# Three-dimensional orbit and physical parameters of HD 6840 

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#### Abstract

HD 6840 is a double-lined visual binary with an orbital period of $\sim 7.5$ years. By fitting the speckle interferometric measurements made by the 6 m BTA telescope and 3.5 m WIYN telescope, Balega et al. gave a preliminary astrometric orbital solution of the system in 2006. Recently, Griffin derived a precise spectroscopic orbital solution from radial velocities observed with OPH and Cambridge Coravel. However, due to the low precision of the determined orbital inclination, the derived component masses are not satisfying. By adding the newly collected astrometric data in the Fourth Catalog of Interferometric Measurements of Binary Stars, we give a three-dimensional orbit solution with high precision and derive the preliminary physical parameters of HD 6840 via a simultaneous fit including both astrometric and radial velocity measurements.


Key words: binaries: spectroscopic - astrometry - stars: fundamental parameters - stars: individual (HD 6840)

## 1 INTRODUCTION

Mass is the most important parameter of a star in deciding its physical state and evolution, and the only reliable way to determine this parameter is determination of a binary orbit requiring two or more types of observational data (Torres et al. 2010). Currently available stellar masses that are measured with high precision are mainly components of double-lined eclipsing binaries, and the physical evolution of these components is seriously influenced by tidal effects (Andersen 1991; Torres et al. 2010). Therefore, precise determination of the component masses in doublelined spectroscopic visual binaries, especially those without close encounters between components, is important for constraining stellar evolutionary models.

Generally speaking, there are no close encounters between components or strong tidal effects in binaries with orbital periods larger than several years. HD 6840 (HIP 5531 ) is such a system. Its orbital period is $\sim 7.5$ years and observational data derived from both its astrometric and spectroscopic measurements are enough to give a precise three-dimensional orbital solution.

Though identified as a visual binary by the Hipparcos mission (ESA 1997), there was only one relative positional datum between the two components provided by Hipparcos. Not long after the publication of the Hipparcos catalog, Horch et al. (1999, 2002) and Balega et al. (2002, 2004, 2006) carried out speckle interferometric measurements. From the resulting tangential position data (TPD), a preliminary astrometric orbital solution of the system was given by Balega et al. (2006). Afterwards, more TPD were provided by Horch et al. (2008, 2009), Balega et al. (2013)
and Mason et al. (2009), including those obtained with the adaptive optics instrument Robo-AO (Riddle et al. 2015).

As a double-lined spectroscopic binary, the mass ratio of 0.99 was published in 2004 (Nordström et al. 2004). In 1993, HD 6840 was included in the Cambridge spectroscopic-binary observing program. The long-term radial velocity data (RVD) allowed Griffin (2012) to give a spectroscopic orbital solution with high precision. However, due to the low precision of the determined orbital inclination, the derived component masses are not precise enough to be used in constraining stellar evolutionary models.

In order to give a precise three-dimensional orbital solution, together with the component masses and the orbital parallax, all the above-mentioned observational data coming from different sources should be appropriately weighted and used in a simultaneous fit. To do so, we adopt the weighting scheme by Wang et al. (2015) and apply the fitting method by Ren \& Fu (2010).

The observational data that we used are described in Section 2 and the determined three-dimensional orbit is presented in Section 3. Discussions are provided in Section 4.

## 2 OBSERVATIONAL DATA

### 2.1 Interferometric Data

Since the first astrometric measurement made by the Hipparcos mission (ESA 1997), HD 6840 has been observed with the speckle interferometric technique by several teams. Horch et al. $(1999,2002)$ carried out three
speckle interferometric measurements with the Wisconsin-Indiana-Yale-NOAO (WIYN) 3.5 m telescope located at Kitt Peak, Arizona. Using the 6 m BTA telescope of the Special Astrophysical Observatory, Balega et al. (2002, 2004 , 2006) made seven speckle interferometric measurements. These measurements lead to 10 TPD, from which a preliminary astrometric orbit solution was given by Balega et al. (2006). Afterwards, 14 more TPD were provided, including seven by Horch et al. $(2008,2009)$, four by Balega et al. (2013), two by Mason et al. (2009), and one by Riddle et al. (2015) with the adaptive optics instrument Robo-AO.

