

Studying dynamical models of the core galaxy NGC 1399 with merging remnants

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Abstract An investigation on the possible dynamical models of the core galaxy NGC 1399 is performed. Because early-type galaxies are likely to be formed through merging events, remnant rings are considered in the modeling process. A numerical survey over three parameters is employed to obtain the best-fit models that are completely consistent with observations. It is found that the inner slope of the dark matter profile is cuspy for this core galaxy. The existence of remnant rings in best-fit models indicates a merging history. The remnant ring explains the flattened surface brightness and thus could be the physical counterpart of the core structure of NGC 1399.

Key words: galaxies: kinematics and dynamics — galaxies: elliptical and lenticular, cD — galaxies: formation

1 INTRODUCTION

NGC 1399 is a giant elliptical galaxy located near the center of the Fornax cluster. According to Dullo & Graham (2014), it is classified as a core galaxy with a core radius of 202 pc. As cosmological N-body simulations showed that the density profiles of dark matter halos can be approximated by a centrally cuspy function, i.e. a Navarro-Frenk-White (NFW) profile (Navarro et al. 1997), it is not clear why some early-type galaxies such as NGC 1399 could have a central core.

The most popular scenario to form a core is through the gravitational sling-shot ejections of stars (Milosavljević & Merritt 2001, Merritt 2006) by the inspiralling binary super-massive black hole (SMBH) near the center during merging processes of galaxies. If this does occur, as the dark matter particles also experience gravitational sling-shot ejections, it is likely that the galactic central dark matter distribution will get changed. Further, because the masses of stars and dark matter particles are different, the luminous and dark parts of galaxies shall settle to different distributions in the end. Thus, it is very important to relax the usual assumption that

“mass traces light” and investigate the dark matter profiles near the centers of galaxies through dynamical modeling.

On the other hand, there are still problems for this sling-shot scenario of core formation. Because each merger can only deplete about 0.5 SMBH mass from the center (Merritt 2006), a larger number of mergers is needed for those giant galaxies with big cores. For NGC 1399, the data in table 4 of Dullo & Graham (2014) imply that there should be about 16 mergers if the core was formed through the sling-shot scenario. However, according to the estimations by Conselice et al. (2008), it is unlikely that a galaxy would experience more than five mergers. In addition, investigating the properties of mergers makes Khochfar & Burkert (2005) and Naab et al. (2006) claim that mergers could lead to slowly rotating boxy remnants. A boxy remnant could become the main part of a newly formed giant elliptical galaxy. The slow rotation implies that some part of the remnant owns a certain amount of angular momentum and it is possible that this part might become a disk remnant ring hidden in the galaxy. This remnant ring could contribute to the surface brightness of a core structure.

Therefore, this motivates us to study whether a model containing a stellar remnant ring could fit the observational constraints well. That is, in this paper, we will investigate the existence of dynamical models which include both the main stellar part and the remnant stellar part. The main stellar part is assumed to be spherically distributed and the remnant could be a ring-like structure, which is located on the orbital plane of the inspiralling binary SMBH during the merging of galaxies.

As for previous work, Saglia et al. (2000) presented a detailed study on the mass distributions of NGC 1399. Since then, previous studies about NGC 1399 focused on either dynamical structure of the outskirts or mass measurement of the central SMBH. For example, employing planetary nebula data, Napolitano et al. (2002) studied the velocity structures of outer regions of NGC 1399 and concluded that the interactions from nearby galaxies are important. In addition, Schuberth et al. (2010) and Samurović (2016) also addressed the dynamics of outer parts through the kinematic data of globular clusters. Schulz et al. (2016) even estimated the star formation rates of NGC 1399 from the ages of globular clusters. Samurović & Danziger (2006) established the total dynamical mass of NGC 1399 through both studies in X-rays and kinematics of globular clusters. Moreover, focusing on the very central region of NGC 1399, Houghton et al. (2006) and Gebhardt et al. (2007) provided precise estimations of the SMBH mass.

In addition to employing Jeans equations as in Samurović (2016), to construct a model of early-type galaxies, the orbit-based method (Schwarzschild 1979, 1993) is often used. The superposition of orbits with different weights in a fixed galactic potential is employed to build theoretical models which could fit the observed brightness profiles and kinematic data. This method has been widely used in many papers such as Rix et al. (1997) and van der Marel et al. (1998). On the other hand, Syer & Tremaine (1996) proposed a particle-based method in which the weights of particles could be changed when these particles were proceeding along their fixed orbits; see the discussions about these methods in McMillan & Binney (2012).

Because the main goal of our work here is to investigate the dark matter density profile of core galaxy NGC 1399 and study the existence of an associated stellar remnant ring, in order to explore possible profiles of both luminous and dark matter within the framework of standard dynamical systems and have the freedom to

consider the possible stellar remnant ring, different from Schwarzschild (1979) and Syer & Tremaine (1996), the usual particle-based dynamical simulations will be used here. In fact, N-body simulations were used to construct models of globular clusters (Baumgardt 2017). However, for galaxies, many more particles will be needed and it would be very difficult to tune model parameters to fit observational data if expensive N-body simulations are employed. The model in Kandrup et al. (2003) gives an excellent example using fixed galactic total potential such that N-body test-particle simulations can lead to stellar structures that fit with observations well.

