or power-law high-density tails arising from the dense star-forming regions.

As the nearest massive star-forming region ( $d = 414$  pc, Menten et al. 2007), the Orion A giant molecular cloud (GMC) is notable for its complex hierarchical filamentary structure and intense star formation activities (Bally 2008). There have been plenty of large-scale surveys toward the Orion A GMC at multiple wavelengths (Bally et al. 1987; Sakamoto et al. 1994; Johnstone & Bally 1999; Shimajiri et al. 2011; Megeath et al. 2012; Fischer et al. 2013; Ripple et al. 2013; Stutz et al. 2013; Berné et al. 2014; Shimajiri et al. 2014; Nishimura et al. 2015; Stutz & Kainulainen 2015; Großschedl et al. 2018; Hacar et al. 2018; Kong et al. 2018; Suri et al. 2019). The GMC is mainly composed of a large and dense integral-shaped filament (ISF, Bally et al. 1987) in the northern part that contains star-forming regions OMC 1 – 4, and a relatively extended and less dense tail in the southern part that covers the LDN 1641 region. Kong et al. (2018) have made a brief review of the surveys that cover the ISF in their table 1. The broad dynamic range of column densities revealed by the previous studies makes the GMC an ideal case for N-PDF analysis. The N-PDF of the Orion A GMC has been derived with multi-wavelength observations (Kainulainen et al. 2009; Lombardi et al. 2015; Stutz & Kainulainen 2015; Berné et al. 2014), with most of them presenting an N-PDF of power-law shape. However, most of the previous N-PDF studies of Orion A are limited to the ISF region except for the *Herschel* observations (Stutz & Kainulainen 2015) (S15 hereafter). S15 found that all the N-PDFs in different subregion-

s of the Orion A GMC exhibit power-law distributions, and the power-law exponent of the N-PDF correlates with the fraction of Class 0 protostars. For a panoramic view of the Orion A GMC, it is valuable to study the N-PDF of the entire Orion A GMC using molecular line emission and make comparison with N-PDFs derived using dust emission. Furthermore, for investigating the relation between N-PDF forms and the underlying physics, it is necessary to investigate the dependence of the N-PDF forms and the role of self-gravity on spatial scales. There are several automatic algorithms that can identify structures in molecular clouds, like CLUMPFIND (Williams et al. 1994), GAUSSCLUMPS (Stutzki & Guesten 1990), FELLWALKER (Berry 2015), CPROPS (Rosolowsky & Leroy 2006) and DENDROGRAM (Rosolowsky et al. 2008). Among the algorithms, DENDROGRAM can reveal the hierarchical nature of molecular clouds, and it is relatively insensitive to the input parameters.

In this work, we present a detailed analysis of N-PDF of the Orion A GMC using the  $^{12}\text{CO}$  and  $^{13}\text{CO}$   $J = 1 - 0$  emission line data from a large-scale ( $\sim 4.4$  deg $^2$ ) survey toward the GMC. The N-PDFs of the hierarchical structures and the role of gravity on different spatial scales in the Orion A GMC have been studied employing the DENDROGRAM technique. In Section 2, we describe the observations and data reduction processes. The main results are presented in Section 3. The N-PDF properties and the importance of gravity in the GMC on different spatial scales are discussed in Section 4. We summarize our results and make conclusions in Section 5.

## 2 OBSERVATIONS AND DATA REDUCTION

### 2.1 Observations

The observations were made using the Purple Mountain Observatory (PMO)-13.7 m millimeter-wavelength telescope located in Delingha, China during June 2011 as a pilot survey of the Milky Way Imaging Scroll Painting (MWISP) project<sup>1</sup> (Su et al. 2019). The PMO-13.7 m telescope is equipped with a nine-beam Superconducting Spectroscopic Array Receiver (SSAR) that works in the 85 – 115 GHz frequency band (Shan et al. 2012). With a carefully selected local oscillator (LO) frequency, the  $^{12}\text{CO}$ ,  $^{13}\text{CO}$  and  $\text{C}^{18}\text{O}$   $J = 1 - 0$  line emission data can be obtained simultaneously with this instrument. The upper sideband contains the  $^{12}\text{CO}$   $J = 1 - 0$  and the lower sideband contains the  $^{13}\text{CO}$  and  $\text{C}^{18}\text{O}$   $J = 1 - 0$  line emission. For each sideband, a Superconductor-Insulator-Superconductor (SIS) mixer works as the front end of the receiver. The back end of the receiver is a Fast Fourier

<sup>1</sup> <http://www.radioast.nsd.cnr.cn/mwisp.php>

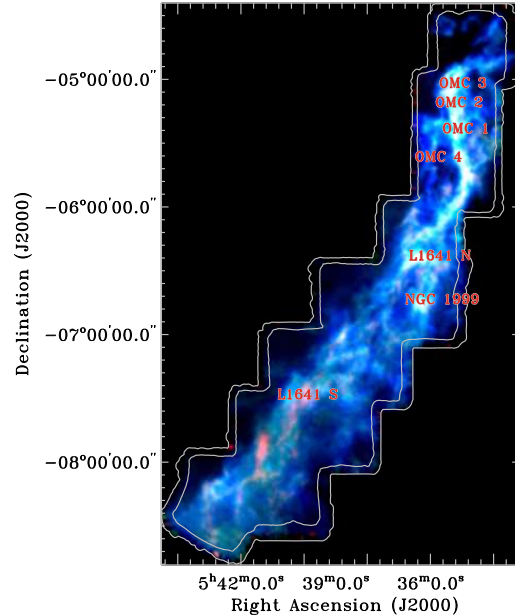
Transform Spectrometer (FFTS) with 16 384 frequency channels and a total bandwidth of 1 GHz, providing a velocity resolution of  $0.17 \text{ km s}^{-1}$  at 110 GHz. At 110 GHz and 115 GHz, the half-power beam width (HPBW) of the telescope is about  $52''$  and  $50''$ , respectively.

The observations were conducted in the position-switch on-the-fly (OTF) mode. The Orion A GMC is divided into twelve  $30' \times 30'$  cells. For each cell, two scanings were made along the directions of right ascension and declination, respectively. The scanning rate of the observation is  $50''$  per second and the dump time is 0.3 s. The antenna temperature is calibrated according to  $T_{\text{MB}} = T_{\text{A}}^* / \eta_{\text{MB}}$  during the data reduction processes. According to the status report of the PMO-13.7 m telescope, the main beam efficiencies are 0.44 and 0.48 at the  $^{12}\text{CO } J = 1 - 0$  and  $^{13}\text{CO } J = 1 - 0$  wavelengths, respectively. We apply the GILDAS/CLASS software package to reduce the data, which include the subtraction of a second order baseline from each spectrum and the re-gridding of the raw data. At the positions where multiple spectra are taken at different times, a combination of the spectra is made using the reciprocal square of the root mean square (RMS) noise level of each spectrum as the weight. The final reduced data cube covers a sky area of  $\sim 4.4 \text{ deg}^2$ , which contains the majority CO emission of the GMC as revealed by Bally et al. (1987). However, the spectra at the edge of the surveyed area have low signal-to-noise ratios and they are removed in the analysis of this work. The trimmed edge area, indicated with grey lines in Figure 1, accounts for about twenty percent of the scanned area. The final median RMS noise level of the  $\sim 3.5 \text{ deg}^2$  effective region is 0.61 K per channel at 115 GHz and 0.37 K per channel at 110 GHz.

## 2.2 Method of Structure Identification

In this work, we use the DENDROGRAM algorithm to extract “tree” structures from the  $\text{H}_2$  column density map and investigate the properties of the N-PDFs of the hierarchical structures and the importance of self-gravity at various spatial scales in Orion A in Section 4. The threshold and the difference between two separate column density peaks for the identification of the “leaf” of the tree structure are set to be 2.0 and 3.0 times the median noise level of  $N_{\text{H}_2}$  (see text in Sect. 3.1), respectively. The minimum pixel number of a “leaf” structure is set to 200, which physically corresponds to a clump of the size  $\sim 0.8 \times 0.8 \text{ pc}^2$  at the cloud distance. The outputs of the DENDROGRAM provide masks of the identified structures.

We evaluate the importance of self-gravity in a molecular structure with the virial parameter  $\alpha_{\text{vir}}$ , which measures the ratio between the total kinetic energy and the gravitational energy. The widely used definition of  $\alpha_{\text{vir}}$  is



**Fig. 1** Color-coded image of integrated intensity of the Orion A GMC, with the  $^{12}\text{CO}$  emission in the velocity range from  $-10$  to  $20 \text{ km s}^{-1}$  in blue, the  $^{13}\text{CO}$  emission from  $0$  to  $18 \text{ km s}^{-1}$  in green and the  $\text{C}^{18}\text{O}$  emission from  $0$  to  $14 \text{ km s}^{-1}$  in red. The grey lines outline the noisy edge of the surveyed area that has been trimmed in the analysis. Active star-forming regions in the GMC are indicated with red letters.

$5\sigma_v^2 R / GM_c$ , where  $\sigma_v$  is the one-dimensional velocity dispersion,  $G$  is the gravitational constant, and  $R$  and  $M$  are the effective radius and mass of the structure, respectively. The critical value of  $\alpha_{\text{vir}}$  for a marginally bound structure is 2 (Kauffmann et al. 2013). The angular size of a structure is defined as the geometric mean of the full widths at half maximum (FWHMs) of its major and minor axes, which can be obtained in the output table of the DENDROGRAM algorithm, and the local thermodynamic equilibrium (LTE) mass can be obtained using the total column density within the periphery of the structure. The velocity dispersion of a molecular structure is obtained by fitting a Gaussian function to the average spectrum of the  $^{13}\text{CO}$  emission.

## 3 RESULTS

Figure 1 presents the composite intensity map of the  $^{12}\text{CO}$ ,  $^{13}\text{CO}$  and  $\text{C}^{18}\text{O } J = 1 - 0$  emission from the Orion A GMC. The  $^{12}\text{CO}$  and  $^{13}\text{CO}$  emission in the region is much more extended than the  $\text{C}^{18}\text{O}$  emission, which is mostly concentrated in the active star-forming regions indicated in Figure 1. Compared with the emission of the  $^{12}\text{CO}$  and  $^{13}\text{CO}$ , the  $\text{C}^{18}\text{O}$  emission traces positions with high column density, therefore, only providing a limited dynamical range for the N-PDF study. In the present work, we consid-

er the  $^{12}\text{CO}$  and  $^{13}\text{CO}$  data for the N-PDF analysis, and the analysis of the  $\text{C}^{18}\text{O}$  data is deferred to a future paper.