Extracted from the online version of the Fourth Catalog of Interferometric Measurements of Binary Stars (Hartkopf et al. 2001), the above-mentioned data are listed with their post-fit residuals and associated references in Table 1. In this table, $\rho$ and $\theta$ are the polar coordinates of the primary relative to the secondary in the plane of sky with respect to north.

### 2.2 Spectroscopic Data

In 1993, HD 6840 was included in the Cambridge spectroscopic-binary observing program, and long term RVD of the system were acquired by OPH Coravel and

Cambridge Coravel (Griffin 2012). From 1993 to 1998, 19 RVD were obtained by OPH Coravel, and 12 among these RVD were successfully identified as double-lined binaries. In addition, a further 75 RVD were obtained by Cambridge Coravel, and among these, 58 RVD were identified as double-lined cases. By fitting these RVD, a high precision spectroscopic orbital solution was determined by Griffin (2012). Because the RVD of the two component stars cannot be separated spectroscopically, they are not used to fit the orbit in case of error (Griffin 2012) in our work. The RVD that were identified as double-lined cases are listed in Table 2.

## 3 ORBIT DETERMINATION

For convenience of calculation, the TPD are expressed in rectangular coordinates

$$
\begin{aligned}
& x=\rho \cos \theta \\
& y=\rho \sin \theta
\end{aligned}
$$

When we use the least squares method to determine the three-dimensional orbit by combining the TPD and the RVD, a simultaneous adjustment of all orbital elements is applied. The objective function is

$$
\begin{equation*}
\chi^{2}=\sum_{i=1}^{N_{1}}\left[\left(\frac{x_{\mathrm{o}, i}-x_{i}}{\sigma_{x, i}}\right)^{2}+\left(\frac{y_{\mathrm{o}, i}-y_{i}}{\sigma_{y, i}}\right)^{2}\right]+\sum_{j=1}^{N_{2}}\left[\left(\frac{V_{\mathrm{po}, j}-V_{\mathrm{p}, j}}{\sigma_{\mathrm{vp}, j}}\right)^{2}+\left(\frac{V_{\mathrm{so}, j}-V_{\mathrm{s}, j}}{\sigma_{\mathrm{vs}, j}}\right)^{2}\right] \tag{1}
\end{equation*}
$$

where $N_{1}$ and $N_{2}$ represent the numbers of data points in the TPD and RVD, respectively. The subscript ' $o$ ' indicates the observational data, and ' p ' and ' s ' indicate the primary and secondary, respectively. The quantities $x, y, V_{\mathrm{p}}$ and $V_{\mathrm{s}}$ can be calculated from the orbital elements (Pourbaix 1998).

In Equation (1), the observational data need to be weighted. However, not all the data have known errors. Therefore, post-fit residuals are used to estimate the required errors (Wang et al. 2015). Because the post-fit residual of a datum, namely the difference between the observed and calculated values, depends on model parameters, an iterative process is necessary. Let us first recall this process in the general text. We start with the values of model parameters obtained with the equal weighting scheme. Then the post-residuals can be calculated. For a group of $N$ data observed with the same equipment, we assume a single value for their error, which is simply estimated as the averaged absolute residual

$$
\begin{equation*}
\sigma=\sum_{i=1}^{N} \frac{\left|O_{i}-C_{i}\right|}{N} \tag{2}
\end{equation*}
$$

where $O_{i}\left(C_{i}\right)$ is the $i$ th observed (calculated) value. Now the weights of the observational data are well estimated, and so are values in the next iterative step. The iterative process does not stop until the standard errors are all convergent.

The errors of TPD and RVD are calculated separately. Considering the astrometric precision is at about the milliarcsecond (mas) level, when the derived errors are smaller than 1 mas, an error of 1 mas is assumed. After calculation, the errors of the TPD in the declination direction are $1.6,1.0,1.4,4.3$ and 4.9 mas for the astrometric data observed by WIYN, BTA, the Hipparcos mission and Robo-AO, and those provided by Mason et al. (2009) respectively, and the corresponding errors of the TPD in the right ascension direction are 2.3, 1.0, 15.0, 1.5 and 1.0 mas. Note that the RVD derived from a close blend are considered as a group of data that is different from the other data for the same component and with the same equipment, and the errors associated with RVD are listed in Table 2.