In this paper, we set the total galactic potential to be fixed and use N-body particles to represent the stellar part. With reasonable choices of initial conditions for stellar particles, the theoretical surface brightness and velocity dispersion can be obtained when these particles approach a quasi-equilibrium. The model results will be compared with observational data. In order to consider the possible merging remnants, further stellar particles will be added in models in a way to improve the fitting with observational surface brightness and velocity dispersion.

The principal procedure of seeking an equilibrium through an N-body dynamical system is described in Section 2. The model details are in Section 3 and the results are in Section 4. Concluding remarks are in Section 5.

2 THE PROCEDURE

N-body dynamical systems are often employed to model galaxies (Wu & Jiang 2009, 2012, 2015). For an N-body system, any particle with coordinate (x, y, z) follows the equations of motion given below:

$$\begin{cases} \frac{d^2x(t)}{dt^2} = -\frac{\partial\Phi(x, y, z, t)}{\partial x}, \\ \frac{d^2y(t)}{dt^2} = -\frac{\partial\Phi(x, y, z, t)}{\partial y}, \\ \frac{d^2z(t)}{dt^2} = -\frac{\partial\Phi(x, y, z, t)}{\partial z}, \end{cases} \quad (1)$$

where $\Phi(x, y, z, t)$ is the total potential of this system. In a realistic N-body simulation, $\Phi(x, y, z, t)$ is evaluated repeatedly at each time step. However, in this paper, in order to be more efficient in searching for equilibrium models constrained by observational data, the total galactic potential is fixed and the SMBH is represented by a point mass at the center. The total potential is set to be a

summation of galactic total potential and SMBH potential.

Because the image of NGC 1399 is circularly symmetric, for convenience, the total galactic potential is assumed to be spherical as in Samurović (2016). All particles that represent the stellar part are governed under the parameterized total potential.

For particles' initial positions, due to the fact that NGC 1399 is a core galaxy (Dullo & Graham 2014), these stellar particles are set to follow a spherical core-double-power-law density distribution. The initial velocities are set based on a reasonable function of anisotropic parameters.

After initial positions and velocities are given, all particle orbits will be determined through the above equations of motion. When the system settles into a quasi-steady distribution at a particular time, i.e., t_{end} , all particle positions and velocities are recorded at this snapshot. The corresponding stellar surface brightness and velocity dispersion are calculated and compared with the observations.

To investigate the existence of a stellar remnant ring, an axisymmetric stellar part is then considered. The initial positions and velocities of axisymmetric particles are chosen in such a way that after they are integrated to t_{end} and added into the system, the overall t_{end} snapshot can better fit the observations. That is, through particle superposition, an axisymmetric stellar part is added in a way to improve the surface-brightness and kinematic fittings. It is called the remnant ring hereafter, which could be a structure left over during the formation of this system.

3 THE MODELS

Following the procedure mentioned in the previous section, further details are described here.

3.1 The Observational Constraints

Because the observed surface brightness profile was fitted well by a core-Sersic law in Dullo & Graham (2014), the core-Sersic law is used as our observational constraint for the surface brightness of NGC 1399. The long-slit velocity dispersion data from Graham et al. (1998) cover the whole core region of NGC 1399 with reasonable resolution. Thus, it is employed as our observational constraint as it fits our goal of determining the luminous and dark matter distributions around this region.

Table 1 The Density Profiles

Profile	α	β	γ	$\rho_{\text{total}}(r)$
A	2	3	0	$\rho_t \left\{ 1 + \left(\frac{r}{r_{\text{tb}}} \right)^2 \right\}^{-1.5}$
B	2	5	0	$\rho_t \left\{ 1 + \left(\frac{r}{r_{\text{tb}}} \right)^2 \right\}^{-2.5}$
C	1	4	1	$\rho_t \left(\frac{r}{r_{\text{tb}}} \right)^{-1} \left\{ 1 + \frac{r}{r_{\text{tb}}} \right\}^{-3}$
D	2	5	1	$\rho_t \left(\frac{r}{r_{\text{tb}}} \right)^{-1} \left\{ 1 + \left(\frac{r}{r_{\text{tb}}} \right)^2 \right\}^{-2}$
E	1	4	2	$\rho_t \left(\frac{r}{r_{\text{tb}}} \right)^{-2} \left\{ 1 + \frac{r}{r_{\text{tb}}} \right\}^{-2}$
F	1	6	2	$\rho_t \left(\frac{r}{r_{\text{tb}}} \right)^{-2} \left\{ 1 + \frac{r}{r_{\text{tb}}} \right\}^{-4}$

In addition, the mass of the central SMBH was determined to be $5.1 \pm 0.7 \times 10^8 M_{\odot}$ in Gebhardt et al. (2007) and $1.2_{-0.6}^{+0.5} \times 10^9 M_{\odot}$ in Houghton et al. (2006). The above two values are actually consistent with each other. Due to the fact that very central kinematics are measured in Houghton et al. (2006), we set the mass of the SMBH to be $1.2 \times 10^9 M_{\odot}$ in this paper.

3.2 The Units

The mass unit is $1.2 \times 10^{12} M_{\odot}$, the length unit is kpc and the time unit is 4.3×10^5 years. With these units, the gravitational constant $G = 1$.