### 3.1 Calculation of the Column Density

The  $^{12}\text{CO}$  emission is usually optically thick in typical molecular cloud environments, while the  $^{13}\text{CO}$  emission is often optically thin. Providing the molecular clouds are under the conditions of LTE and the molecules are uniformly excited, the column density of the clouds can be derived with the  $^{12}\text{CO}$  and  $^{13}\text{CO}$  spectra.

Firstly, the excitation temperature can be obtained with the peak brightness temperature of the optically thick  $^{12}\text{CO}$  line (Li et al. 2018),

$$T_{\text{ex}} = 5.532 \left[ \ln \left( 1 + \frac{5.532}{T_{\text{peak}} + 0.819} \right) \right]^{-1}, \quad (1)$$

where  $T_{\text{peak}}$  is the peak brightness temperature of the  $^{12}\text{CO}$   $J = 1 - 0$  line. The optical depth and the column density of the  $^{13}\text{CO}$   $J = 1 - 0$  emission can be derived through (Pineda et al. 2010; Li et al. 2018)

$$\tau_v^{13} = -\ln \left\{ 1 - \frac{T_{\text{MB}}(^{13}\text{CO})}{5.29[J(T_{\text{ex}}) - 0.164]} \right\}, \quad (2)$$

$$N_{^{13}\text{CO}} = 2.42 \times 10^{14} \frac{T_{\text{ex}} + 0.88}{1 - e^{-5.29/T_{\text{ex}}}} \int \tau_v^{13} dv, \quad (3)$$

where  $T_{\text{ex}}$  is the excitation temperature, and  $J(T_{\text{ex}}) = [\exp(5.29/T_{\text{ex}}) - 1]^{-1}$ . According to Pineda et al. (2010), when the optical depth of the  $^{13}\text{CO}$  emission is small,  $\tau_v^{13} < 1$ , the integral item  $T_{\text{ex}} \int \tau dv$  can be approximated to  $\tau_0 / (1 - e^{-\tau_0}) \int T_{\text{mb}} dv$ , where  $\tau_0$  is the peak optical depth of the  $^{13}\text{CO}$  emission line. Provided that the abundance ratios  $[^{12}\text{C}]/[^{13}\text{C}] = 69$  (Wilson 1999) and  $[\text{CO}]/[\text{H}] \sim 10^{-4}$  (Solomon & Klemperer 1972; Herbst & Klemperer 1973), the  $[\text{H}_2/^{13}\text{CO}]$  ratio is expected to be  $7 \times 10^5$ , the column density of molecular hydrogen can be obtained with the following formula (Li et al. 2018)

$$N_{\text{H}_2} = 1.694 \times 10^{20} \frac{\tau_0}{1 - e^{-\tau_0}} \frac{1 + 0.88/T_{\text{ex}}}{1 - e^{-5.29/T_{\text{ex}}}} \times \int T_{\text{MB}}(^{13}\text{CO}) dv. \quad (4)$$

The peak brightness temperature of  $^{12}\text{CO}$  emission and the integrated intensity of  $^{13}\text{CO}$  emission are calculated in the velocity range from 0 to  $18 \text{ km s}^{-1}$ . Observationally, molecular clouds are defined as contiguous structures above a fixed brightness temperature in the position-position-velocity space. The molecular line emission from the clouds should have a certain width of velocity dispersion ( $\sigma_v \sim 1 \text{ km s}^{-1}$ ). To avoid missing weak signals and to ensure an adequate signal-to-noise ratio, we

only use the spectra that have at least five contiguous velocity channels with intensities higher than  $3\sigma_{\text{rms}}$  for  $^{12}\text{CO}$  for the calculation of excitation temperature, and  $1.5\sigma_{\text{rms}}$  for  $^{13}\text{CO}$  for the calculation of column density. According to the above criteria, the signal-to-noise ratio of selected  $^{13}\text{CO}$  spectra is above 3.35, which is sufficiently high to exclude the noisy channels. The three-sigma detection limit of the  $\text{H}_2$  column density is  $\sim 1.5 \times 10^{21} \text{ cm}^{-2}$  under the criteria.

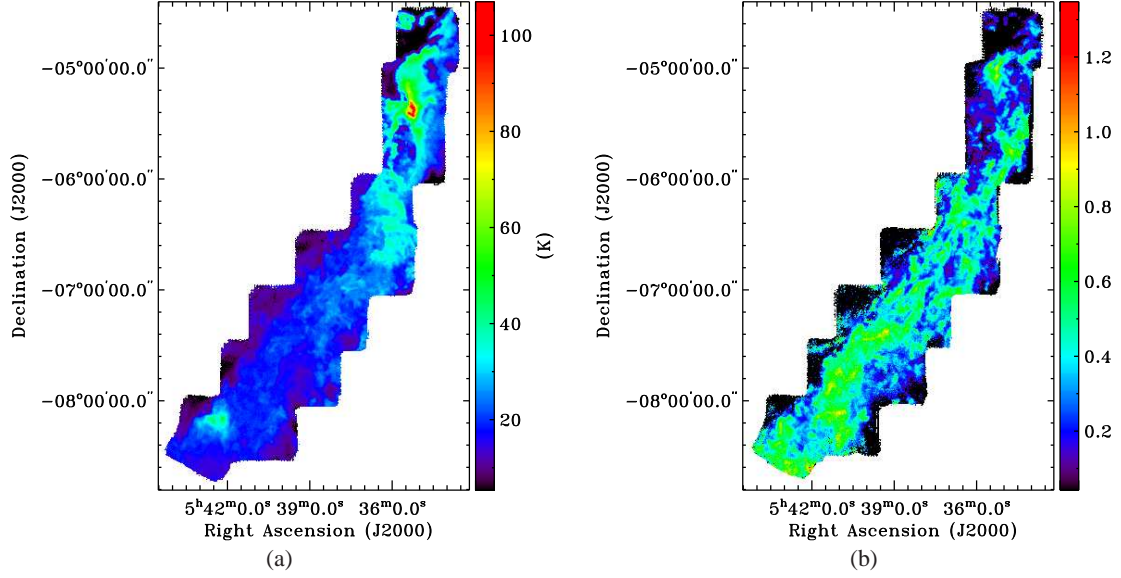
### 3.2 Basic Properties of the Orion A GMC

Figure 2(a) displays the spatial distribution of the excitation temperature derived using Equation (1). The excitation temperatures of Orion A range from 5 to 107 K. In the ISF and L 1641 N regions, most of the excitation temperatures are above 25 K. In the OMC 1 region, which lies behind the Orion Nebula, the temperatures are  $\sim 50$  K on average and reach the maximum 107 K at the position of Orion KL. Comparatively, the southern part of the GMC is much colder except for the southeastern tail. The distribution of the  $^{13}\text{CO}$  optical depth is depicted in Figure 2(b). The optical depths,  $\tau^{13}$ , range from 0.04 to 1.35 with a median value of 0.37, and only 23 pixels have optical depths greater than 1, indicating the  $^{13}\text{CO}$  emission in the region is mostly optically thin.

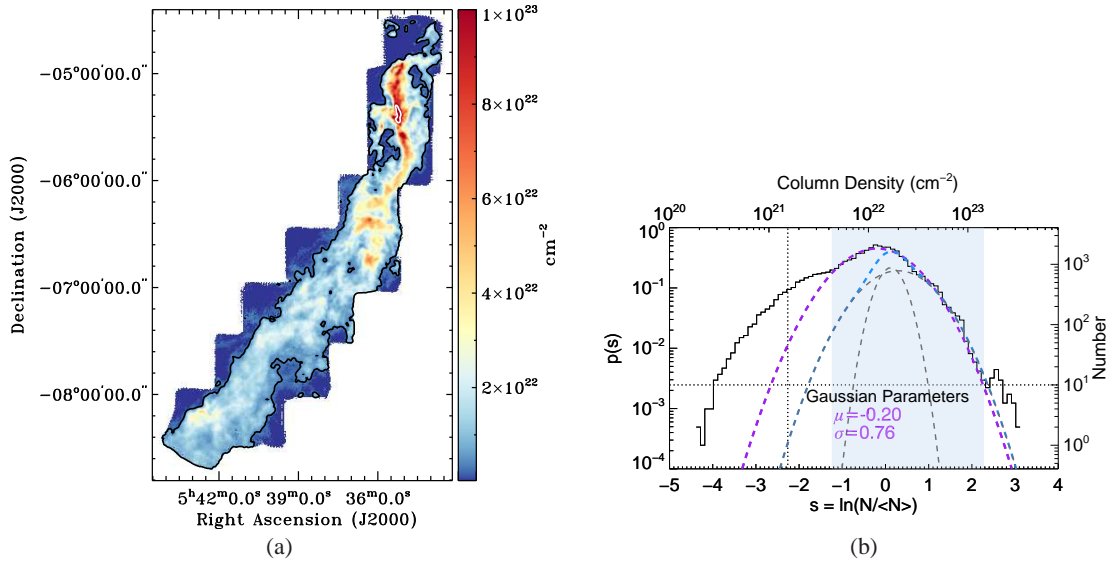
### 3.3 N-PDF of the Entire Orion A GMC

#### 3.3.1 Overall properties of the $\text{H}_2$ column density distribution

The spatial distribution of the  $\text{H}_2$  column density of Orion A GMC is displayed in Figure 3(a). The corresponding pixel-by-pixel statistic is given in Figure 3(b). The median detection limit based on the selection criteria described in Section 3.1 is  $1.5 \times 10^{21} \text{ cm}^{-2}$ . As shown in Figure 3(a), the northern ISF and the L 1641 N regions contain more high-density gas than the southern regions. In Figure 3(b), we totally use 40 592 pixels for the statistics and the mean  $\text{H}_2$  column density is about  $1.5 \times 10^{22} \text{ cm}^{-2}$ , which is much higher than the threshold of star formation of  $6.3 \times 10^{21} \text{ cm}^{-2}$  (Johnstone et al. 2004; Lada et al. 2010; Kainulainen et al. 2014). The highest column density is associated with the Orion KL region, up to a value of  $\sim 3 \times 10^{23} \text{ cm}^{-2}$ . The column densities derived with CO line emission in the Orion A GMC in this work are higher than those derived with the dust tracer (S15) and are also higher than the column densities derived with CO in other nearby star-forming regions, like the Perseus molecular cloud (Goodman et al. 2009a; Kainulainen et al. 2009).