There are 10 parameters that need to be adjusted, and the modified grid method developed in Ren \& Fu (2010) is used to find the global minimum of Equation (1). The determined values of all the parameters including the radial velocity of the barycenter $\left(V_{0}\right)$, the amplitudes of the radial velocity curves ( $K_{1}, K_{2}$ ), the semimajor axis of the relative orbit ( $a$ ), the inclination ( $i$ ), the latitude of the ascending node $(\Omega)$, the argument of the periastron $\left(\omega_{A}\right)$, the eccentricity $(e)$, the period $(P)$, and the time of passage at periastron $(T)$ are given in Table 3, together with the orbital parallax and the component masses ( $M_{1}$ and $M_{2}$ ). Moreover, the orbital solutions given by Griffin (2012) and Balega et al. (2006) are also listed in the same table for comparison. From this table, we see that the semimajor

Table 1 Astrometric Data of HD 8460

| Julian Year | $\rho$ <br> $\left({ }^{\prime \prime}\right)$ | $\theta$ <br> $\left({ }^{\circ}\right)$ | $(O-C)_{\rho}$ <br> $\left({ }^{\prime \prime}\right)$ | $(O-C)_{\theta}$ <br> $\left({ }^{\circ}\right)$ | Reference |
| :---: | :---: | :---: | :---: | :---: | :--- |
| 1991.2500 | 0.136 | 165.0 | 0.005 | -6.3 | ESA (1997) |
| 1997.6300 | 0.122 | 162.8 | -0.000 | 0.6 | Horch et al. (1999) |
| 1998.7745 | 0.131 | 171.9 | -0.000 | 0.0 | Balega et al. (2002) |
| 1999.6342 | 0.125 | 182.6 | 0.001 | 3.5 | Horch et al. (2002) |
| 1999.8211 | 0.121 | 180.4 | -0.000 | -0.5 | Balega et al. (2004) |
| 2000.7646 | 0.102 | 193.3 | 0.003 | 1.7 | Horch et al. (2002) |
| 2000.8784 | 0.095 | 193.1 | -0.001 | -0.3 | Balega et al. (2006) |
| 2002.7960 | 0.032 | 310.4 | 0.006 | -2.7 | Balega et al. (2006) |
| 2002.7965 | 0.026 | 310.0 | 0.000 | -3.3 | Balega et al. (2013) |
| 2003.6373 | 0.065 | 140.1 | 0.001 | 0.6 | Horch et al. (2008) |
| 2003.6373 | 0.065 | 141.2 | 0.001 | 1.7 | Horch et al. (2008) |
| 2003.7880 | 0.075 | 145.0 | 0.001 | 1.1 | Balega et al. (2006) |
| 2003.9277 | 0.082 | 146.8 | -0.000 | -0.3 | Balega et al. (2013) |
| 2003.9280 | 0.082 | 146.8 | -0.000 | -0.3 | Balega et al. (2006) |
| 2004.8155 | 0.116 | 159.6 | -0.000 | 0.1 | Balega et al. (2007) |
| 2004.8160 | 0.116 | 159.5 | -0.000 | -0.0 | Balega et al. (2006) |
| 2005.8625 | 0.122 | 167.9 | -0.009 | -1.0 | Mason et al. (2009) |
| 2006.6900 | 0.129 | 175.2 | 0.000 | -0.5 | Balega et al. (2013) |
| 2007.0093 | 0.121 | 177.7 | -0.004 | -0.7 | Horch et al. (2010) |
| 2007.0120 | 0.127 | 177.8 | 0.002 | -0.6 | Horch et al. (2010) |
| 2007.6049 | 0.114 | 184.4 | -0.001 | 0.2 | Mason et al. (2009) |
| 2007.8229 | 0.110 | 188.2 | 0.000 | 1.6 | Horch et al. (2010) |
| 2008.6911 | 0.084 | 198.7 | 0.000 | -0.9 | Horch et al. (2009) |
| 2009.7533 | 0.039 | 243.3 | -0.001 | -0.0 | Horch et al. (2012) |
| 2012.7021 | 0.121 | 163.6 | -0.004 | -0.1 | Riddle et al. (2015) |
|  |  |  |  |  |  |

axis $(a)$ and the orbital inclination $(i)$ are greatly improved. Then the component masses are two times more precise than those given by Griffin (2012).