3.3 The Density Profiles

The central galactic total density profile, i.e. the stellar part plus dark matter, follows the double-power law as

$$\rho_{\text{total}}(r) = \rho_t \left(\frac{r}{r_{\text{tb}}} \right)^{-\gamma} \left\{ 1 + \left(\frac{r}{r_{\text{tb}}} \right)^{\alpha} \right\}^{\frac{\gamma-\beta}{\alpha}}, \quad (2)$$

where ρ_t is a constant and the scale length r_{tb} is the total break radius. When $r \gg r_{\text{tb}}$, the above becomes a power law with index $-\beta$. For $r \ll r_{\text{tb}}$, γ is the inner cusp slope of this density profile.

In order to include different possible slopes for the central cusp, we choose six profiles with different values of α , β and γ as listed in Table 1. In Table 1, Profiles A and B are for $\gamma = 0$; Profiles C and D are for $\gamma = 1$; Profiles E and F are for $\gamma = 2$. These profiles are equivalent to some of those with analytic potentials discussed in Zhao (1996).

In addition to the above, due to the fact that the velocity dispersion remains nearly constant from $R = 2$ kpc to $R = 6$ kpc, more dark matter shall be present

around that region (Saglia et al. 2000). In order to have more galactic mass out of $R = 2$ kpc, another power-law profile is employed. Thus,

$$\rho(r) = \begin{cases} \rho_{\text{total}}(r) & \text{if } r \leq r_d, \\ cr^p & \text{if } r > r_d, \end{cases} \quad (3)$$

where p is the power-law index, the constant $c = \frac{\rho_{\text{total}}(r_d)}{(r_d)^p}$ and r_d is the transition radius.

In order to search for the best model, several grids of parameters are considered. There would be a total of six central galactic density profiles, 10 values of r_{tb} , 10 values of p and four values of r_d . That is, under Profiles A, B, C, D, E and F, we have $r_{\text{tb}} = 0.3$ to 1.2 with step 0.1, $p = -2.1$ to -1.2 with step 0.1 and $r_d = 2.5, 3.0, 3.5$ and 4.0. Thus, totally 2400 models should be calculated in this paper.

Note that one SMBH is placed at the coordinate center. In addition to the total galactic potential derived from the above density profiles, the gravitational potential of one SMBH is added.

Since NGC 1399 is a core galaxy, 10^6 stellar particles are set to follow an initial distribution as Profile A. Thus,

$$\rho_{\text{star}}(r) = \rho_s \left\{ 1 + \left(\frac{r}{r_{\text{sb}}} \right)^2 \right\}^{-1.5}, \quad (4)$$

where ρ_s is a constant and the scale length r_{sb} is the stellar break radius.

It is found that we need to set $r_{\text{sb}} = 1.0$ in order to have enough stellar particles in the main part of the system. At this radius, a typical velocity is estimated to be $v_{\text{sb}} = 0.1$ and a dynamical time $t_d \equiv r_{\text{sb}}/v_{\text{sb}} = 10$. Employing the leapfrog integrator (Binney & Tremaine 2008), the orbits of all particles are calculated from $t = 0$ to $t = t_{\text{end}} \equiv 10t_d$.

3.4 The Initial Velocities

The assignment of particles' initial velocities is described here. The velocity magnitude is set to be the circular velocity with respect to the galactic total mass (excluding SMBH mass) at the particle's position, i.e. $v_{\text{cir}}(r)$. This velocity is divided into two components, the radial velocity v_r and the tangential velocity v_t . Thus, $v_{\text{cir}}^2(r) = v_t^2 + v_r^2$.

In this case, the anisotropy parameter β_a (Binney & Tremaine 2008) satisfies

$$\beta_a = 1 - \frac{\bar{v}_t^2}{2\bar{v}_r^2}, \quad (5)$$

where \bar{v}_t^2 is the average tangential velocity over particles and \bar{v}_r^2 is the average radial velocity over particles. Theoretical models of galaxy formation show that β_a generally increases with radius (Binney & Tremaine 2008). In order to choose our initial velocities properly to make sure that β_a approximately increases with radius, we create a function $\beta_p(r)$ which has a value -1 at $r = 0$ kpc and becomes 1 at $r = 6$ kpc (note we set the outer boundary to be 6 kpc for the system considered in this paper). The simplest nonlinear polynomial function which has this mathematical property is

$$\beta_p(r) = -\frac{1}{18}r^2 + \frac{2}{3}r - 1. \quad (6)$$

Because the magnitudes of radial and tangential velocities satisfy

$$v_t^2 + v_r^2 = v_{\text{cir}}^2 \equiv \frac{GM(r)}{r}, \quad (7)$$

where $M(r) = 4\pi \int_0^r \bar{r}^2 \rho(\bar{r}) d\bar{r}$, and we set $v_t^2 = 2(1 - \beta_p(r))v_r^2$, they can be obtained as

$$\begin{cases} v_r = \sqrt{\frac{GM(r)}{\left[\left(2 - \frac{1}{3}r\right)^2 + 1\right]r}}, \\ v_t = \left| \left(2 - \frac{1}{3}r\right) \right| v_r. \end{cases} \quad (8)$$

As for the directions, the radial velocity is set to be either leaving from the system center (outward) or going to the system center (inward) with equal probability. The direction of tangential velocity is set to be isotropic. The particle velocity is thus determined after the radial and tangential velocities are settled.