**Fig. 2** (a) Excitation temperature derived from the <sup>12</sup>CO emission. (b) Distribution of peak optical depth of the <sup>13</sup>CO emission.



**Fig. 3** (a) Spatial distribution of H<sub>2</sub> column density of the Orion A GMC. The *black contours* and the *white contour* at the middle of ISF correspond to the lower and higher critical values  $4 \times 10^{21} \text{ cm}^{-2}$  and  $1.5 \times 10^{23} \text{ cm}^{-2}$ , respectively, at which the N-PDF departs from a lognormal distribution. (b) N-PDF of H<sub>2</sub> column density for the Orion A GMC. The *purple dashed line* traces the fitted Gaussian function of  $s = \ln(N/\langle N \rangle)$  within the fitting range from  $N_{\text{H}_2} = 4.4 \times 10^{21} \text{ cm}^{-2}$  to  $N_{\text{H}_2} = 1.4 \times 10^{23} \text{ cm}^{-2}$ , which is indicated with *light blue shadow*. The *vertical* and *horizontal dashed lines* mark the median detection limit and the level at which the number of pixels in a bin is ten respectively. The fitted parameters  $\mu$  and  $\sigma$  of the Gaussian function are indicated in *purple* below the *horizontal dashed line*. The *grey dashed lines* are the N-PDFs of the dendrogram structures 5 (narrow) and 11 (wide), and the *blue dashed line* is the summation N-PDF of the two structures. For structures 5 and 11, see discussions in Sect. 4.2.

Mathematically, if a variable  $N$  follows a lognormal distribution, its natural logarithm distribution is normal. The lognormal probability density function has the form

$$p(N) = \frac{1}{N} \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(\ln N - \mu)^2}{2\sigma^2}}, \quad (5)$$

where  $\mu$  and  $\sigma$  are the mean and dispersion of  $\ln N$ , respectively. In the histogram in Figure 3(b), the H<sub>2</sub> column density  $N$  is normalized by its mean, i.e., the statistical variable is  $s = \ln(N/\langle N \rangle)$ . As shown in Figure 3(b),  $s$  can be well fitted with a Gaussian function rather than a power-law function in the column density range from  $4 \times 10^{21} \text{ cm}^{-2}$  to  $1.5 \times 10^{23} \text{ cm}^{-2}$ . In the log-log space, the

lognormal function is a parabolic curve, as signified by the purple dashed line in Figure 3(b). Beyond the fitting range, the N-PDF deviates from the lognormal distribution at both the low-density and high-density ends. The low-density deviation mostly corresponds to diffuse gas at the edge of the cloud, which is outside the black contour in Figure 3(a), while the high-density excess is associated with the very active star-forming regions Orion KL and Orion Bar.

### 3.3.2 The low-density excess above the lognormal distribution

In Figure 3(b), the low-density deviation from the lognormal distribution of the N-PDF is quite obvious and is different from the previous results of the Orion A region using either dust or gas tracers (Berné et al. 2014, S15). We present channel maps of the  $^{12}\text{CO}$  emission in Figure 4, and those of  $^{13}\text{CO}$  emission in Figure B.1, to investigate which velocity components contribute to the low-density end of the N-PDF. The  $4 \times 10^{21} \text{ cm}^{-2}$  contour is overlaid in each panel of Figures 4 and B.1. Outside the  $4 \times 10^{21} \text{ cm}^{-2}$  contour, extended diffuse gas is present in the velocity channels from 5.5 to 8.5  $\text{km s}^{-1}$ , which is more apparent in the  $^{12}\text{CO}$  channel maps than in the  $^{13}\text{CO}$  channel maps. From Figure 4, it can be seen that the diffuse gas mainly exists in the region below  $\delta = -5^\circ 57' 00''$ . Dividing the Orion A GMC by the declination of  $\delta = -5^\circ 57' 00''$ , we separately calculated the N-PDFs of the northern and southern parts of the GMC. The results are presented in Figure 5. The N-PDFs of the two parts are quite different. The excesses above the lognormal distribution at the low-density end of the N-PDF are more obvious in the southern portion than in the northern portion of the GMC.

Figure 6 presents the position-velocity (P-V) diagrams of the  $^{12}\text{CO}$  emission at every declination interval of  $0.25^\circ$ . The P-V diagrams of the  $^{13}\text{CO}$  emission are depicted in Figure B.2 in the Appendix. From Figures 6 and B.2, it can be seen that there is an apparent velocity gradient from north to south for the main cloud, which is represented by red in the panels. However, it can also be seen from the 3rd and 4th panels in the second row that there is a weak component at 6  $\text{km s}^{-1}$ , represented by the narrow white strips at the left side of the two panels. This 6  $\text{km s}^{-1}$  component is different from the main cloud in terms of the velocity gradient. This component also can be seen in other panels from  $-6^\circ$  to  $-7.75^\circ$ , although it has similar velocity to the main cloud in regions below  $\delta = -6.5^\circ$ , and therefore cannot be easily distinguished from the main cloud.

The 6  $\text{km s}^{-1}$  diffuse component is most likely the counterpart of the “Extended Component (EC)”, defined by Sakamoto et al. (1997). The EC has been fully observed by Nishimura et al. (2015) and they suggest that the EC has

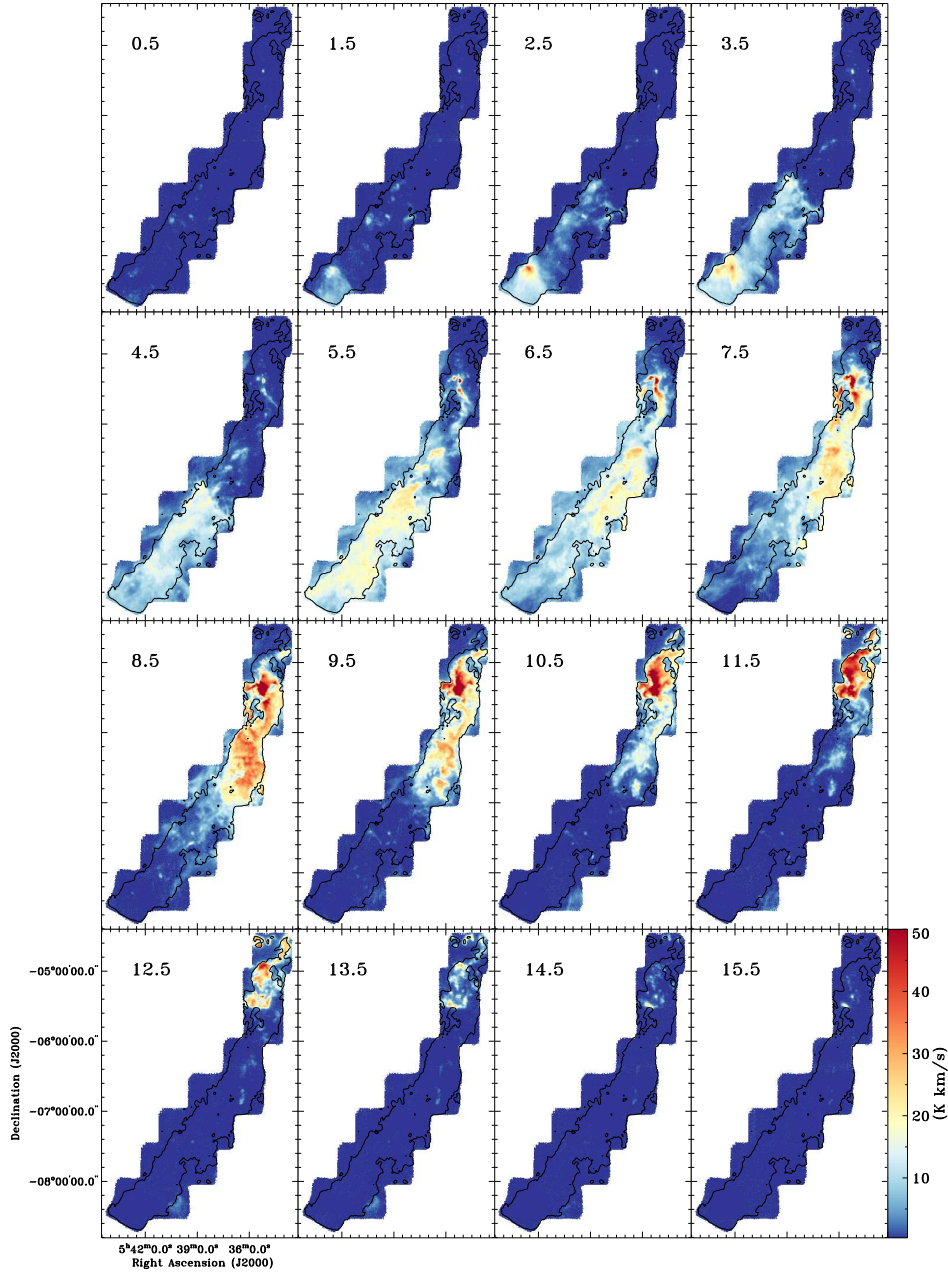
a typical velocity of  $\sim 6 \text{ km s}^{-1}$  and is widely distributed to the east of the main ridge of Orion A GMC. We present the histograms of the  $^{12}\text{CO}$  peak brightness temperature for the EC counterpart ( $N_{\text{H}_2} < 4 \times 10^{21} \text{ cm}^{-2}$ ), the main ridge ( $N_{\text{H}_2} > 4 \times 10^{21} \text{ cm}^{-2}$ ) and the entire observed region of Orion A GMC in Figure 7. The  $^{12}\text{CO}$  emission of the EC counterpart has peak temperatures in the range from 7 to 13 K, which accounts for the low-temperature excess in the histogram of the entire GMC.