The calculated velocity curve and the RVD are shown in Figure 1. The filled circles and open squares with an error bar represent the RVD observed with OPH and Cambridge Coravel, respectively. In addition, the RVD which cannot be used to separate the two components of the system are indicated by open triangles. The apparent orbits given by us and by Balega et al. (2006) are shown in Figure 2 with a solid and dotted ellipse, respectively. Also shown in this figure are the TPD with error bars. The point where the straight dotted lines intersect indicates the periastron. The open circles, squares, triangles, diamond and star with error bars indicate the measurements given by Balega et al. (2002, 2004, 2006, 2013), Horch et al. (1999, 2002, 2012), Mason et al. (2009), Riddle et al. (2015) and Hipparcos mission (ESA 1997), respectively.

## 4 DISCUSSION

The apparent magnitude in the $V$ band for the system is $6.555 \pm 0.010$ (Høg et al. 2000), and the corresponding difference in magnitude between the two components, derived from the average of interferometric observations near the $V$ band (Hartkopf et al. 2001), is about $0.70 \pm 0.1$. So, the apparent magnitudes in the $V$ band can be calculated as $7.01 \pm 0.04$ and $7.71 \pm 0.07$ for the primary and secondary, respectively. Along with the orbital parallax of $16.4 \pm 0.2$ mas, we can calculate the absolute magnitudes of


Fig. 1 Radial velocity curve and the RVD. The filled circles and open squares with error bars indicate the RVD obtained with OPH and Cambridge Coravel, respectively. The open triangles represent the RVD which are not used to fit the orbit since these data cannot be used to separate the two components of the system.
the primary and secondary as $3.09 \pm 0.04$ and $3.79 \pm 0.07$, respectively. Using the color index $(B-V)=0.0553 \pm$ 0.005 from the Hipparcos catalog (van Leeuwen 2007), the bolometric correction can be derived as $0.036 \pm 0.02$ (Flower 1996). Then, the luminosities can be derived as $4.78 \pm 0.20$ and $2.51 \pm 0.17$ for the primary and secondary, respectively.