As an example, Figure 1 gives the information on initial velocities of a model with parameters $r_{\text{tb}} = 1.0$, $p = -1.3$ and $r_d = 3.0$. The anisotropy parameter β_a as a function of radius for Profiles A-F is presented in Figure 1(a). The average v_t^2 (dashed curves) and the average v_r^2 (solid curves) as functions of radius for Profiles A-F are shown in Figure 1(b).

3.5 The Surface Brightness and Velocity Dispersion

In our coordinate system, the line of sight is along the z -axis and the plane of the sky is set to be the x - y plane. In order to calculate the theoretical surface brightness, radial bins on the x - y plane are set as below. The circle with radius R_0 centered on the coordinate center is the 0-th radial bin. The annulus between R_0 and R_1 is the 1st radial bin. In general, the i -th radial bin is the annulus between R_{i-1} and R_i , where $i = 1, 2, 3, \dots$. Here we

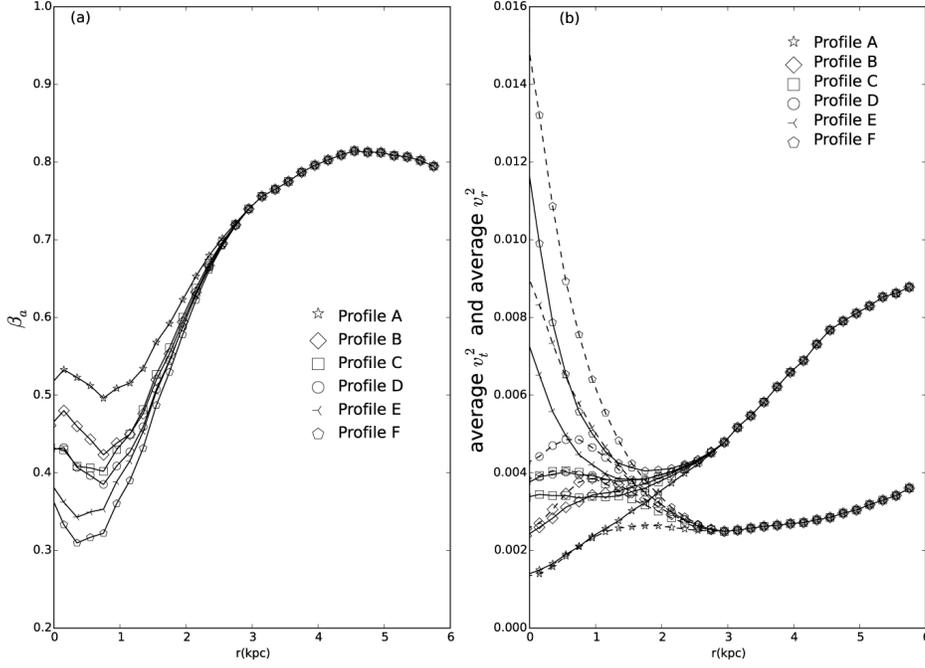


Fig. 1 The initial velocities. (a) The value of β_a as a function of radius r for Profiles A-F. (b) The average v_t^2 (dashed curves) and the average v_r^2 (solid curves) as functions of radius r for Profiles A-F.

choose $R_0 = 0.1$ and $\delta R \equiv R_i - R_{i-1} = 0.2$ for any positive integer i .

To calculate the velocity dispersion, cells are further set at the long-slit positions along the x -axis. The cell height is defined to be h . Here we set $h = 0.1$. Within the 1st radial bin, the cell ranging from $\theta = -\tan^{-1}(h/R_1)$ to $\theta = \tan^{-1}(h/R_1)$ is called the right cell, and the cell ranging from $\theta = \pi - \tan^{-1}(h/R_1)$ to $\pi + \theta = \tan^{-1}(h/R_1)$ is called the left cell.

Similarly, within the i -th radial bin for any integer $i > 0$, the cell ranging from $\theta = -\tan^{-1}(h/R_i)$ to $\theta = \tan^{-1}(h/R_i)$ is the right cell, and the cell ranging from $\theta = \pi - \tan^{-1}(h/R_i)$ to $\theta = \pi + \tan^{-1}(h/R_i)$ is the left cell. For NGC 1399, the observational data of velocity dispersion along the $+x$ -axis and $-x$ -axis are both available. The average values of the two sides are used as observational values. The particles in both right and left cells are included in the calculations of theoretical velocity dispersion.

Figure 2 shows the surface brightness as a function of radius R . The solid curve is the observational profile derived from the R -band data (Dullo & Graham 2014). That is

$$\mu(R) = -2.5 \log_{10} \left(I(R)/I(R_b) \right) + \mu_b, \quad (9)$$

where $\mu_b = 16.36$ is the mag at the core radius $R_b = 0.202$ kpc, and the analytic core-Sersic law gives (Dullo & Graham 2014)

$$I(R) = I_0 \left[1 + \left(\frac{R_b}{R} \right)^{\alpha_n \gamma_n / \alpha_n} \right]^{\alpha_n \gamma_n / \alpha_n} \times \exp \left[-b_n \left(\frac{R^{\alpha_n} + R_b^{\alpha_n}}{R_e^{\alpha_n}} \right)^{1/(\alpha_n n)} \right], \quad (10)$$

where $R_e = 3.22$ kpc, $\alpha_n = 2$, $\gamma_n = 0.11$, $b_n = 2n - 1/3$ and $n = 5.6$. Note that I_0 is a normalization constant which can be determined by $\mu_b = 16.36$.