## 3.4 N-PDFs in Sub-regions

### 3.4.1 Calculation of N-PDFs with star-formation activities

S15 have studied the column density distribution in Orion A using the *Herschel* observations of the dust emission. They referenced a joint protostar catalog that contains the PACS bright red sources (PBRS) (Stutz et al. 2013) and the Class 0, I and Flat-spectrum sources in the *Herschel* Orion Protostar Survey (HOPS) (Furlan et al. 2016) to divide the Orion A GMC into eight  $0.5^\circ \times 0.5^\circ$  sub-regions according to the protostar distribution. They found that the N-PDF of the hydrogen nucleus ( $N_{\text{H}}$ -PDF) derived from dust emission has a power-law distribution in each sub-region and the index of the power-law distribution varies with the number fraction of the Class 0 protostars. For direct comparison, we use the first seven sub-regions in S15 to calculate the  $N_{\text{H}}$ -PDFs except for sub-region 3 that is not fully covered by our observation. The seven sub-regions are indicated with squares in Figure 8(a) and their corresponding  $N_{\text{H}}$ -PDFs are presented in Figure 8(b). The physical parameters of each sub-region, such as the averaged  $\text{H}_2$  column density, excitation temperature, line width, LTE mass, number of young stellar objects (YSOs) and SFE, are listed in Table 1. In addition to the Class 0 and Class I catalog utilized by S15, we also included the disk dominated pre-main-sequence stars (Class II sources) from Megeath et al. (2012, 2016) to calculate the SFE in each sub-region. The Class II sources are marked with green dots in Figure 8(a).

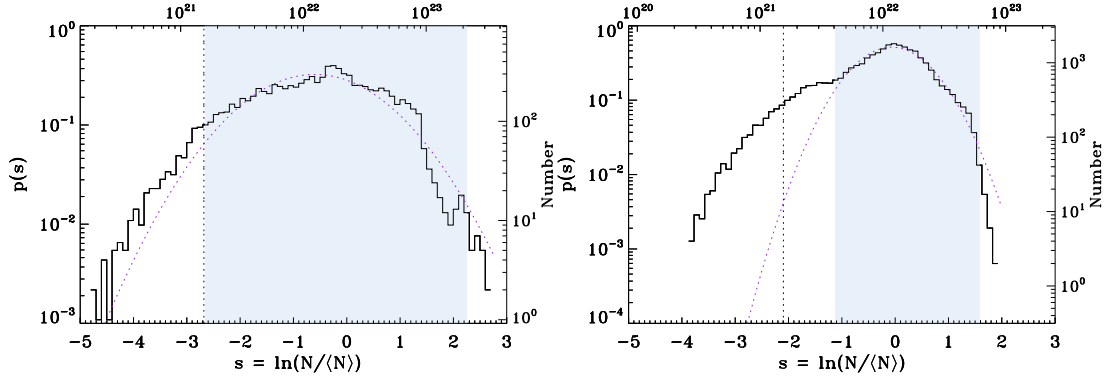
As demonstrated in Figure 8(b), although the  $N_{\text{H}}$ -PDFs of the sub-regions cannot be fitted well with lognormal or power-law functions, it can be ascertained that the width of the  $N_{\text{H}}$ -PDF gradually increases from south to north, which resembles the trend of the increasingly flattened power-law  $N_{\text{H}}$ -PDFs derived using the dust emission (fig. 2 in S15). However, unlike the dust-derived  $N_{\text{H}}$ -PDFs that can be fitted well by power-law distributions at the high density end, the gas-derived  $N_{\text{H}}$ -PDFs manifest quick decline at the high density end, but have relatively extended lognormal-like low-density tails. There



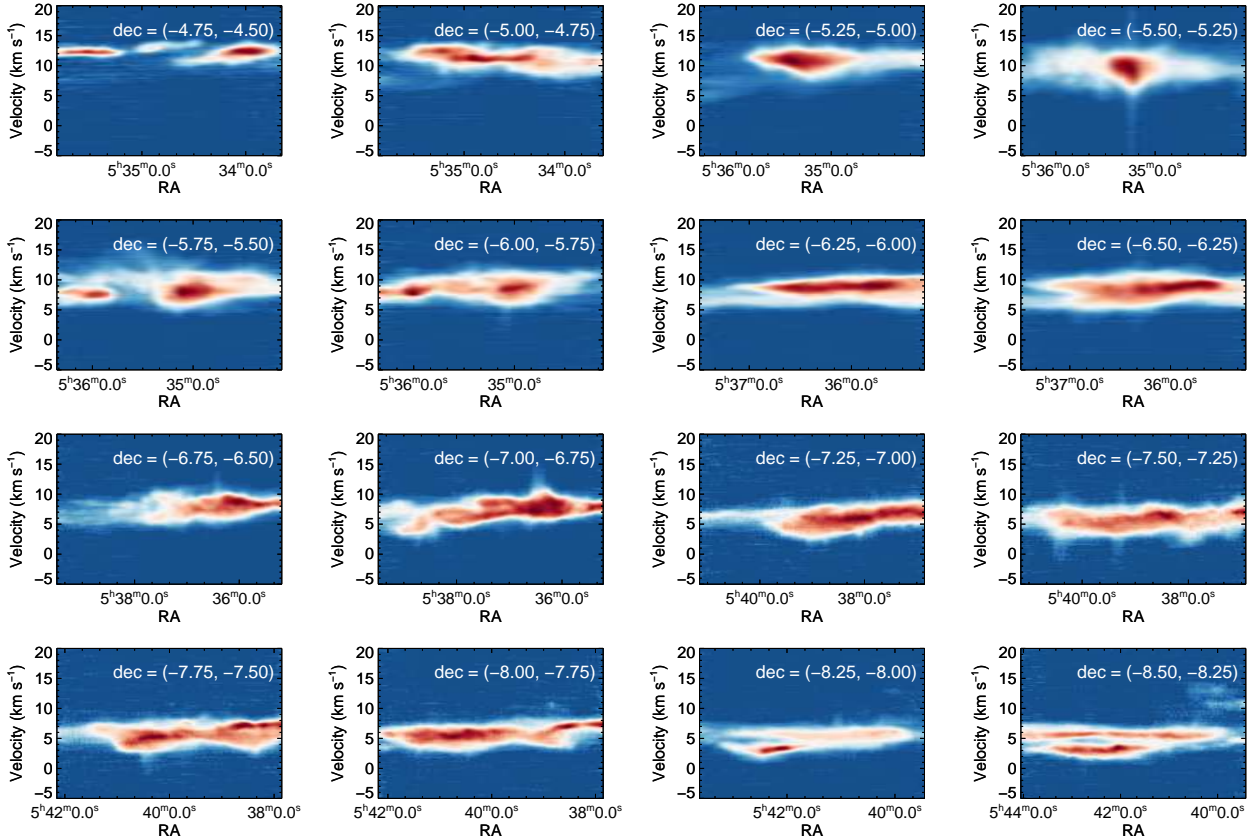
**Fig. 4** Channel maps of the  $^{12}\text{CO}$  emission with channel width of  $1 \text{ km s}^{-1}$  in the velocity range from 0 to  $16 \text{ km s}^{-1}$ . The colors start from  $1.5 \sigma_{\text{rms}}$ . The black contour in each panel corresponds to  $N_{\text{H}_2} = 4 \times 10^{21} \text{ cm}^{-2}$ . The central velocity of each panel is expressed in the upper-left corner of each panel.

is a trend of increasing column density from the south to the north sub-regions. The southernmost sub-regions 5 – 7 have median and maximum H column densities of  $2.5 \times 10^{22}$  and  $7.9 \times 10^{22} \text{ cm}^{-2}$ , respectively, which are a factor of about 1.5 lower than the northern sub-regions. As listed in the last column of Table 1, only  $\sim 70\%$  of the  $\text{H}_2$  mass is distributed at positions with  $\text{H}_2$  column density above  $1.25 \times 10^{22} \text{ cm}^{-2}$  in sub-regions 5 – 7, while this ratio is  $\sim 90\%$  in the northernmost three sub-regions. This difference in column density between the south and north

sub-regions may be in part caused by the different extents of CO depletion in these sub-regions. According to chemical evolutionary models of molecular clouds (Bergin et al. 1995), the gas-phase CO abundance is strongly affected by the depletion effect in cold ( $T_{\text{dust}} \sim 10 \text{ K}$ , even up to  $20 \text{ K}$ ), dense ( $n_{\text{H}_2} > 10^4 \text{ cm}^{-3}$ ) and well-shielded ( $A_v \sim 10 \text{ mag}$ , corresponds to  $N_{\text{H}_2} = 9.4 \times 10^{21} \text{ cm}^{-2}$ ) (Bohlin et al. 1978) regions of molecular clouds, and it is dominated by thermal evaporation in regions with dust temperatures higher than  $22 \text{ K}$ . It can be seen from Table 1 that the



**Fig. 5** N-PDFs of the two parts of Orion A GMC divided by the declination of  $\delta = -5^{\circ}57'00''$ , overlaid with the fitted lognormal functions as indicated in *purple dashed lines*. The fitting range in each panel is indicated with a *light blue shadow*.



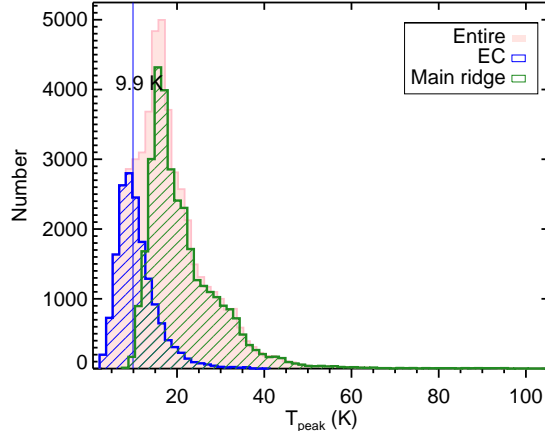
**Fig. 6** P-V diagrams of the  $^{12}\text{CO}$  emission from declination of  $-4.5^{\circ}$  to  $-8.5^{\circ}$  in steps of  $0.25^{\circ}$ . The colors indicate the integrated intensity in units of K arcdeg from  $2\sigma$  to the maximum in each panel. The declination interval of each panel is shown in white in the upper-right corner.

dust temperatures in the three southern sub-regions are less than 17 K, indicating that the southern sub-regions are significantly colder than the northern sub-regions. Ripple et al. (2013) have investigated the relationship between the  $^{13}\text{CO}$  column density and the extinction in Orion A, and found that the  $^{13}\text{CO}$  column density in the southern portion of the GMC, which contains sub-regions 5 – 7 and part of sub-region 4 in this work, no longer increases with