Table 2 Radial Velocity Data of HD 6840

| MJD | $\begin{array}{r} \mathrm{RV}_{p} \\ \left(\mathrm{~m} \mathrm{~s}^{-1}\right) \end{array}$ | $\begin{array}{r} \sigma_{p} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{array}$ | $\begin{aligned} & \hline(O-C) \\ & \left(\mathrm{km} \mathrm{~s}^{-1}\right) \end{aligned}$ | $\begin{array}{r} \mathrm{RV}_{\mathrm{s}} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{array}$ | $\begin{array}{r} \sigma_{s} \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{array}$ | $\begin{aligned} & \hline(O-C) \\ & \left(\mathrm{km} \mathrm{~s}^{-1}\right) \end{aligned}$ | Equipment |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 49028.810(*) | -8.9 | 0.2 | 0.1 | -10.9 | 0.7 | -1.2 | OPH Coravel |
| 49064.780(*) | -9.1 | 0.2 | 0.1 | -10.5 | 0.7 | -1.0 | OPH Coravel |
| 49176.110(*) | -10.1 | 0.2 | -0.2 | -8.6 | 0.7 | 0.1 | OPH Coravel |
| 49346.890(*) | -11.3 | 0.2 | 0.0 | -7.1 | 0.7 | 0.1 | OPH Coravel |
| 49402.770(*) | -11.6 | 0.2 | 0.2 | -5.9 | 0.7 | 0.7 | OPH Coravel |
| 49566.110 | -13.9 | 0.5 | 0.2 | -5.5 | 0.8 | -1.4 | OPH Coravel |
| 49698.840 | -17.2 | 0.5 | 0.3 | -0.2 | 0.8 | 0.1 | OPH Coravel |
| 49720.790 | -17.4 | 0.6 | 1.0 | 2.2 | 0.5 | 1.6 | OPH Coravel |
| 49875.120 | -27.8 | 0.8 | -0.6 | 9.5 | 0.5 | -0.9 | OPH Coravel |
| 50082.830 | -6.4 | 0.8 | 0.0 | -13.0 | 0.6 | -0.4 | OPH Coravel |
| 50171.790 | -6.0 | 0.5 | -0.7 | -13.9 | 0.8 | -0.1 | OPH Coravel |
| 50197.830 | -6.0 | 0.5 | -0.8 | -15.6 | 0.8 | -1.7 | OPH Coravel |
| 52298.850 | -14.9 | 0.2 | -0.4 | -5.3 | 0.5 | -1.2 | Cambridge Coravel |
| 52321.820 | -14.8 | 0.2 | 0.2 | -3.1 | 0.5 | 0.5 | Cambridge Coravel |
| 52340.820 | -15.5 | 0.2 | -0.1 | -3.0 | 0.5 | 0.1 | Cambridge Coravel |
| 52448.080 | -18.5 | 0.2 | 0.3 | -0.1 | 0.5 | -0.7 | Cambridge Coravel |
| 52482.090 | -20.5 | 0.2 | -0.1 | 1.7 | 0.5 | -0.7 | Cambridge Coravel |
| 52515.120 | -22.4 | 0.2 | 0.1 | 3.8 | 0.5 | -0.8 | Cambridge Coravel |
| 52544.070 | -24.7 | 0.2 | -0.1 | 7.4 | 0.5 | 0.4 | Cambridge Coravel |
| 52565.050 | -26.6 | 0.2 | -0.4 | 9.0 | 0.5 | 0.3 | Cambridge Coravel |
| 52588.980 | -27.6 | 0.2 | -0.2 | 10.2 | 0.5 | 0.1 | Cambridge Coravel |
| 52612.940 | -26.6 | 0.2 | 0.0 | 8.3 | 0.5 | -0.9 | Cambridge Coravel |
| 52619.070 | -25.8 | 0.2 | 0.1 | 9.1 | 0.5 | 0.7 | Cambridge Coravel |
| 52625.760 | -25.1 | 0.2 | -0.2 | 8.0 | 0.5 | 0.6 | Cambridge Coravel |
| 52627.820 | -24.2 | 0.2 | 0.4 | 6.9 | 0.5 | -0.1 | Cambridge Coravel |
| 52643.760 | -21.6 | 0.2 | -0.2 | 3.0 | 0.5 | -0.5 | Cambridge Coravel |
| 52650.870 | -19.9 | 0.2 | 0.0 | 1.2 | 0.5 | -0.6 | Cambridge Coravel |
| 52662.870 | -17.4 | 0.2 | 0.1 | -0.9 | 0.5 | -0.1 | Cambridge Coravel |
| 52671.800 | -15.7 | 0.2 | 0.2 | -2.5 | 0.5 | 0.1 | Cambridge Coravel |
| 52683.850 | -14.4 | 0.2 | -0.4 | -4.2 | 0.5 | 0.5 | Cambridge Coravel |
| 52688.860 | -12.9 | 0.2 | 0.4 | -4.6 | 0.5 | 0.9 | Cambridge Corvael |