With the same normalization, the values of theoretical surface brightness in our models are then determined. In Figure 2, the points are the average surface brightness of 2400 models at the t_{end} snapshot. The error bars are the corresponding standard deviations. Thus, for $R \geq 1$ kpc, the theoretical surface brightness of all models generally follows the observations. However, for $R < 1$ kpc, the theoretical surface brightness of all models is smaller than the observations.

3.6 The Remnant Ring

An additional component in the form of a remnant ring is considered here. These added particles are called remnant-ring particles. For convenience, the particles

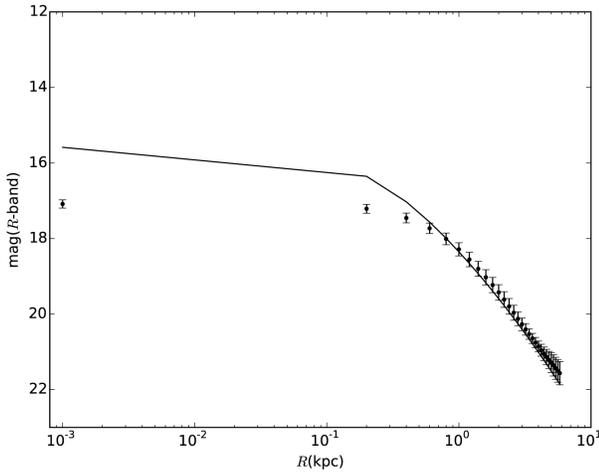


Fig. 2 The surface brightness as a function of radius R of main-part stellar particles at the t_{end} snapshot. The average theoretical surface brightness of all 2400 models and their standard deviations are shown by the points with error bars. The solid curve is for the observation, set by Eqs. (9)–(10) with the same parameters as written in the main text.

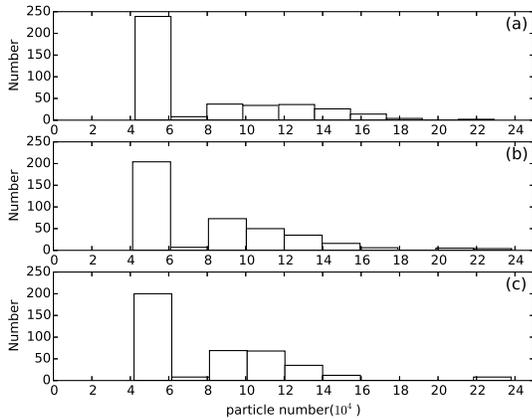


Fig. 3 The histograms of particle numbers of the remnant ring in 400 models for three profiles. Panel (a) is for Profile C, Panel (b) is for Profile D and Panel (c) is for Profile E.

which belong to the original spherical part would be called the main-part particles.

The numbers of remnant-ring particles in radial bins are decided by comparing the theoretical surface brightness contributed from main-part particles in these radial bins with the observational surface brightness.

Figure 3(a)–(c) shows histograms of the number of remnant-ring particles for all models in Profiles C, D and E. In each radial bin, the initial positions of remnant-ring particles are uniformly distributed between two boundaries of the bin and within a z interval $[-z_t, z_t]$, where $z_t = R_i/60$. This leads to a linearly increasing thickness

for the remnant ring. The particles’ radial distances on the x - y plane are $R = \sqrt{x^2 + y^2}$. Their x and y components of velocities are assigned in a way that their orbits are circular on the x - y plane.

The z components of remnant-ring particle velocities, which are along the line-of-sight, will affect the values of theoretical velocity dispersion. A target line-of-sight velocity distribution in each radial bin is set as a Gaussian distribution function with a σ being the same as the observational velocity dispersion. The remnant-ring particle’s v_z is set in a way to make the total number of main-part and remnant-ring particles over v_z velocity bins equal to this target distribution’s integral in v_z velocity space for each radial bin.

With the above initial conditions, the orbits of remnant-ring particles are calculated from $t = 0$ to $t = t_{\text{end}}$ through the leapfrog integrator (Binney & Tremaine 2008). Considering t_{end} snapshots, these remnant-ring particles would be included as part of stellar particles when the final theoretical velocity dispersion and surface brightness are calculated. Thus, after remnant rings are included, our models become complete. As we can see from Figure 3, the numbers of remnant-ring particles in our models range from 50 000 to 150 000, which is about 5 to 15 percent of the main-part.

4 THE RESULTS

The t_{end} snapshots of all these 2400 models are considered and used to compare with observations. The surface brightness of these models can fit the observationally determined core-Sersic law very well. There are some deviations around the outer part of the considered region due to a very small number of particles around there. We ignore those deviations as our study focuses on the central profiles around the core structure.

We then calculate the theoretical velocity dispersion of these 2400 models in order to compare with the observational velocity dispersion. The chi-square fitting is used to do the above comparison and obtain the best-fit models. We set

$$\chi^2 = \sum_{i=0}^{28} \frac{(O_i - T_i)^2}{O_i}, \quad (11)$$

where O_i is the observational velocity dispersion of the i -th radial bin and T_i is the theoretical velocity dispersion of the i -th radial bin. There are 29 bins, so the degrees of freedom is 28 and the reduced chi-square $\chi_{\text{red}}^2 = \chi^2/28$. We obtain χ_{red}^2 for all 2400 models.