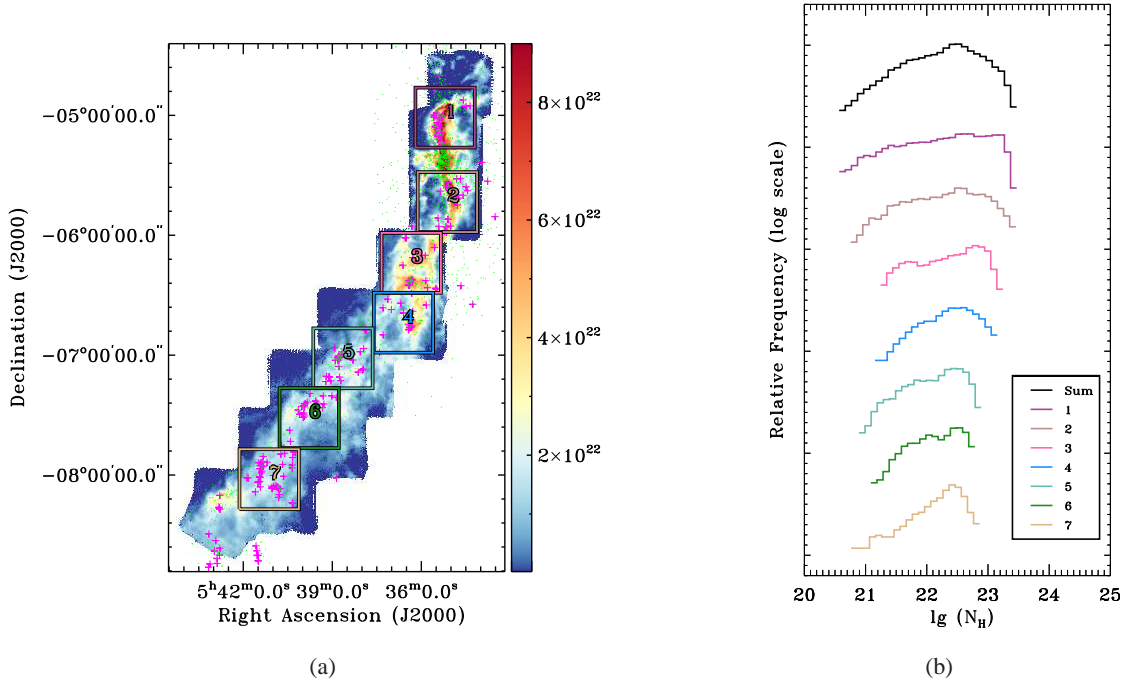
extinction when  $A_v \sim 10$  mag. Compared with sub-regions 1 – 4, the lack of high column density gas in sub-regions 5 – 7 is consistent with the scenario that the  $^{13}\text{CO}$  abundance is reduced by depletion in the cold and well-shielded southern sub-regions.

Whether an N-PDF is intrinsically a lognormal distribution can be tested with the relationship  $\mu_s = -\sigma_s^2/2$  resulting from the normalization of the column density





**Fig. 7** Histograms of the  $^{12}\text{CO}$  peak brightness temperature of the EC counterpart (*blue*), the main ridge (*green*) and the entire observed region (*pink*) of Orion A GMC. The *blue* vertical line and the *black* number on that line signify the median temperature of the EC counterpart.



**Fig. 8** (a)  $\text{H}_2$  column density map overlaid with sub-regions 1 – 7 in S15. The number of each sub-region is indicated in the upper-right corner of the squares. The *magenta pluses* and the *green dots* mark the positions of the protostars used in S15, and the disk dominated pre-main-sequence stars from the Spitzer catalog (Megeath et al. 2012, 2016), respectively. (b) Hydrogen nucleus  $N_{\text{H}}(2N_{\text{H}_2})$ -PDFs of sub-regions 1 – 7 and the summed N-PDF of all the sub-regions.

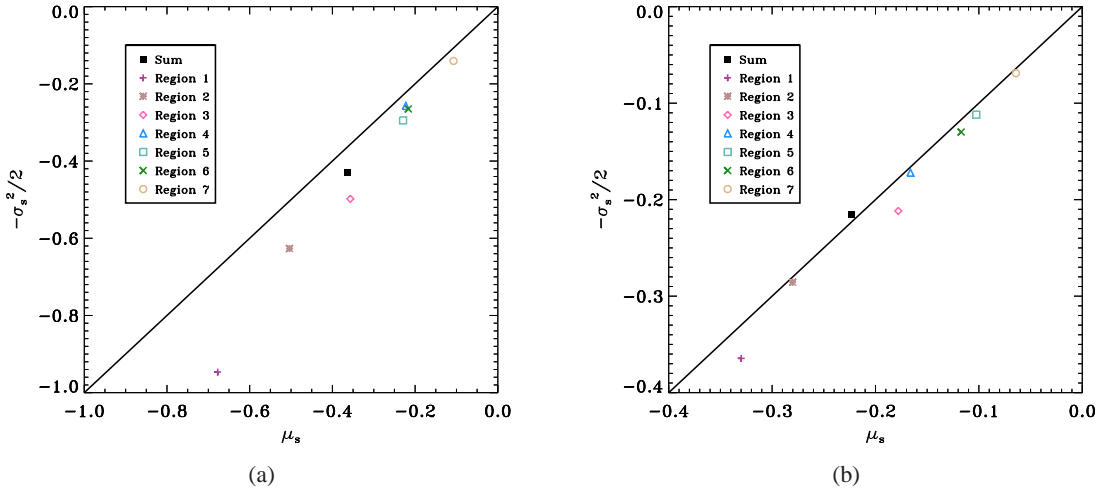
(Goodman et al. 2009a) (see details in the Appendix). The relationship between the mean and dispersion of the normalized logarithmic column densities of sub-regions 1 – 7 is exhibited in Figure 9(a). The diagonal in Figure 9 represents the relationship  $\mu_s = -\sigma_s^2/2$  and intrinsic log-normal distributions should fall on this line. As shown in Figure 9(a), the N-PDFs of the sub-regions more or less deviate from the mean-dispersion relationship for lognor-

mal functions, and the N-PDFs of the southern sub-regions are closer to the line than the northern sub-regions. As discussed in Section 3.3.1, the low-density excess in the N-PDF of the GMC probably originates from the EC counterpart of the Orion A GMC. The  $\mu_s - \sigma_s$  relationship when the low-density part is excluded shows that the N-PDFs of all sub-regions are distributed much closer to the lognor-

**Table 1** Physical Parameters of Each Sub-region

Region	$\overline{N_{\text{H}_2}}$ ( $\times 10^{22} \text{ cm}^{-2}$ )	$\mu_s$	$\sigma_s$	$T_{\text{ex}}$ (K)	$T_{\text{dust}}$ (K)	$\sigma_v$ ( $\text{km s}^{-1}$ )	$M_{\text{LTE}}$ ( $M_{\odot}$ )	$n'_{\text{YSO}}$	$n_{\text{YSO}}$	SFE	Mass Fraction
(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)	(11)	(12)
1	2.6	-0.33	0.85	29.5	27.3	0.83	5638	44	420	3.59%	92.38%
2	2.0	-0.28	0.76	24.7	23.0	1.03	5583	25	408	3.52%	88.14%
3	2.4	-0.18	0.65	29.2	18.2	1.07	6967	22	166	1.18%	92.58%
4	1.8	-0.17	0.59	25.2	17.8	0.94	5265	17	74	0.70%	83.34%
5	1.2	-0.10	0.47	20.4	16.4	0.99	3265	31	127	1.91%	68.93%
6	1.2	-0.12	0.51	18.1	15.4	0.96	3444	26	98	1.40%	72.14%
7	1.3	-0.06	0.37	19.4	15.0	0.83	3634	48	125	1.69%	66.97%

Notes: Columns (2)–(4) list the average  $\text{H}_2$  column density, and the mean and dispersion of the natural logarithm of the normalized  $\text{H}_2$  column density ( $N_{\text{H}_2} > 4 \times 10^{21} \text{ cm}^{-2}$ ) of each sub-region respectively. Columns (5)–(8) express the median excitation temperature, median dust temperature from the *Herschel-Planck* temperature map (Lombardi et al. 2014), median velocity dispersion of the  $^{13}\text{CO}$  emission and the LTE mass of each sub-region respectively. The last four columns give the total number of protostars (Class 0, I and Flat-spectrum sources), the total number of all YSOs (protostars and Class II sources), the SFE and the dense gas ( $N_{\text{H}_2} > 1.25 \times 10^{22} \text{ cm}^{-2}$ ) mass fraction of each sub-region. Information on the protostars is from the PBRs and HOPS catalogs (Stutz et al. 2013; Furlan et al. 2016), while information on Class II sources is from the Spitzer catalog (Megeath et al. 2012, 2016). The numbers of protostars and YSOs are counted within the boundaries of each sub-region, which are the boxes in Fig. 8. The SFE is derived using the assumption that the average YSO mass is  $0.5 M_{\odot}$ .



**Fig. 9** (a) Relationship between the mean and dispersion of the logarithmic normalized column densities in the sub-regions and (b) the same relationship but excluding the positions where  $N_{\text{H}_2}$  is lower than  $4 \times 10^{21} \text{ cm}^{-2}$ . The *solid diagonal* in each panel represents the relation  $\mu_s = -\sigma_s^2/2$ .

mal line (Fig. 9(b)), suggesting intrinsic lognormal distributions of the  $\text{H}_2$  column density in these sub-regions.

### 3.4.2 The evolutionary trend of the N-PDF

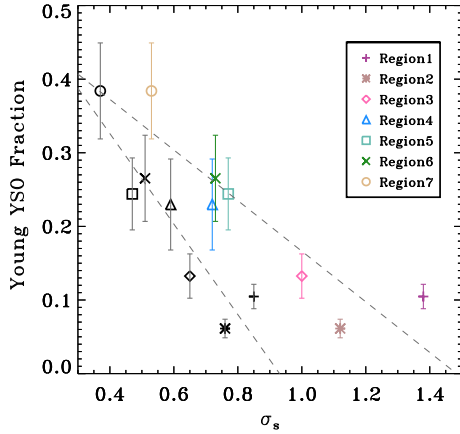
In Table 1, we summarize the total number of YSOs and total number of protostars (Class 0, I and the Flat-spectrum sources) in each sub-region. The protostars are at an earlier evolutionary stage than the Class II YSOs (Dunham et al. 2014). Figure 10(a) shows the relationship between the protostar fraction and  $\sigma_s$  for the sub-regions. If we assume that the Orion A GMC is undergoing star formation with a constant star formation rate, the fraction of protostars is related to the evolutionary status of the molecular cloud. Higher protostar fraction indicates an earlier evolutionary stage. Figure 10(a) demonstrates that the proto-

star fraction is anti-correlated with  $\sigma_s$ , indicating that the column density structure of the molecular clouds in the Orion A region is coupled with the evolutionary stages of star formation, with such a trend that a later evolutionary stage corresponds to a broader column density dispersion.