| 52712.790(*) | -11.6 | 0.5 | -0.8 | -6.3 | 1.2 | 2.0 | Cambridge Coravel |
| 52801.080(*) | -6.6 | 0.5 | 0.1 | -13.3 | 1.2 | -0.6 | Cambridge Coravel |
| 52834.090 | -6.4 | 0.2 | -0.3 | -14.2 | 0.5 | -0.9 | Cambridge Coravel |
| 52871.110 | -5.7 | 0.2 | 0.0 | -14.4 | 0.5 | -0.6 | Cambridge Coravel |
| 52900.120 | -5.6 | 0.2 | -0.1 | -14.1 | 0.5 | -0.1 | Cambridge Coravel |
| 52930.030 | -5.6 | 0.2 | -0.2 | -14.8 | 0.5 | -0.6 | Cambridge Coravel |
| 52970.940 | -5.2 | 0.2 | 0.0 | -14.5 | 0.5 | -0.2 | Cambridge Coravel |
| 53013.790 | -4.9 | 0.2 | 0.3 | -14.5 | 0.5 | -0.1 | Cambridge Coravel |
| 53060.830 | -5.0 | 0.2 | 0.2 | -15.1 | 0.5 | -0.7 | Cambridge Coravel |
| 53189.090 | -5.7 | 0.2 | -0.4 | -14.9 | 0.5 | -0.6 | Cambridge Coravel |
| 53248.070 | -5.5 | 0.2 | -0.2 | -14.6 | 0.5 | -0.4 | Cambridge Coravel |
| 53274.070 | -5.2 | 0.2 | 0.2 | -14.6 | 0.5 | -0.4 | Cambridge Coravel |
| 53304.010 | -5.3 | 0.2 | 0.1 | -14.6 | 0.5 | -0.5 | Cambridge Coravel |
| 53356.880 | -5.4 | 0.2 | 0.1 | -14.2 | 0.5 | -0.2 | Cambridge Coravel |
| 53593.130 | -5.7 | 0.2 | 0.4 | -13.5 | 0.5 | -0.1 | Cambridge Coravel |
| 53669.990 | -6.0 | 0.2 | 0.3 | -13.8 | 0.5 | -0.6 | Cambridge Coravel |
| 53763.780 | -6.6 | 0.2 | 0.0 | -13.4 | 0.5 | -0.5 | Cambridge Coravel |
| 53800.790(*) | -7.1 | 0.5 | -0.4 | -12.1 | 1.2 | 0.7 | Cambridge Coravel |
| 53945.130(*) | -6.2 | 0.5 | 0.9 | -12.6 | 1.2 | -0.3 | Cambridge Coravel |
| 54008.110(*) | -6.9 | 0.5 | 0.4 | -12.9 | 1.2 | -0.9 | Cambridge Coravel |
| 54067.000(*) | -7.4 | 0.5 | 0.1 | -12.8 | 1.2 | -1.0 | Cambridge Coravel |
| 54313.120(*) | -8.3 | 0.5 | 0.2 | -10.7 | 1.2 | 0.1 | Cambridge Coravel |
| 54691.140(*) | -11.2 | 0.5 | -0.6 | -6.7 | 1.2 | 1.7 | Cambridge Coravel |
| 54756.000(*) | -11.4 | 0.5 | -0.2 | -6.1 | 1.2 | 1.7 | Cambridge Coravel |
| 54806.990(*) | -12.3 | 0.5 | -0.7 | -5.5 | 1.2 | 1.8 | Cambridge Coravel |
| 54865.800(*) | -12.8 | 0.5 | -0.5 | -5.2 | 1.2 | 1.4 | Cambridge Coravel |
| 55055.110 | -15.0 | 0.2 | 0.3 | -3.7 | 0.5 | -0.4 | Cambridge Coravel |
| 55084.100 | -15.6 | 0.2 | 0.3 | -3.0 | 0.5 | -0.5 | Cambridge Coravel |
| 55117.010 | -17.1 | 0.2 | -0.2 | -2.1 | 0.5 | -0.6 | Cambridge Coravel |
| 55155.960 | -17.8 | 0.2 | 0.4 | 0.2 | 0.5 | 0.2 | Cambridge Coravel |
| 55185.870 | -19.3 | 0.2 | 0.2 | 0.9 | 0.5 | $-0.5$ | Cambridge Coravel |
| 55222.780 | -21.8 | 0.2 | -0.3 | 3.4 | 0.5 | -0.2 | Cambridge Coravel |
| 55259.810 | -23.7 | 0.2 | 0.4 | 7.0 | 0.5 | 0.6 | Cambridge Coravel |
| 55371.090 | -20.4 | 0.2 | 0.0 | 1.5 | 0.5 | -0.8 | Cambridge Coravel |
| 55407.120 | -13.7 | 0.2 | 0.2 | -4.8 | 0.5 | 0.0 | Cambridge Coravel |
| 55432.140(*) | -11.4 | 0.5 | -0.4 | -5.9 | 1.2 | 2.1 | Cambridge Coravel |
| 55538.960 | -6.4 | 0.2 | 0.0 | -13.7 | 0.5 | -0.7 | Cambridge Coravel |
| 55817.070 | -5.1 | 0.2 | 0.1 | -13.9 | 0.5 | 0.5 | Cambridge Coravel |
| 55892.950 | -5.1 | 0.2 | 0.1 | -14.1 | 0.5 | 0.3 | Cambridge Coravel |