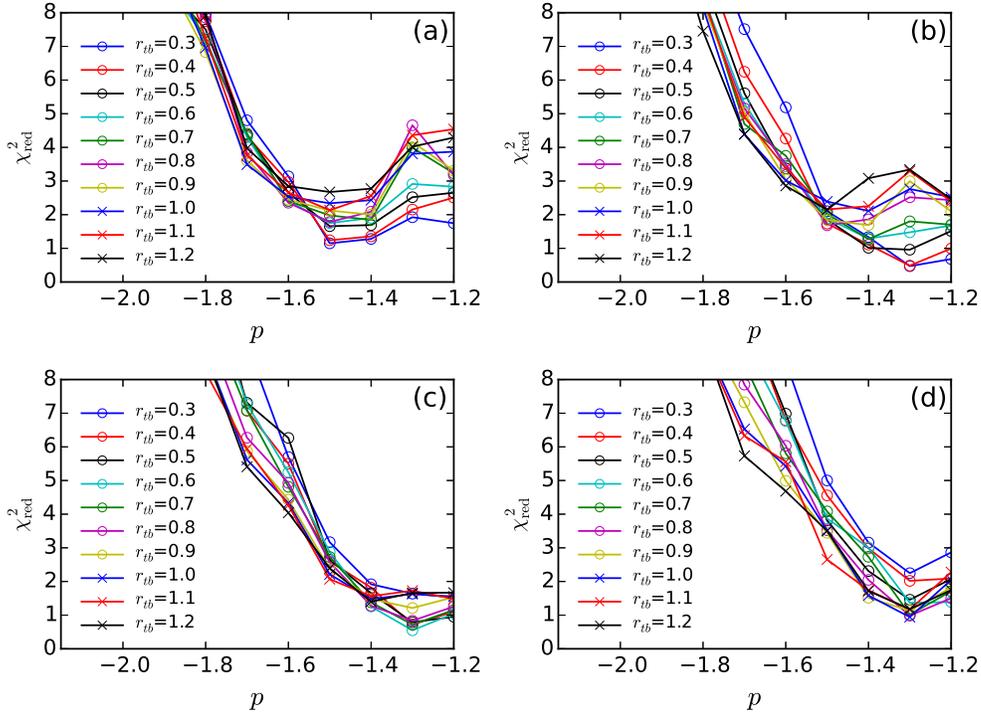


Fig. 4 The value of reduced chi-square χ_{red}^2 as a function of p for different values of r_{tb} in Profile C. Panel (a) is for $r_d = 2.5$, Panel (b) is for $r_d = 3.0$, Panel (c) is for $r_d = 3.5$ and Panel (d) is for $r_d = 4.0$.

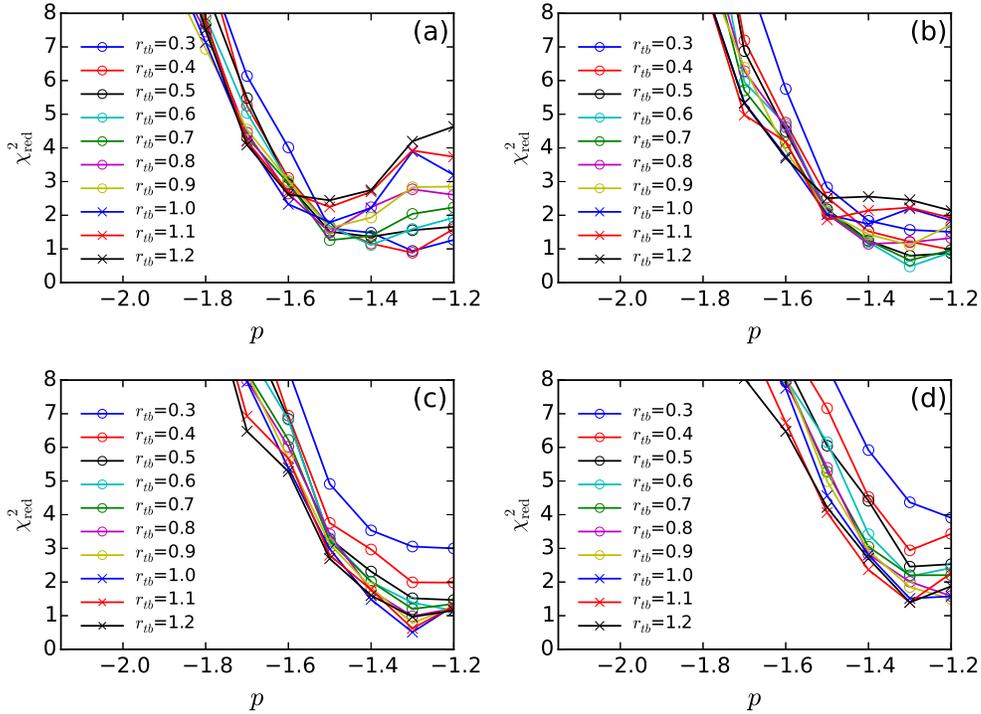


Fig. 5 The value of reduced chi-square χ_{red}^2 as a function of p for different values of r_{tb} in Profile D. Panel (a) is for $r_d = 2.5$, Panel (b) is for $r_d = 3.0$, Panel (c) is for $r_d = 3.5$ and Panel (d) is for $r_d = 4.0$.