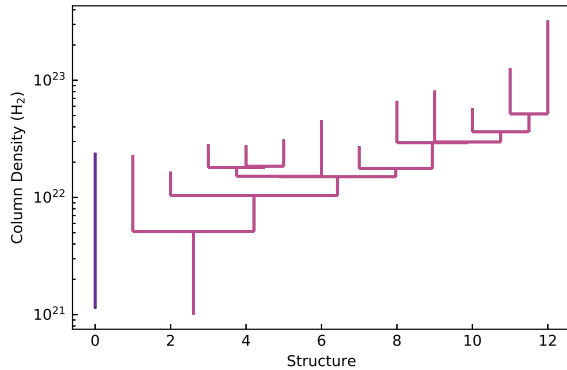
## 4 HIERARCHICAL COLUMN DENSITY STRUCTURE

### 4.1 Hierarchical “Tree” and the Importance of Self-gravity on Different Spatial Scales

The dendrogram of the tree structure for the Orion A GMC is illustrated in Figure 11. The observed region contains two “trunk” structures, as visible in Figure 11. The right trunk is the main cloud, while the left trunk is the small cloud in the top-left corner of Figure 3(a). To investigate



**Fig. 10** Relation between the dispersion of the natural logarithmic normalized  $H_2$  column density,  $\sigma_s$  and the fraction of protostars across the sub-regions. The *color* and *black* symbols distinguish between the two cases where the calculation of  $\sigma_s$  includes (*color*) and does not include (*black*) the positions of  $N_{H_2} < 4 \times 10^{21} \text{ cm}^{-2}$ . The *dashed lines* trace the linear fit to the data points. The Pearson correlation coefficient between  $\sigma_s$  and the protostar fraction is  $-0.90$  (*color*) and  $-0.93$  (*black*).



**Fig. 11** Resulting “tree” generated from the DENDROGRAM algorithm, where the values of the  $x$  axis have no physical meaning, and different colors correspond to separate “trunk” structures of the “tree.”

the properties of structures at various scales, we only use the right trunk in the following analysis. There are 23 individual structures in the right trunk, among which twelve are “leaves”, ten are “branches”, and one is the trunk itself. The sizes of the leaves span a large range and there is no favorable scale for the leaf structure. The leaves contain both large filaments and small clumps. The “genealogy” diagrams of the spatial distribution of all the structures are plotted in Figure 12. As displayed in Figure 12, the ridge of the Orion A GMC is composed of two main structures, branch 11 that contains the entire ISF and the L1641 N regions, and branch 5 that contains the southern tail of Orion A GMC. Comparatively, the density structures are richer in the northern branch than in the southern

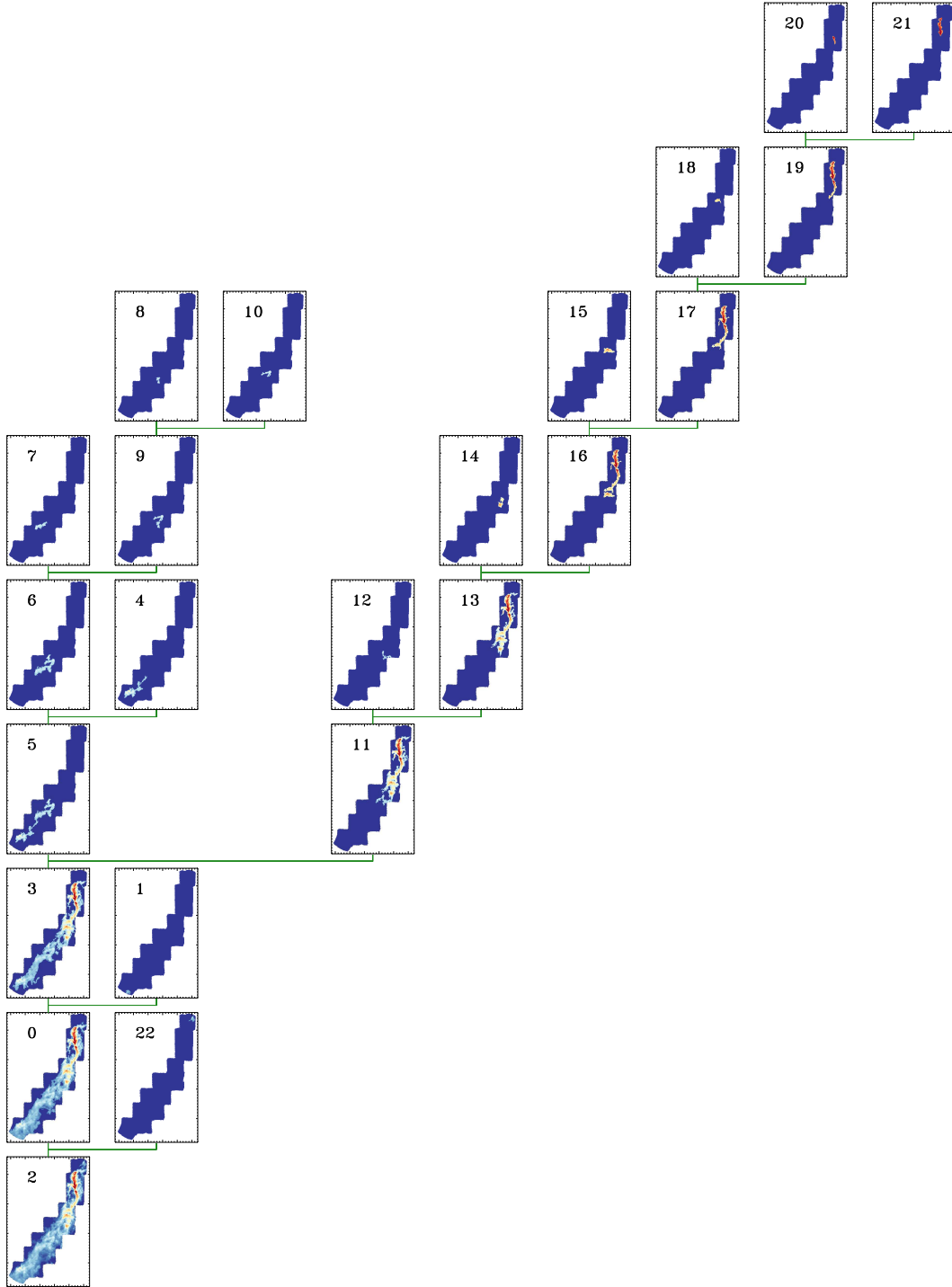
branch, and there are more levels in branch 11 than branch 5. Downward from branch 3, the northern and southern structures of the GMC merge into one cloud.

The significance of self-gravity for the dynamics of dense cores on scales of  $\sim 0.1$  pc is well-known (Larson 2003; di Francesco et al. 2007). However, turbulent simulations without self-gravity successfully yield density and velocity distributions of molecular clouds that resemble observations (Vázquez-Semadeni & García 2001; Padoan & Nordlund 2002; Federrath et al. 2009). Goodman et al. (2009b) have made a “dendrogram” analysis of the L 1448 cloud using  $^{13}\text{CO}$  observations and found that self-gravity is important on the full range of scales of the structures in that cloud, from subparsec to  $\sim 1$  pc. We present the genealogy diagram of the derived virial parameters and N-PDFs of the structures identified in this work in Figure 13. The panels in Figure 13 that correspond to gravitationally bound structures are filled with light blue. Except for leaf 1 that corresponds to a clump at the southernmost end of the GMC, all structures, on scales from 0.3 pc (leaf 20) to 4.3 pc (trunk 2), are gravitationally bound. This result suggests that self-gravity is also important on much larger scales, i.e., on the clump- to cloud- scales. Our result is consistent with the results of Goodman et al. (2009b) and further highlights the necessity of including self-gravity in simulations of molecular clouds on pc scales.

## 4.2 Properties of N-PDFs on Different Spatial Scales

The N-PDFs of the dendrogram structures depicted in Figure 13 are uniformly normalized by the mean column density of the Orion A GMC, which is  $1.5 \times 10^{22} \text{ cm}^{-2}$ . We have performed lognormal or power-law fittings on the N-PDFs as appropriate. The results are indicated with dotted and dashed lines in Figure 13 respectively. We note that for most of the dendrogram structures in Figure 13, the adopted uniform mean column density for the normalization of N-PDF is lower than the actual mean column density of the individual structures, which translates the N-PDFs shown in Figure 13 to the right along the  $\ln N / \langle N \rangle$  axis and therefore increases the value of the fitted  $\mu$  parameter. Due to this reason, most of the fitted  $\mu$  parameters have positive values.