Notes: (*) The RV data are derived from close blends.

Table 3 The Newly Derived and Historical Orbital Parameters and Masses of HD 8640

| Parameter | The present work | Griffin (2012) | Balega et al. (2006) |
| :--- | :---: | :---: | :---: |
| $V_{0}\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$ | $-9.57 \pm 0.03$ | $-9.57 \pm 0.04$ |  |
| $K_{1}\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$ | $11.16 \pm 0.05$ | $11.18 \pm 0.06$ |  |
| $K_{2}\left(\mathrm{~km} \mathrm{~s}^{-1}\right)$ | $12.30 \pm 0.09$ | $12.34 \pm 0.12$ |  |
| $\omega_{A}\left({ }^{\circ}\right)$ | $215.6 \pm 0.3$ | $215.2 \pm 0.5$ | $219.1 \pm 1.4$ |
| $e$ | $0.7433 \pm 0.0014$ | $0.7442 \pm 0.0020$ | $0.720 \pm 0.008$ |
| $P(\mathrm{~d})$ | $2722.4 \pm 0.7$ | $2722.0 \pm 1.0$ | $2666 \pm 40$ |
| $T$ (JD-2400000.5) | $52622.6 \pm 0.6$ | $52622.2 \pm 0.9$ | $49976 \pm 40$ |
| $a$ (mas) | $83.0 \pm 0.3$ |  | $87 \pm 2$ |
| $i\left(^{\circ}\right)$ | $50.9 \pm 0.5$ | $54.7 \pm 1.5$ |  |
| $\Omega\left(^{\circ}\right)$ | $151.3 \pm 0.3$ |  | $151.6 \pm 1.3$ |
| Orbital parallax (mas) | $16.4 \pm 0.2$ |  |  |
| $M_{1}\left(M_{\odot}\right)$ | $1.22 \pm 0.03$ | $1.06 \pm 0.06$ |  |
| $M_{2}\left(M_{\odot}\right)$ | $1.11 \pm 0.03$ | $0.96 \pm 0.06$ |  |



Fig. 2 Apparent orbit and the astrometric data of HD 6840. The solid ellipse is the newly derived apparent orbit and the dotted one is derived from Balega et al. (2006).

The effective temperature of $5956 \pm 35 \mathrm{~K}$ for the system was given by Ramírez et al. $(2012,2013)$. Considering the effective temperature of the system as that of the primary, we attempt to investigate the evolutionary status by comparing the $\left(\log T_{\text {eff }}, \log L / L_{\odot}\right)$ values of the component stars with the evolutionary model given by Mowlavi et al. (2012). We find that the primary is on the horizontal branch of the Hertzsprung-Russell diagram, so the mass and age of the primary are hardly influenced by the effective temperature. Then, we find a good match between the observation and evolutionary model with metallicity $Z=$ 0.01 (Mowlavi et al. 2012). The tracks representing masses $1.10,1.12,1.20$ and $1.22 M_{\odot}$ are shown by the solid lines in Figure 3, and the isochrones for $\log \left(\right.$ age $\left.\mathrm{yr}^{-1}\right)=9.7$ and 9.8 are also shown by the dashed lines in the same figure.

From Figure 3, the logarithm of the isochrone age of about 9.71 can be inferred, and the temperature of the secondary can be derived as $6240 \pm 35 \mathrm{~K}$ by the same isochrone age as the primary. Although we have found a good match between the observation and model with the value of metallicity $Z=0.01$, the value $Z=0.01$ is


Fig. 3 Evolutionary tracks and isochrones for the two component stars of HD 6840 (Mowlavi et al. 2012). The solid lines and dashed lines indicate the mass tracks of $1.10,1.12,1.20$ and 1.22 $M_{\odot}$ and the isochrones of $\log \left(\right.$ age $\left.^{\mathrm{yr}}{ }^{-1}\right)=9.7$ and 9.8 , respectively.
slightly different from the observation of $[\mathrm{Fe} / \mathrm{H}]=-0.38$ corresponding to $Z=0.0053$ (Ramírez et al. 2012, 2013).

In this work, we obtain the three-dimensional orbit of the system HD 6840 and preliminarily analyze the properties of its components by the stellar evolutionary model. In order to improve the precision of the orbit, interferometric observations are still needed to cover the whole orbit. On the other hand, in order to obtain the model-independent physical properties and test the stellar evolutionary model, high resolution and high signal-to-noise spectral observations are also needed and the composite spectra of the system are expected to be disentangled in the future.

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