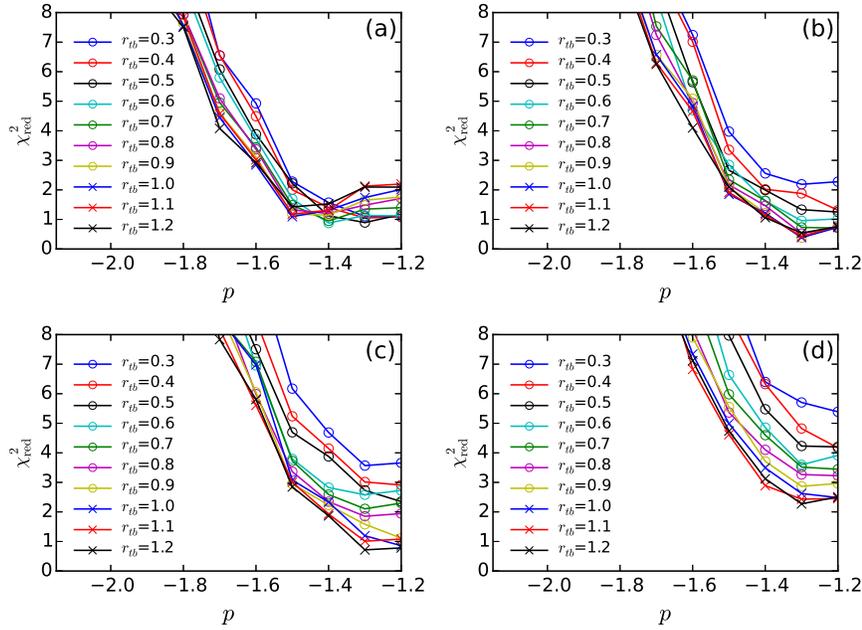


Fig. 6 The value of reduced chi-square χ_{red}^2 as a function of p for different values of r_{tb} in Profile E. Panel (a) is for $r_d = 2.5$, Panel (b) is for $r_d = 3.0$, Panel (c) is for $r_d = 3.5$ and Panel (d) is for $r_d = 4.0$.

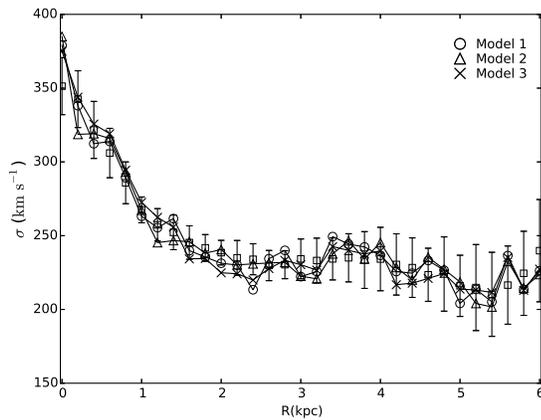


Fig. 7 The velocity dispersion as a function of R for three best-fit models. The line with circles is for Model 1, the line with triangles is for Model 2 and the line with crosses is for Model 3. The squares with error bars are for the observational data.

Figures 4–6 show the values of reduced chi-square χ_{red}^2 for 400 models in Profiles C, D and E, respectively. In general, when the χ_{red}^2 value is much larger than one, the model is unlikely to be the correct one; when the χ_{red}^2 value is around one, the model has a high probability to be the correct one. For example, as shown in Figures 4–6, those models with $p = -1.7$ are all unlikely cases. However, there are also plenty of possible models. The one with the smallest χ_{red}^2 is regarded as the most likely

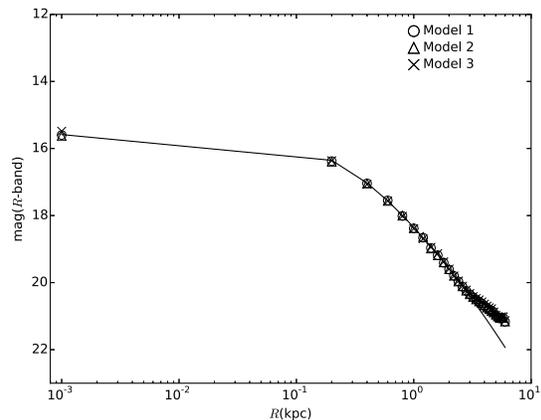


Fig. 8 The surface brightness as a function of R for three best-fit models. The circles are for Model 1, the triangles are for Model 2 and the crosses are for Model 3. The solid curve is for the observation, set by Eqs. (9)–(10), with the same parameters as written in the main text.

model. Because many models have very similar values of χ_{red}^2 , we decide to select three models, whose χ_{red}^2 are smaller than all the rest, as best-fit models.

In Table 2, the parameters of these three best-fit models are presented. Although their central galactic total density profiles are different, they are all centrally cuspy models. That is, Model 1 and Model 2 have the same inner cusp slope $\gamma = 1$, while Model 3 has a larger inner