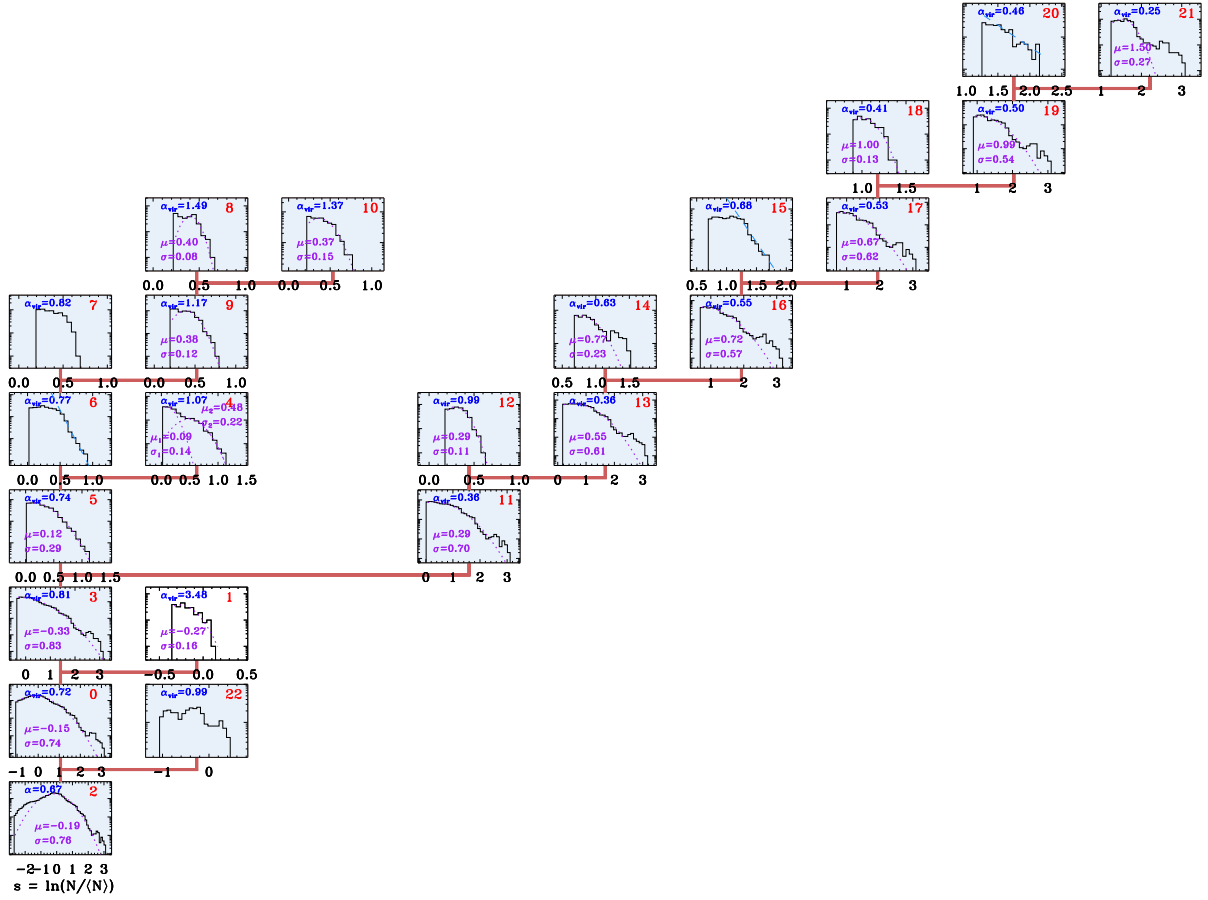
The leaves of branch 11 can be divided into three categories, leaves 18 and 12 with pure lognormal N-PDFs, leaves 21 and 14 that have lognormal N-PDFs with high-density excesses, and leaves 20 and 15 that have power-law N-PDFs at the high-density end. As displayed in Figure 12, leaf 18 is located at the south of the ISF structure, and corresponds to the center of sub-region 3 in Section 3.4. A relatively low number of protostars are associated with leaf 18, indicating inactive star formation within leaf 18. Leaf



**Fig. 12** “Genealogy” diagram of the sub-structures in the dendrogram in Fig. 11 and their spatial distribution. The number in each panel is the index of the structure in the dendrogram. The *green line* illustrates the relationship between the structures.

12 is a relatively faint filament located at the southernmost end of branch 11, and this filament is also quiescent in star formation as indicated by the few associated Class II YSOs in Figure 8. Leaves 21 and 14 correspond to the OMC-1/2/3 regions, which contain a cluster of intermediate-mass protostars and the NGC 1999 region. The high-density ex-

cesses in leaves 21 and 14 are concentrated in regions with  $s \sim 2.3 - 3.2$  ( $N_{\text{H}_2} \sim 1.5 - 3.7 \times 10^{23} \text{ cm}^{-2}$ ) and  $s \sim 1.2 - 1.5$  ( $N_{\text{H}_2} \sim 5.0 - 6.7 \times 10^{22} \text{ cm}^{-2}$ ), respectively. The high-density regions account for 12.8% of the mass and 4.2% of the area for leaf 21. For leaf 14, the high-density mass and area fractions are 23.7% and 16.6%, respectively. Leaves



**Fig. 13** Same configuration as Fig. 12, but with N-PDF rather than the spatial distribution of each structure being presented in each panel. The lognormal and power-law fit to the N-PDFs are indicated with the *purple dotted line* and the *blue dashed line*, respectively. The fitted lognormal parameters are expressed in each panel. The virial parameter of each structure is written in the upper-left corner in each panel. The panels corresponding to structures with  $\alpha < 2$  are filled with *light blue*.

20 and 15 correspond to OMC-4, which includes a dense star-forming region and the HII region L 1641 N. Leaf 20 is possibly at a later evolutionary stage than leaf 21, as indicated by the pure power-law PDF and the lower protostar fraction as discussed in Section 3.4.2. The N-PDFs of branches 19, 17, 16, 13 and 11 can be well-fitted with lognormal functions below  $s = 2.3$ . The high-density excesses in the N-PDFs of these branches are caused by the pixels with density above  $N_{\text{H}_2} \sim 1.5 \times 10^{23} \text{ cm}^{-2}$  which is confined to the Orion KL region in leaf 21 and is highlighted with the white contour in Figure 3(a). The high-density pixels with  $s > 2.3$  only account for a small mass and area proportion of the branch N-PDFs below leaf 21. The mass proportion decreases from 12.8% of leaf 21 to 2.6% of trunk 2, while the corresponding area proportion decreases from 4.2% to 0.2%. Therefore, the majority of the structures of branch 11 are dominated by lognormal N-PDFs and departures from lognormal N-PDFs at high-densities only occur in active star-forming regions.

Except for leaf 7 that corresponds to the HII region L 1641 S, all leaves in branch 5 have lognormal N-PDFs without high-density excesses. The N-PDF of leaf 4 is fitted well with double lognormal functions, indicating the possible existence of mixed components along the line-of-sight. We can see from the last two panels in Figure 6 that there are two separate velocity components at the location of leaf 4, one of which is in the range from 5 to 8  $\text{km s}^{-1}$ , the same as the EC counterpart. However, it is most likely that the velocity separation in the leaf 4 region is a local dynamical property and not caused by the EC gas. The N-PDFs of branches 9 and 5 are fitted with lognormal functions, while the N-PDF of branch 6 that contains the HII region L 1641 S is fitted with a power-law at its high density tail.

Generally, the  $N_{\text{H}_2}$  dynamical ranges of the structures above branch 5 are smaller than those of the structures above branch 11. From leaf 21 to branch 11, the  $\mu$  of the fitted lognormal function decreases from  $\sim 1.5$  to  $\sim 0.3$ , and

the  $\sigma_s$  increases from  $\sim 0.3$  to  $\sim 0.70$ . From leaf 8 to branch 5, the  $\mu$  and  $\sigma_s$  of the fitted lognormal functions vary gradually from  $\sim 0.4$  to  $\sim 0.1$  and  $\sim 0.1$  to  $\sim 0.3$ , respectively. The ranges of  $\mu$  and  $\sigma_s$  of structures in branch 5 are much smaller than those in branch 11, indicating the southern filament (branch 5) of the Orion A GMC is at an earlier evolutionary stage than the northern filament (branch 11), which is consistent with the results in Section 3.4. We also plot the fitted lognormal N-PDFs of branches 5 and 11, and their summation in Figure 3. The N-PDFs of the two filaments account for the high-density part of the column density distribution of Orion A, supporting that the Orion A molecular cloud is mainly composed of these two filaments.

Below branches 11 and 5, there are two leaves and three branches. Leaves 1 and 22 correspond to a southernmost and a northernmost clump, respectively, both inactive in terms of star formation. The N-PDF of leaf 1 is fitted with a lognormal function while the N-PDF of leaf 22 has an irregular shape. Branch 3 is mainly the combination of filaments 5 and 11, and is approximately the main ridge of the Orion A GMC. The N-PDFs of branches 3, 0 and 2 are fitted with lognormal functions and getting closer to the overall N-PDF of the whole cloud successively. The high-density excesses in the N-PDFs of these three branches are caused by leaf 21, while the low-density excess of branch 2 is caused by the EC gas, as discussed in Section 3.3.2.

In summary, regardless if the sub-structure is in the northern or southern part of the GMC, power-laws and deviations from lognormal distributions at the high-density tail of N-PDFs only exist in active star-forming regions. The majority of the structures in Orion A GMC have lognormally dominated N-PDFs on scales from  $R \sim 0.4$  to 4 pc. The predominant existence of lognormal N-PDFs in structures on such a broad range of scales suggests a dominant role of turbulence on these spatial scales.

## 5 SUMMARY AND CONCLUSIONS

We have conducted a large-field survey of  $^{12}\text{CO}$ ,  $^{13}\text{CO}$  and  $\text{C}^{18}\text{O } J = 1 - 0$  emission toward the Orion A GMC with a sky coverage of  $\sim 4.4 \text{ deg}^2$ . Using the  $^{12}\text{CO}$  and  $^{13}\text{CO}$  data, we have investigated the N-PDFs of  $\text{H}_2$  column density of the GMC and compared the  $N_{\text{H}}$ -PDFs with previous results from *Herschel* observations in seven sub-regions. The importance of self-gravity and properties of N-PDFs on different spatial scales are studied using the DENDROGRAM method. The main results are summarized as follows.

1. The  $\text{H}_2$  column density N-PDF for the entire GMC is fitted with a lognormal function in the range from

$\sim 4 \times 10^{21}$  to  $\sim 1.5 \times 10^{23} \text{ cm}^{-2}$ , with excesses at both the low-density and high-density ends. The excess at the high-density end corresponds to the Orion KL region, and the excess at the low-density end is possibly caused by an extended and low-temperature component ( $\sim 10 \text{ K}$ ) with velocities in the range of  $5 - 8 \text{ km s}^{-1}$ .

2. To compare with the results from *Herschel* observations, we divided the Orion A GMC into seven sub-regions. The N-PDFs of the sub-regions are irregular in shape, but are lognormally distributed at the high column density end. Compared with the northern sub-regions, the three southern sub-regions have less high-density gas, which may be in part caused by the effect of CO depletion. The  $\text{H}_2$  column density structure is coupled with the evolutionary stage of clouds in Orion A GMC. Broader column density dispersions correspond to later evolutionary stages.
3. In terms of structure hierarchy, Orion A GMC is mainly composed of two filamentary structures located in the north and south, respectively. All the structures in the dendrogram tree except leaf 1 are gravitationally bound across spatial scales from 0.3 to 4.3 pc. Although power-laws and departures from lognormal distributions exist in N-PDFs of structures in five active star-forming regions mostly with scales  $< 0.6 \text{ pc}$ , the N-PDFs of structures in the Orion A GMC are predominantly lognormal on scales from  $R \sim 0.4$  to 4 pc.

**Acknowledgements** We thank the PMO-13.7m telescope staffs for their supports during the observation. The MWISP project is supported by National Key R&D Program of China (2017YFA0402701) and Key Research Program of Frontier Sciences of CAS (QYZDJ-SSW-SLH047). Y. Ma acknowledges supports by the National Natural Science Foundation of China (Grant Nos. 11503086 and 11503087). This work makes use of the SIMBAD database, operated at CDS, Strasbourg, France.

## Appendix A: THE RELATIONSHIP BETWEEN THE MEAN AND DISPERSION OF THE LOGARITHMIC NORMALIZED COLUMN DENSITY

From the definition of the lognormal distribution introduced in Equation (5) in Section 3.3, the mathematical expectation of  $N$  is

$$\begin{aligned} E(N) &= \int_0^{+\infty} N f(N) dN \\ &= \int_0^{+\infty} \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(\ln N - \mu)^2}{2\sigma^2}} dN, \end{aligned} \quad (\text{A.1})$$

where  $N$ ,  $\sigma$  and  $\mu$  have the same meaning as in Equation (5). If we let  $t = (\ln N - \mu)/(\sqrt{2}\sigma)$ , then  $N = \exp(\sqrt{2}\sigma t + \mu)$  and  $dN = \sqrt{2}\sigma \exp(\sqrt{2}\sigma t + \mu) dt$ . The expectation can be written as

$$\begin{aligned} E(N) &= \int_{-\infty}^{+\infty} \frac{1}{\sqrt{\pi}} e^{-t^2 + \sqrt{2}\sigma t + \mu} dt \\ &= \frac{1}{\sqrt{\pi}} \int_{-\infty}^{+\infty} e^{-(t - \frac{\sqrt{2}}{2}\sigma)^2 + \mu + \frac{\sigma^2}{2}} dt. \end{aligned} \quad (\text{A.2})$$

Again, after substituting  $u = t - \sqrt{2}/2\sigma$  and utilizing the integral formula  $\int_{-\infty}^{+\infty} e^{ax^2} dx = \sqrt{\pi/a}$ , the above equation is finally converted to

$$E(N) = \frac{1}{\sqrt{\pi}} e^{\mu + \frac{\sigma^2}{2}} \int_{-\infty}^{+\infty} e^{-u^2} du = e^{\mu + \frac{\sigma^2}{2}}. \quad (\text{A.3})$$

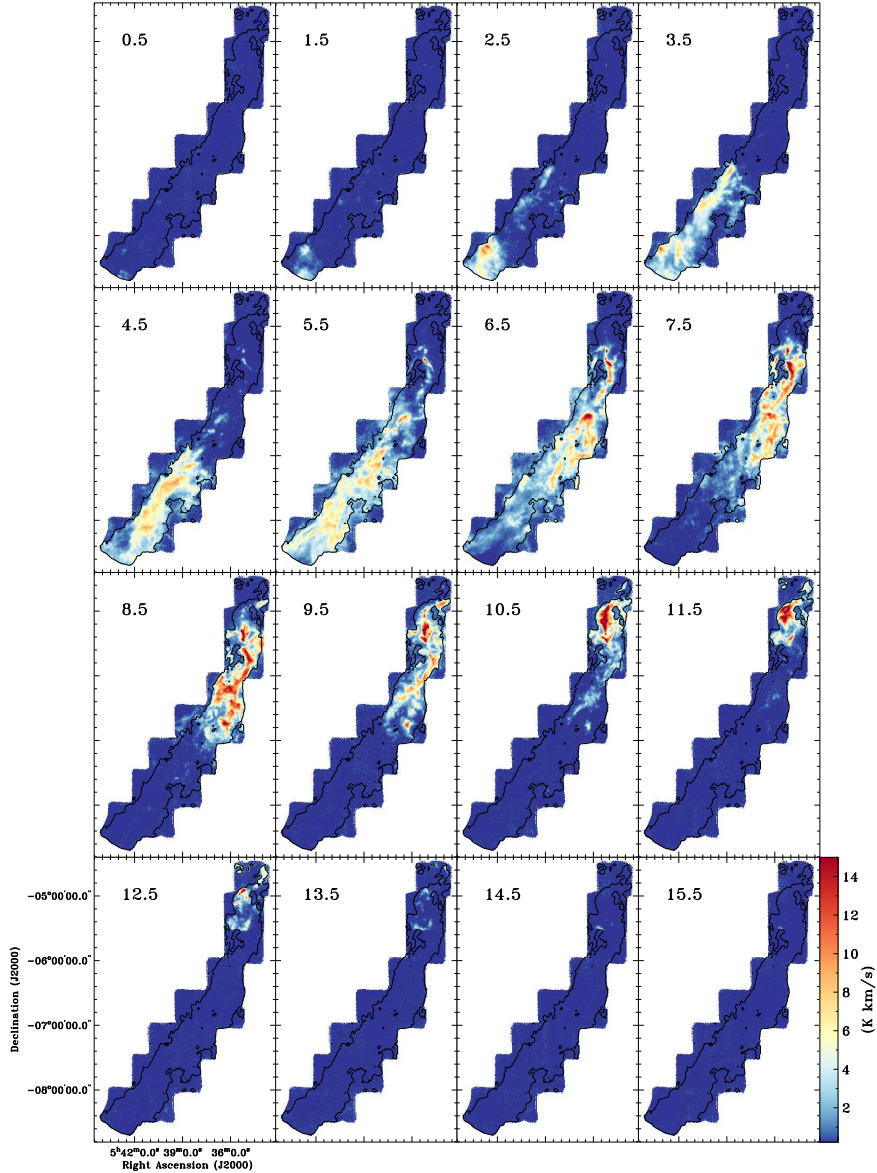
Because of the normalization when calculating the N-PDF in this work, the mathematical expectation of  $N$  should be unity which means  $\mu + \sigma^2/2 = 0$ , i.e.,  $\mu = -\sigma^2/2$ .

## Appendix B: FIGURES

We present the velocity channel maps, P-V diagrams of the  $^{13}\text{CO } J = 1 - 0$  emission in Figures B.1 and B.2, respectively.

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**Fig. B.1** Same as Fig. 4 but for the  $^{13}\text{CO}$  emission.

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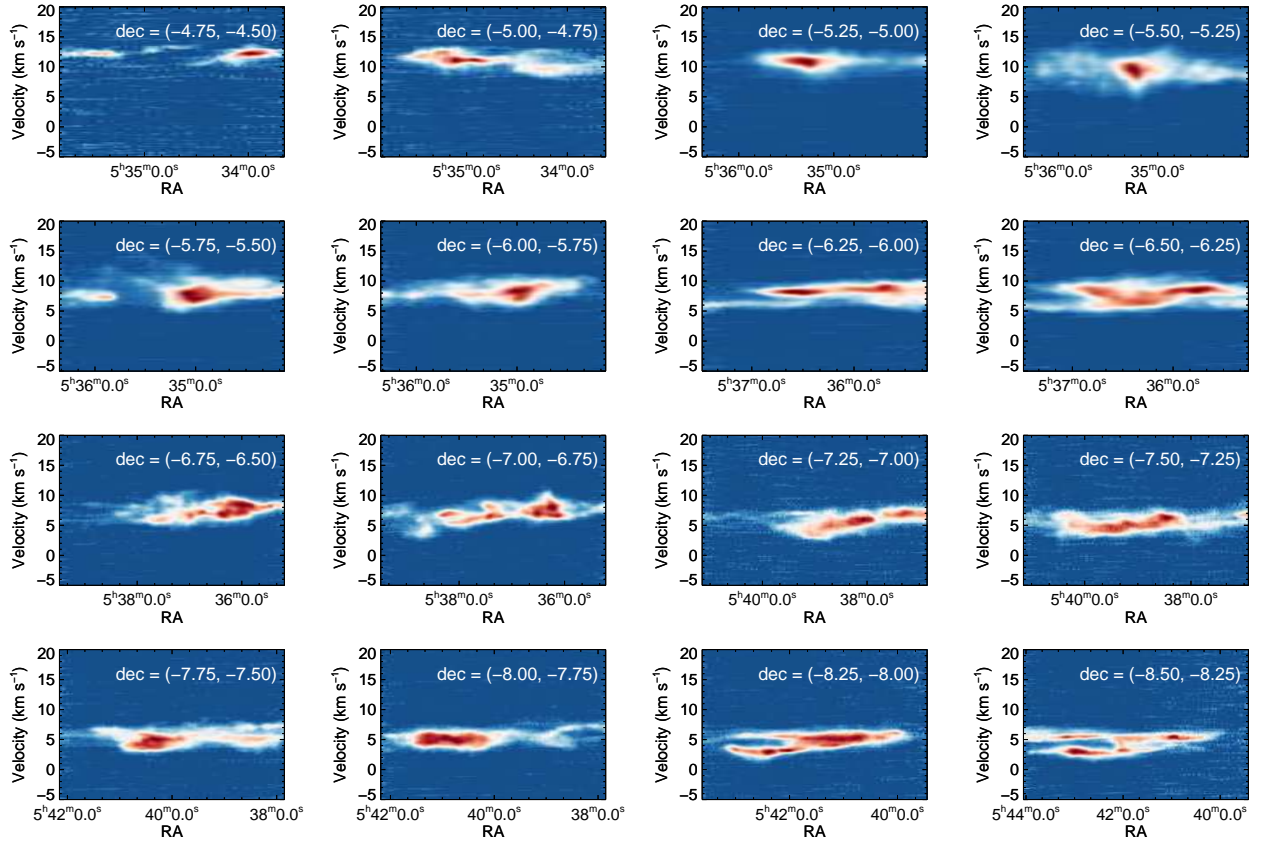
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**Fig. B.2** Same as Fig. 6 but for the  $^{13}\text{CO}$  emission.