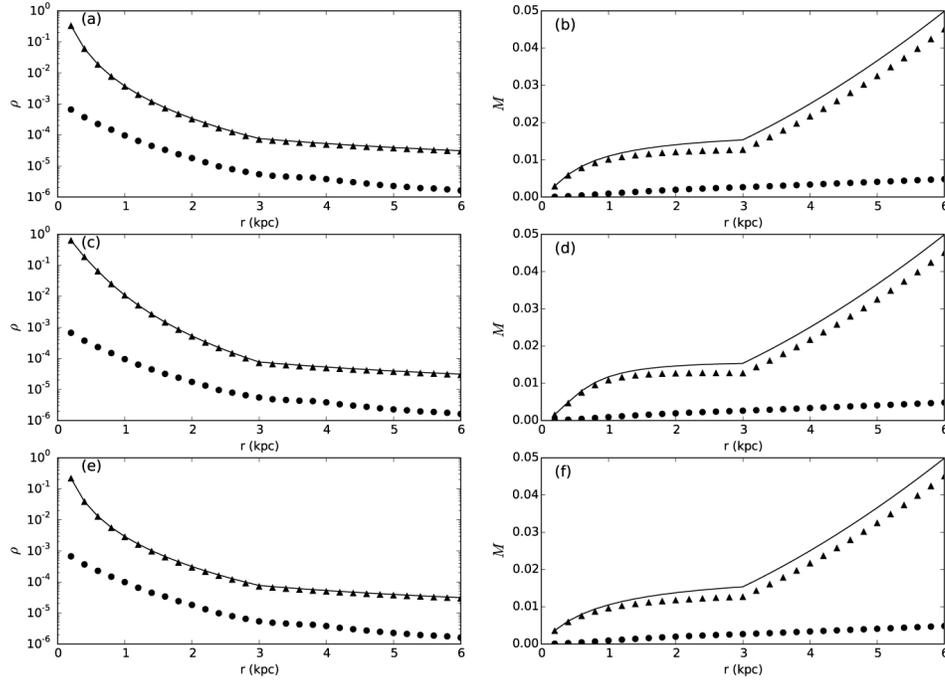


Fig. 9 The density and the cumulative mass as functions of radius r for three best-fit models. Left panels are for the density and right panels are for the cumulative mass. Panels (a)–(b) are for Model 1, Panels (c)–(d) are for Model 2 and Panels (e)–(f) are for Model 3. In each panel, *triangles* are for the dark matter, *circles* are for the stellar part and *solid curves* are for the total. The density unit is $1.2 \times 10^{12} M_{\odot} \text{ kpc}^{-3}$ and the mass unit is $1.2 \times 10^{12} M_{\odot}$.

Table 2 The Best-fit Models

Model	1	2	3
Profile	C	D	E
r_{tb}	0.3	0.6	0.9
r_d	3.0	3.0	3.0
p	-1.3	-1.3	-1.3
Remnant-ring	118 376	115 940	99 347
Particle numbers			
χ_{red}^2	0.47	0.48	0.38

cusps slope with $\gamma = 2$. In addition, they have different total break radius, but their transition radius and power-law index are exactly the same. The numbers of remnant-ring particles are about 10 percent of the main-part stellar particles.

From the values of χ_{red}^2 , it is clear that these three models are completely consistent with the observational data. Figure 7 shows the velocity dispersion as a function of R . The line with circles is for Model 1, the line with triangles is for Model 2 and the line with crosses is for Model 3. The squares with error bars are for observational data. Figure 8 presents the surface brightness of the best-fit models. Circles are for Model 1, trian-

gles are for Model 2, crosses are for Model 3 and the solid curve is the observational surface brightness set by Equations (9)–(10) with the same parameters.

Moreover, the dark matter density profiles can be obtained by subtracting the stellar density from the galactic total density. Considering the spherically distributed parts, Figure 9(a) displays the dark matter density profiles (triangles), the stellar density profiles (circles) and the galactic total density profiles (solid curves) of Model 1. Similarly, Figure 9(c) and Figure 9(e) are for Model 2 and Model 3, respectively.

In addition, the total cumulative mass as a function of radius, $M(r)$, is shown in the right panels of Figure 9. In Figure 9(b), the dark matter (triangles), the stellar part (circles) and the galactic total cumulative mass (solid curves) of Model 1 are presented. Figure 9(d) and Figure 9(f) are for Model 2 and Model 3, respectively.

As can be seen in Figure 9, the inner cusp slope of the galactic total density profile is mainly contributed by dark matter. It is consistent with the results of cosmological simulations, demonstrating that the dark matter profile is cuspy as the NFW profile has a central cusp

with a power-law index $\gamma = 1$. Furthermore, it is clear that the results of Models 1–3 presented in Figure 9 are very similar. That is, the best-fit models converge into one physical model after a numerical survey over several parameters and examining 2400 models. Therefore, this physical model we found could represent the core galaxy NGC 1399 well.

5 CONCLUDING REMARKS

The structures of early-type galaxies continue to be an important subject as they result from the formation and interactions of galaxies. The dynamical histories of galaxies could be revealed through modeling these galaxies. It is interesting that some early-type galaxies have core structures given that cosmological simulations show cuspy dark matter profiles. In order to address this, both the distributions of luminous matter and dark matter shall be determined separately through dynamical modeling.

Motivated by the core structure of the central surface brightness of early-type galaxies, through particle superposition, we construct dynamical models of the core galaxy NGC 1399. The distributions of luminous and dark matter are studied for this galaxy. Because early-type galaxies are likely to be products of mergers, remnant rings are considered in our models.

A numerical survey of parameters is performed and three best-fit models are obtained. We conclude that the inner slope of the dark matter profile is cuspy for this core galaxy NGC 1399. In addition, the remnant ring contributes to the central surface brightness of NGC 1399. Thus, this implies that the remnant ring could be a candidate of the physical counterpart for the core structure of early-type galaxies.

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